

# **STATISTICAL SIGNAL PROCESSING APPROACH TO SEGMENT PRIMARY COMPONENTS FROM PATHOLOGICAL PHONOCARDIOGRAM (PCG)**

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June 2014

# **STATISTICAL SIGNAL PROCESSING APPROACH TO SEGMENT PRIMARY COMPONENTS FROM PATHOLOGICAL PHONOCARDIOGRAM (PCG)**

*A Thesis submitted in partial fulfillment of the requirement for the degree of*

Master of Technology  
In  
Electronics and Communication Engineering  
Specialization: Signal and Image Processing

*Submitted by*  
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June 2014



## **DECLARATION**

I hereby declare that

- 1) The work presented in this paper is original and has been done by myself under the guidance of my supervisor.
- 2) The work has not been submitted to any other Institute for any degree or diploma.
- 3) The data used in this work is taken from only free sources and its credit has been cited in references.
- 4) The materials (data, theoretical analysis, and text) used for this work has been given credit by citing them in the text of the thesis and their details in the references.
- 5) I have followed the thesis guidelines provided by the Institute.

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**2<sup>ND</sup> JUNE 2014**



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## **CERTIFICATE**

This is to endorse that the work presented in the thesis entitled **Statistical Signal Processing Approach to Segment Primary Components from Pathological Phonocardiogram** by **Diddi Sandeep Vara Sankar** is a record of an original research work carried out by him during 2013-2014 under my supervision and guidance in partial fulfillment of the requirement for the award of the degree of Master of Technology in Electronics and Communication Engineering with Signal and Image Processing as specialization, National Institute of Technology, Rourkela. To the best of my knowledge, this thesis has not been submitted for any degree or diploma elsewhere.

Place: NIT Rourkela

Date: 02-05-2014

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Assistant professor

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## ABSTRACT

Cardiac disorders has become pretty common in the current world. On an average 30% of the global deaths are due to cardiovascular diseases. This signifies the need for having research with greater concentration in this field. Despite of the availability of many advanced techniques like electrocardiography (ECG), Echocardiography and Carotid pulse, listening to the heart sounds has become one of the orthodox approach which is being performed from long ago, often named as auscultation methodology or Phonocardiogram. This methodology is the primary tool for the health care physicians to screen the patients for heart pathology. However, to master, it needs a lot of experience and knowledge. Yet the non-availability of advanced techniques at every door step and its cost made this orthodox approach to survive. The proposed study is to make the health care physicians to diagnose the pathology using phonocardiography in an effective manner. The study uses the statistics of the signal information in the form of variance. The proposed technique uses filtering and decimation as preprocessing method to limit the low frequency noises/disturbances and to concentrate only on the components of interest (i.e. S1 and S2). The preprocessed signal is wavelet analyzed and synthesized followed by principal component analysis to extract necessary features which resembles the information of S1 and S2. A proposed splitting algorithm is processed to the featured signal to separate the phonocardiogram signal into series of cardiac cycles and energy envelope is calculated for the same featured signal. By using the information of the cardiac cycles and energy envelopes, segmentation of S1 and S2 from pathological phonocardiogram is performed. The results show that the proposed technique does not rely on any time-frequency parameter which effects the performance of the study. Hence a novel technique based on statistical analysis has been proposed to detect the primary components (S1 and S2) from pathological phonocardiogram with less computational effort and better accuracy.

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# CHAPTER 1

# INTRODUCTION

# 1. Introduction

Heart sounds (HSs) are generated due to flow of blood in the heart. However, these sounds reflect the turbulence created by the beating heart due to opening and closing of the heart valves. Auscultation of heart sounds is a primary tool in cardiac diagnosis. Research has demonstrated poor auscultation skills among health care physicians with correct diagnosis rates as low as 20%. While advanced techniques such as Doppler-electrocardiography (ECG), echocardiography and magnetic resonance imaging (MRI) exist, they are costly and not available at every place in many developing countries. From a different perspective, monitoring the cardiac sound signals which are generated due to mechanical vibrations organisms, it is evident that HS auscultation is the fundamental tool in diagnosis of heart diseases [1]. But, the auscultation of cardiac sound signals requires lots of practice and experience with either an electronic stethoscope or conventional acoustic. Although the stethoscope is the symbol of doctors, in actuality primary health care physicians have poor auscultation skills. This ensures the need for the physicians of primary health care to improve their auscultatory skills which is very strong at primary screening and for the general users to perform auscultation at home (Reed T R, Reed N E, & Fritzson, 2004) [2].

Heart murmurs are the additional sounds caused due to turbulence created by the heart due to some abnormal activity in the valves. Pathological murmurs are produced by the blood flow through narrowed (stenosed) valves, back (regurgitant) flow through inept valves or through septal defects. Normally, each heart sound consist of two regularly repetitive thuds called as primary components (S1 and S2). The time interval between primary components (S1 and S2) is systole and that period is called systolic period, while the interval between S2 and next S1 is diastole and that period is called diastolic period. S1 corresponds to the closure of the tricuspid and mitral valves at the end of diastole, while S2 implies the closing of the aortic and pulmonary valves at the end of systolic phase. In addition to primary components, there were two weak sounds that appear along with S1 and S2 in some conditions called S3 and S4. Generally, in most of the cases S3 is an innocent murmur but S4 is always pathologic. In case of pathology, any dysfunction in the valvular heart produces additional sounds along with the primary heart sounds which have their own pattern. Valvular heart disease are caused due to stenosis and regurgitation. When stenosis occurs the corresponding valve opening becomes narrower which increases the pressure in that

particular chamber. Due to increase in pressure the valve muscle becomes stiffer and leaflet loses its agility resulting in reduced amount blood flow through it. In case of regurgitation, the valve leaflet doesn't close properly letting the blood to flow backward across the valve which increase the burden in that valve. This kind of flow of blood is referred to as regurgitant flow. Most of the defects have murmurs as systolic ejection murmur (e.g. Aortic stenosis), mid-systolic murmur (e.g. pulmonic stenosis) pan systolic murmur (e.g. mitral regurgitation), mid diastolic rumbling murmur (e.g. Mitral stenosis), early diastolic murmur (e.g. aortic regurgitation, pulmonary regurgitation).

These individual patterns of murmur distributions resemble the need for diagnostic aid in this area, both for training and clinical use. The first step in developing such a system is the segmentation of heart sounds into diagnostically relevant components. This is a challenging task because of the non-stationary nature of heart sounds and variability seen between the patients (even with in the same patient over time). So automatic analysis and diagnosis of HSs is required and many researchers are paying much concentration on this field [2].

Many have studied the application of short time Fourier transform (STFT) as one of the way to account for the non-stationarity of the signal. A basic understanding is provided on non-stationary nature of the HSs using short time Fourier transform (STFT) in time-frequency plane by Abdelghani Djebbari and Fethi Bereksi reguig [3] which gives a trade-off between time and frequency resolution due to its fixed window length. The trade-off due to fixed window length is eliminated by the introduction of wavelet transform. J.J Lee, S.M Lee, I.Y kim, H.K Min and S.H Hong [4] showed the comparison between STFT and wavelet transform and stated that wavelet transform acts as the primary step in the feature extraction of HSs.

A method for segmenting HS components based on HS envelopogram is proposed by H. Liang, S. Lukkarinen and L. Hartimo [5] provides a good idea for understanding structure and characteristics of HS signal. Shannon energy is used as a medium for calculating the envelope of the energy of HSs. The algorithm shows promising results but failed in the presence of high intensity murmurs and/or noises.

Time-frequency analysis are probably the most widely used techniques for analyzing HS signals. Segmentation of some pathological PCG signals using time-frequency approach is proposed D. Boutana, M. Benidir, and B. Barkat [6]. In addition to segmentation the work permits

to extract useful information in terms of features for diagnosis and recognition of pathology. The method gives promising results but restricted to abnormalities which have murmur concentration only in systolic phase.

Time-frequency analysis does not work well in cases where primary components and murmurs are inseparable, so a probabilistic approach using hidden Markov model (HMM) was proposed by L. G. Gamero, and R. Watrous [7], to model systolic and diastolic durations, which are further used to detect the presence of primary components (S1 and S2). However, the study needs the QRS peak values of the simultaneous ECG recording as reference for detection of HSs without which the algorithm doesn't work.

Although a model-based approach has the ease of algorithmic implementation, it is sensitive to modelling (such as the choice of the wavelet) and model parameter estimation (like determining the parameters of an HMM). So a homomorphic filtering based self-organizing probabilistic model approach was proposed by Gill D, Gavrieli N, and Intrator N [8], to identify and detect primary HSs. Homomorphic filtering is advantageous due to its scalable smoothing property and its ability in handling the splitting problem and serrated peaks and noisy environment.

Wavelet analysis has become one of the extensively used technique in analysing PCG signals. Wavelets has the capability of analysing the signals, extracting features, detecting specific events of interest, classification and component segmentation. The study of J.J Lee & co... discussed above [4] has given clear understanding of the capability of wavelets in extracting the features. Christer Ahlstrom *et al* in [9] proposed a feature based systolic murmur classification which uses wavelet as one of the deciding factor for detecting murmur and segmenting HSs. M.A.R Santos and M. Souza in [10] demonstrated that Daubechies (4-19), Meyer and Morlet are the family of wavelets which are capable for analysing PCG signals. These wavelets have the property of orthogonality which reduces the correlation problems.

## 1.1. Motivation

Detection of cardiac disorders at the early stages makes the people to get rid of those vicious problems and lead a peaceful life. When cost effectiveness is of concern, ECG and Echocardiogram cannot be afforded by the common people for general check-up and the availability of these facilities are restricted to only towns and cities. These difficulties makes the



general auscultation methodology to become easiest diagnostic technique for pathology detection. For the last few decades, researches have been made to device techniques to segment primary components from pathological phonocardiogram (PCG). Some techniques provides better segmentation results but on the cost of algorithm complexity and price. These researches and the typical behavior of heart sounds (HSs) gives motivation to work for the betterment of the available methods and overcome its drawbacks in the novel technique.

## 1.2. Objective

The main objective of this work is to propose a robust segmentation algorithm based on statistical signal processing which, is capable of identifying key cardiac events, reduces the computational complexity and has ability to address almost all cardiac disorders. The study uses statistical parameters in segmenting two primary components (S1 and S2) from others. The presented segmentation technique uses a proposed splitting algorithm to separate the PCG signal into series of cardiac cycles and also to identify the boundaries of the primary components.

## 1.3. Thesis Outline

The thesis is organized into 5 chapters. The first chapter speaks about, the introduction of heart sounds and some of the discussions made by the researchers in their studies. The second chapter gives a brief idea of the anatomy of heart sounds and their corresponding murmurs. The third chapter briefs the background of the basic concepts used in this study. The fourth chapter describes the proposed techniques and their corresponding results and finally discussion on the entire study is made in the fifth chapter followed by conclusion to the complete work and references.

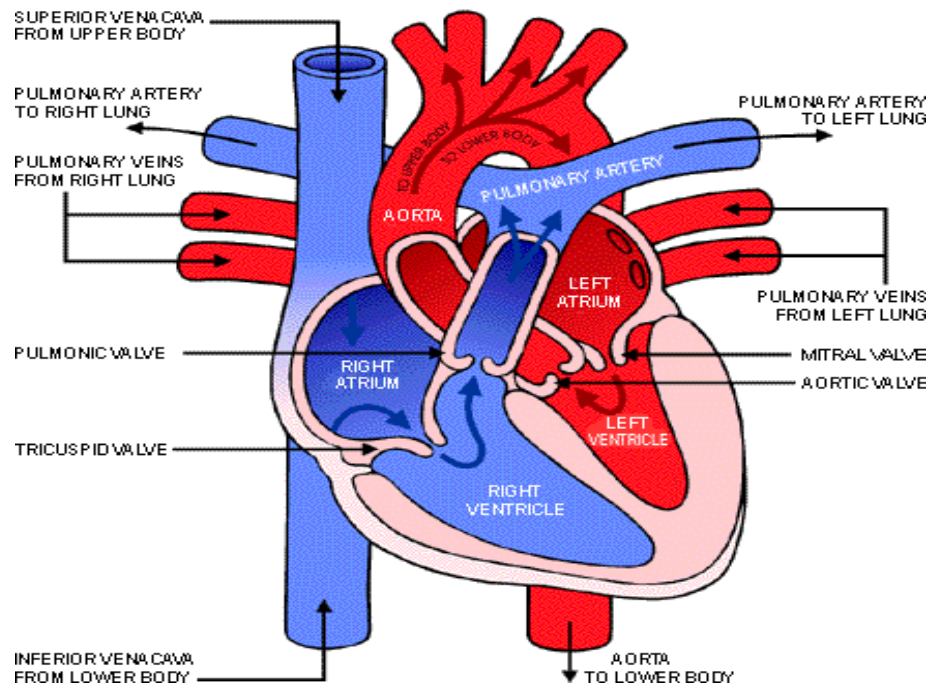
# CHAPTER 2

# CARDIAC ANATOMY

## 2. Cardiac Anatomy

### 2.1. Physiology of heart

The heart is a powerful muscle which serves as a pump propelling blood through the circulatory system [11]. The contraction of the heart is due to electrical pulse generated by the sinoatrial node. When the heart contracts, the blood flows through the valves of atria to the ventricles and eventually out through the body. Each heart consists of four chambers, two upper and two lower. The upper chamber consists of left atria and right atria, and the lower chamber consists of left ventricle and right ventricle. Each heart is divided into two phases namely, systolic and diastolic. The contraction of the heart in which blood is pushed out of the heart into the arteries is called systole and relaxation of heart in which ventricles are filled with blood is called diastole i.e. blood enters from ventricles to lungs to get oxygenated, then to rest of the body during systole and from auricles to ventricles during diastole. Each heart chamber has four valves which acts as a gateway between the chambers. The four valves are grouped into two; atrioventricular valves (tricuspid and mitral valve) and semilunar valves (pulmonary and aortic valves), which prevents the reverse flow of blood. Deoxygenated

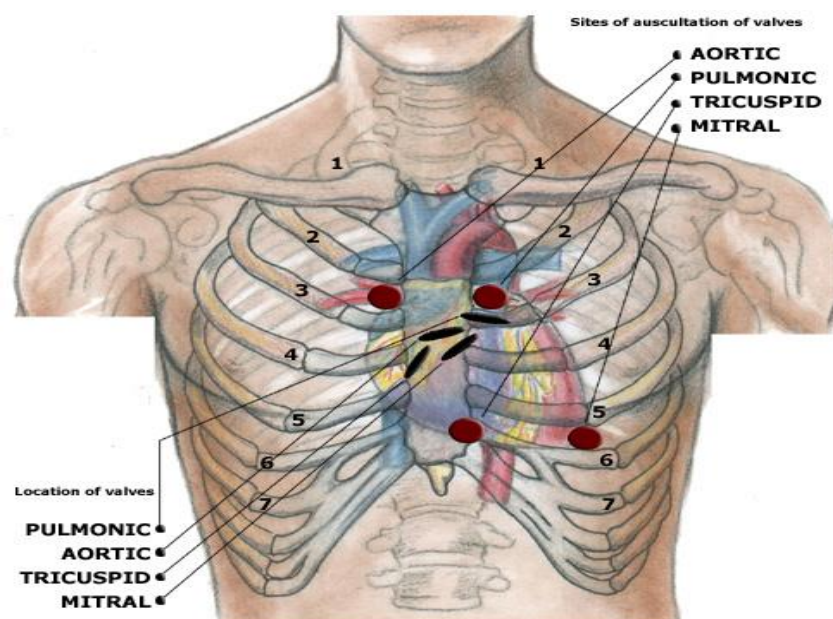


**Fig 2.1 Typical view of Heart.**

blood from the body parts enters the right atrium and is passed to the right ventricle through the tricuspid valve and is ejected into the lungs through pulmonic valve for oxygenation. The Oxygenated blood from the lungs enters the left atrium is passed to left ventricle through mitral valve and is then ejected into the aorta.

## 2.2. Heart Sounds

Heart sounds are a kind of noises generated due to the flow of blood in the heart through the valves. Furthermore, these noises reflect the turbulence created when the heart valve closes suddenly. Appreciating heart sounds is very difficult and it requires lots of experience to master it. It is necessary to listen for a long time to each component of the cardiac cycle at each location of auscultation. Normally, for a healthy person each heart beat consists of two heart sounds often we describe them as lub and dub, but in medical terminology the word lub is named as S1 (first heart sound) and the word dub is named as S2 (second heart sound). These sounds are produced due to the closure of the four valves discussed above. In abnormal cases, along with the normal heart sounds, one may incur with a variety of extra sounds which include S3, S4, murmurs, gallops etc. Here I am going to discuss each type of sounds (including normal and abnormal) separately and their possible auscultation positions [11].



**Fig 2.2 Location of valves and their auscultation positions.**

## 2.3. Primary Heart Sounds

### 2.3.1. First heart sound (S1):

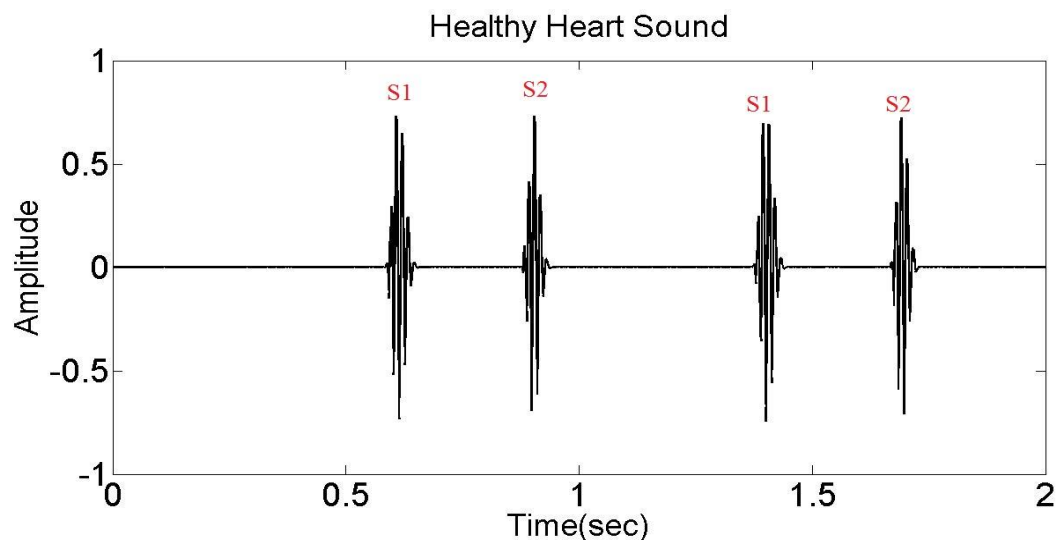
It is a sound which is caused due to closing of Mitral and Tricuspid valves at transition from diastole to systole. It forms *lub* sound.

- 1) S1 is louder than S2
- 2) Intensity of S1 is predominantly determined by its Mitral valve component. Hence it is loudest at Apex region.

### 2.3.2. Second heart sound (S2):

It is a sound which is caused due to closing of Aortic and Pulmonic valve at transition from systole to diastole. It forms *dub* sound.

- 1) High pitch sound, Best heard at Upper sternal boarder.
- 2) Normally split in S2 occurs during inspiration due to contraction time difference between AV and PV.



**Fig 2.3 Healthy PCG signal.**

## 2.4. Extra Heart Sounds

### 2.4.1. Third heart sound (S3):

This is also named as third heart sound. S3 sound is a low pitched early diastolic sound. S3 sound may be innocent or pathological. The cause for the sound may be due to abrupt deceleration of blood as it attempts to fill the failed ventricle resulting in vibration of the ventricular walls which resembles pathology. The S3 sound in youth, women during pregnancy and in athletes is called innocent murmur.

#### Auscultation finding:

Heard clearly at apex with patient lying in left lateral decubitus position.

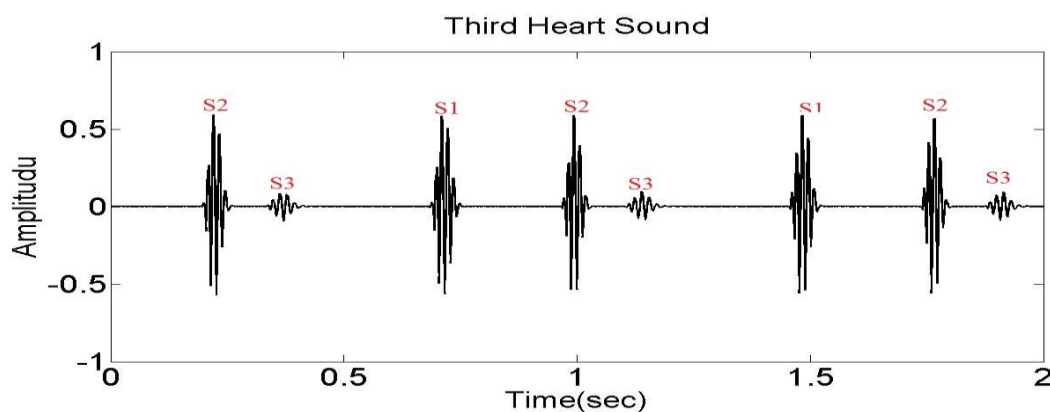


Fig 2.4 PCG signal for 3<sup>rd</sup> HS.

### 2.4.2. Fourth heart sound (S4):

S4 is also named as fourth heart sound. S4 is a sound heard when the blood hits the distended left ventricle. It is a low pitched late diastolic sound or a pre-systolic sound. It is always pathologic and is caused by atrial contraction into a stiff and non-compliant ventricle.

#### Auscultation finding:

Heard clearly at apex with patient lying in left lateral decubitus position with holding of breath.

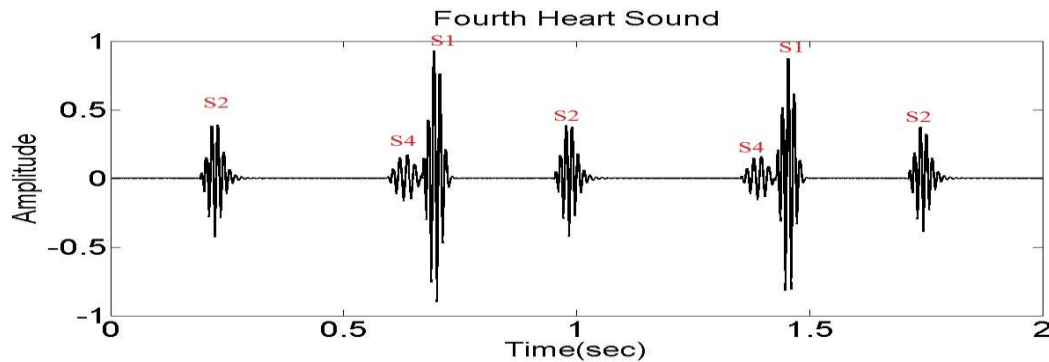


Fig 2.5 PCG signal for 4<sup>th</sup> HS.

## 2.5. Murmurs

### 2.5.1. Aortic Stenosis

Aortic stenosis is a pathology in which aortic valve is narrowed and the blood flow would be reduced which leads to angina followed by syncope, dyspnoea and pulses tardus. As the aortic valve gets narrowed the left ventricular muscle becomes thicker and thicker and produces more pressure in the left ventricle than its volume.

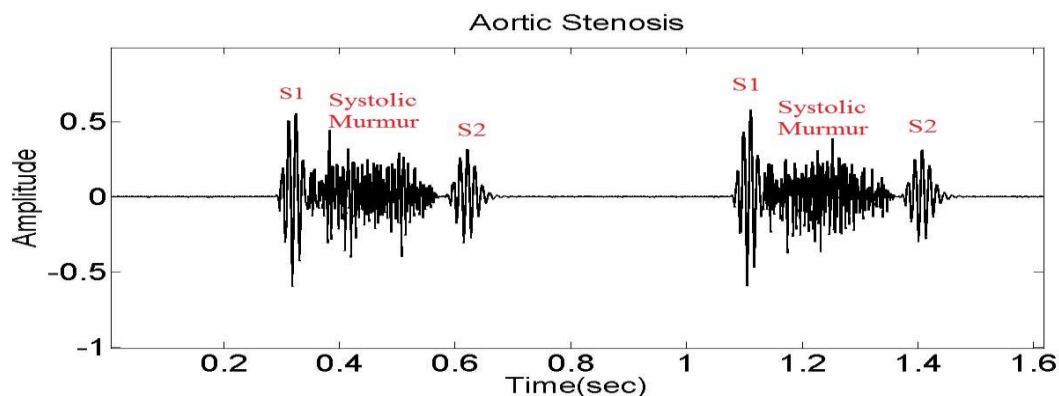


Fig 2.6 PCG signal for aortic stenosis.

#### Symptoms:

Angina – for mild cases (Mean survival < 5years)

Syncope – for severe cases (Mean survival < 3 years)

Congestive Heart failure (CHF) – for worst cases (Mean survival < 2 years)

### Causes:

Unicom or bicuspid valve instead of tricuspid valve, Calcification, Reverse split of S2

### Auscultation findings:

Type of murmur heard is **Crescendo-decrescendo** murmur. It is best heard around 2<sup>nd</sup> Right Intercostal Space.

S4 sound can also be heard in some conditions due to stiffness of LV which is of low frequency. This is heard only when there is no Atrial Fibrillation and it is best heard at **Apex** region.

## 2.5.2. Mitral Stenosis

The mitral valve is situated in the left side of the heart between left atrium and left ventricle. The stenosis in the mitral valve means narrowing of the valve which is responsible for the flow of blood. When the valve starts narrowing the left atrial pressure starts increasing which results in increased pulmonary capillary wedge pressure. Mean survival without any surgery is 3 years.

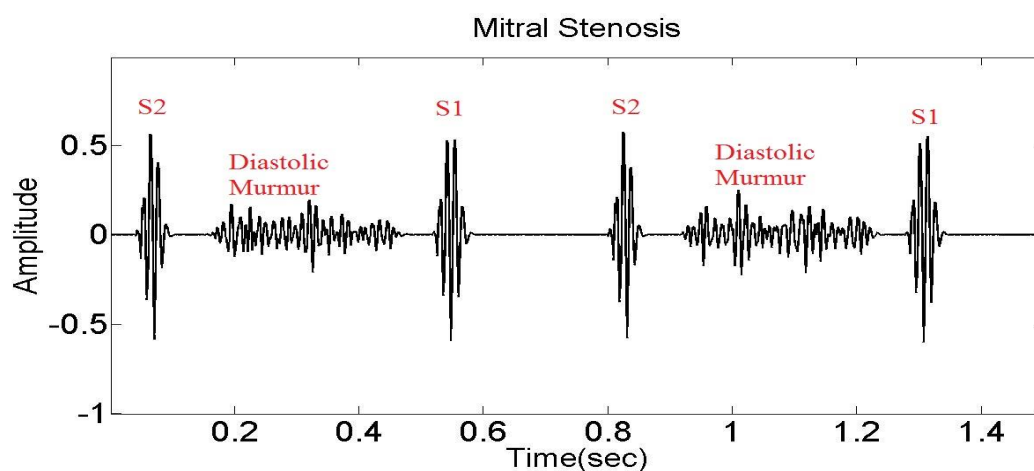


Fig 2.7 PCG signal for mitral stenosis.



### Causes:

Main cause is rheumatic

Other causes: congenital, amyloidosis, malignant carcinoid, left atrial myxoma.

### History:

Orthopnea, Paroxysmal Nocturnal Dyspnea (PNA), Palpitation and Angina

### Auscultation findings:

Loud S1, Opening snap, Mid Diastolic Murmur (MDM), Pulmonary Ejection sound (PES),  
Right ventricular 3<sup>rd</sup> heart sound.

## 2.5.3. Mitral Regurgitation

Regurgitation means reverse flow (back flow). Mitral Regurgitation (MR) is a condition where some of the blood flows back to the Left Atrium (LA) due to narrowed mitral valve. There are two types of regurgitations.

- 1) Chronic MR
- 2) Acute MR

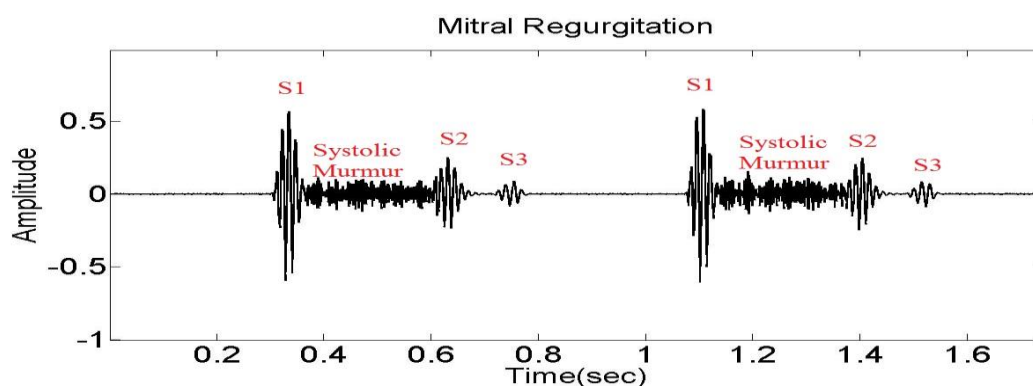


Fig 2.8 PCG signal for mitral regurgitation.

### **Chronic MR:**

It is a gradual onset or development kind of pathology. It allows adaptation. Patient with this may only have Palpitation, other than this they may not have any symptoms for long time.

#### **Causes:**

Rheumatic, Mitral valve prolapse, Cleft MV (congenital condition)

### **Acute MR:**

In this Abrupt volume is dumped into Left Atrium (LA) and there is no time for adaptation. It is mainly seen in 'Ischemic Heart Disease' situation and infective 'Endocarditis' or 'Prosthetic Valve Malfunction'. There exist a sudden fall in forward stroke volume.

#### **Causes:**

Ischemic Heart Disease, Posterior Papillary muscle

### **History:**

#### **Chronic MR:**

Palpitation, Breathlessness on effort, Orthopnea- PND, Pedal Edema

#### **Acute MR:**

Pulmonary edema, Breathlessness

#### **Auscultation findings:**

Soft S1, S3 sound can be heard, Pan Systolic murmur at Apex, Mid Systolic murmur at pulmonary area, Pulmonary Ejection sound.

## **2.5.4. Tetralogy of Fallot**

It refers to 4 things that happens in the heart. Pulmonary stenosis, Right Ventricular Hypertrophy, Overriding of Aorta and Ventricular Septal Defect.

## Pulmonic stenosis

Pulmonic stenosis occurs due to septum occurred between the right and left ventricles. The septum allows the deoxygenated blood to flow from tight ventricle to the left ventricle which results in the narrowing of the pulmonic valve space.

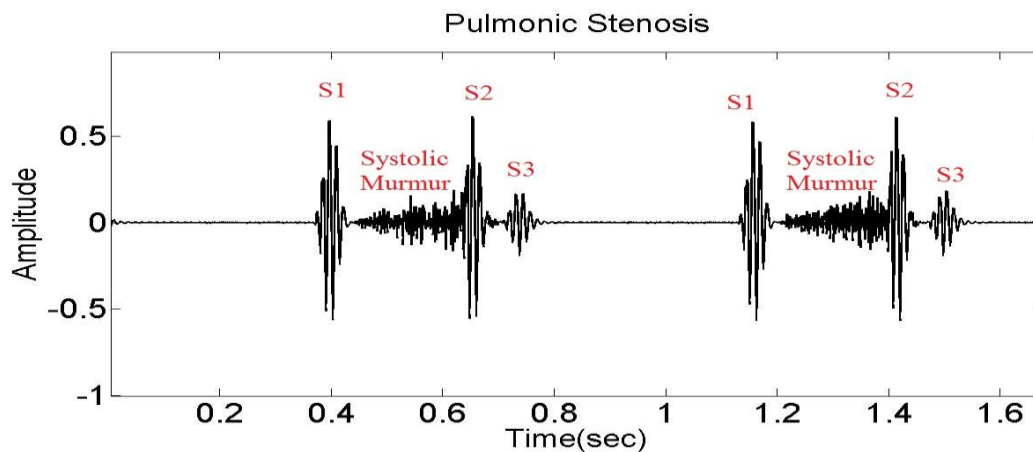


Fig 2.9 PCG signal for pulmonic stenosis.

## Right Ventricular Hypertrophy

As the valve space becomes narrowed due to pulmonic stenosis, the right ventricle needs to work hard to pump blood via narrowed pulmonic valve which results in enlargement of the ventricular muscle (hypertrophy) called right ventricular hypertrophy.

## Ventricular Septal Defect

A hole is formed between right ventricular and left ventricular chambers due to pulmonic valve stenosis. This septum allows de-oxygenated blood from right ventricles to left ventricle and mixes with the oxygenated blood coming from left atrium.

## Overriding of Aorta

The mixed blood in left ventricle should pass through the aortic valve, but the aortic valve is not capable of allowing that huge amount of blood at a time, so there occurs overriding problem which we call as overriding of aorta.

### Causes and symptoms:

Only possible cause is congenital and the symptoms may be dyspnea, poor weight gain, cyanotic and tet spells.

### Auscultation finding:

Pulmonic stenosis can be known physically by examining for the harsh systolic ejection murmur at the 'upper left sternal boarder'.

## 2.5.5. Aortic Regurgitation

Aortic regurgitation is a condition is a condition in which the valve doesn't close tightly. The valve allows some of the blood to flow back to that was just pumped out of your heart's main pumping chamber (left ventricle) to leak back into it.

### Causes:

Congenital heart defect, valve deterioration with age, rheumatic fever, endocarditis.

### Symptoms:

Fatigue and weakness at work effort

Shortness of breath when you lie flat.

Fainting, Irregular pulse (arrhythmia).

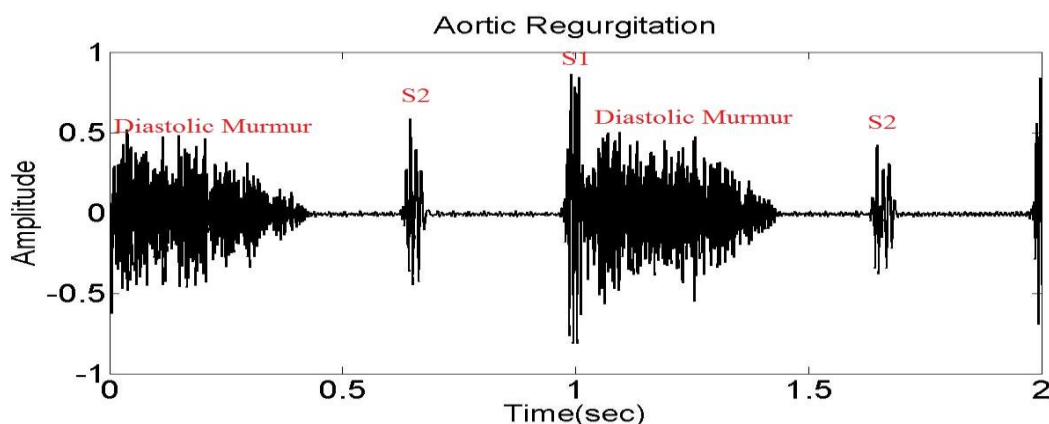


Fig 2.10 PCG signal for aortic regurgitation.

### 2.5.6. Tricuspid Stenosis

Tricuspid stenosis occurs when the valve doesn't open correctly in the tricuspid region. It always contains opening snap with a rumbling diastolic murmur along with wide split of S1. It may occur along with the mitral stenosis in some cases.

#### Auscultation finding:

It is best heard at the left sternal boarder.

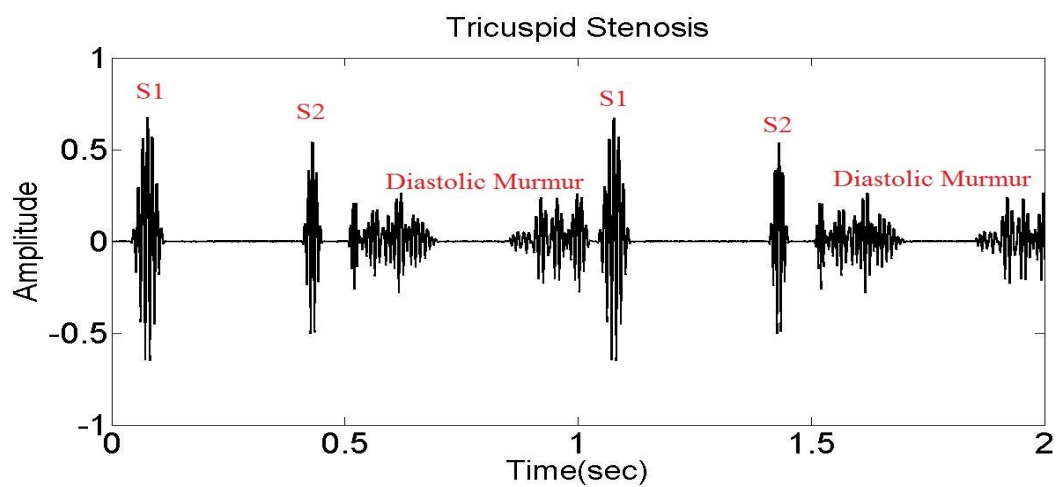


Fig 2.11 PCG signal for tricuspid stenosis.

## CHAPTER 3

# THEORETICAL BACKGROUND

### 3. Basic Theory

Signals carries prodigious amounts of data in which finding an important information is more difficult. It is necessary to process the signal in such a way that only few coefficients reveals the necessary information. These requirements opened the door for the discovery of huge jungle of new transforms. In this work, to segment heart sound signals an extension of methods based on time-frequency will be investigated. In order to have a successful segmentation algorithm, it is necessary to understand the basic concepts behind the techniques. This chapter constitutes fundamentals of Fourier theory followed by time-frequency analysis like windowed Fourier transform and Wavelet analysis. Finally it will be concluded with principal component analysis concept.

#### 3.1. Fourier Analysis

Fourier analysis is useful everywhere in the fields of mathematics and physics because the time invariant convolution operators are diagonalized [12]. It is a method which defines the periodic waveforms by the sum of trigonometric functions. The representation of the Fourier analysis for any energy function  $x(t)$  which is of finite duration is given by sum of sinusoids  $e^{j\omega t}$  as:

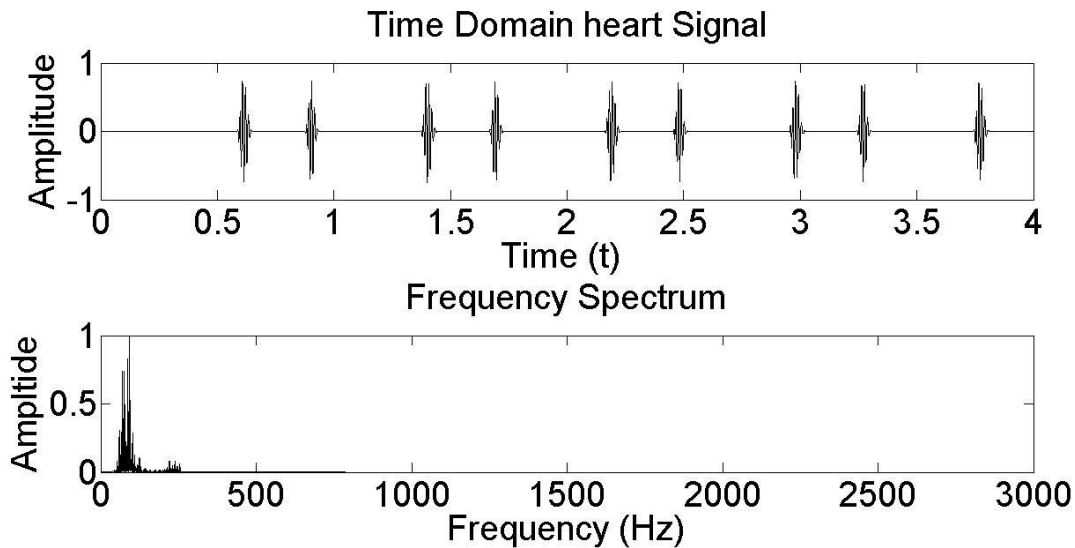
$$x(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} x(\omega) e^{j\omega t} d\omega \quad (3.1)$$

The amplitude  $x(\omega)$  for each of the sinusoidal wave function  $e^{j\omega t}$  is equal to correlation of  $e^{j\omega t}$  with  $x$ , which can also be called as Fourier transform:

$$x(\omega) = \int_{-\infty}^{\infty} x(t) e^{-j\omega t} dt \quad (3.2)$$

The more regular the function  $x(t)$ , the faster will be the decay of the amplitude  $|x(\omega)|$ , when the frequency of  $\omega$  is increased.

These pair of equations are called Fourier transform pair. The Fourier transform gives good results as long as the signals are uniformly regular or linearly time-invariant. But when the signals exhibit transient behavior Fourier transform becomes a heavy tool which requires so many coefficients to represent a local event. So Fourier transform cannot be used in the areas where representing local information is of concern which is the case for heart sounds. Fig 3.1 is a plot of a heart sound for normal patient and its Fourier transform. The transform only provides information in terms of frequency but loses its time information. Heart sound signals are a kind of signals where abrupt changes, positions of the cardiac events, trends plays an important role in segmentation of primary components which cannot be detected using Fourier analysis. Fig 3.1 shows the Fourier transform of the normal patient which gives only the frequency content.



**Fig 3.1. Healthy HS signal and its Fourier transform.**

### 3.2. Time-Frequency Analysis

In the field of signal processing, time frequency analysis is a study of a signal in both time and frequency domains. A 1-dimensional view may not give required information where both timing and frequency are of much concern. For those cases a transform which gives information in both time and frequency is required, here comes the concept of time frequency analysis. This

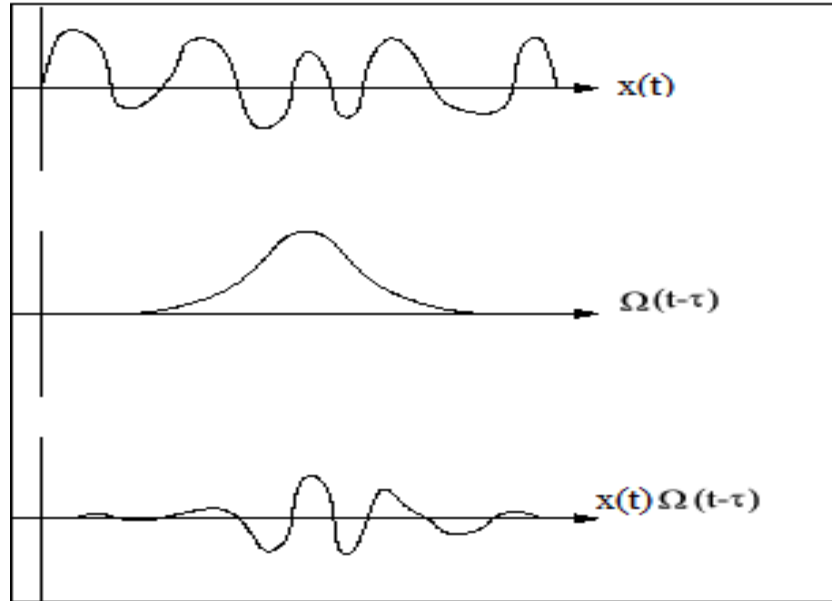


analysis uses time localization technique which plays an important role in speech and sound processing. The main issue is to understand how to adapt time-frequency component to signal processing. In this context Heisenberg uncertainty principle plays a promising role.

### 3.2.1. Short time/term Fourier transform

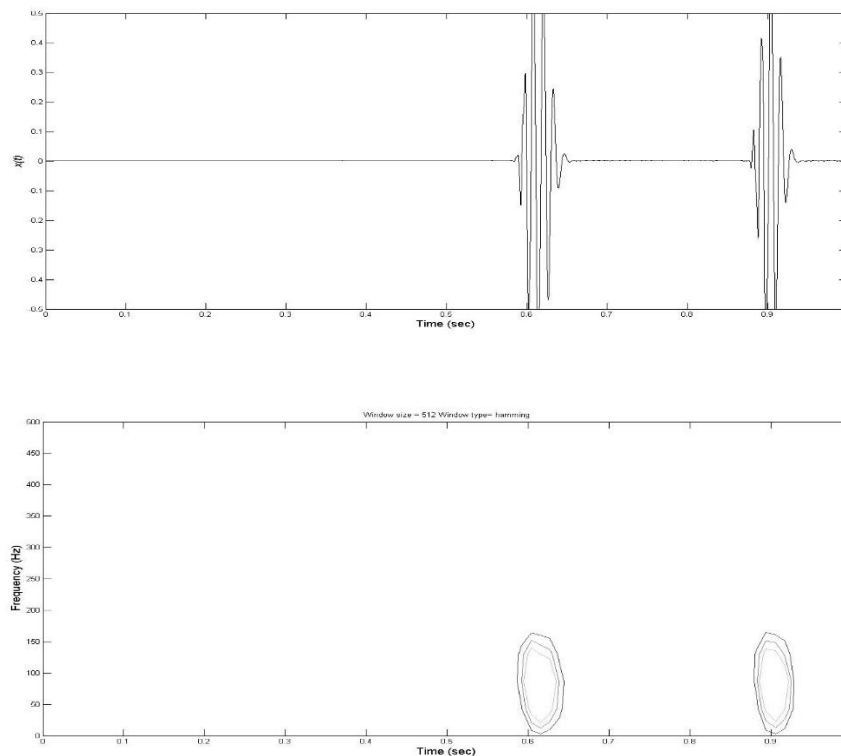
It can also be named window Fourier transform. A Short time/term Fourier transform (STFT) is constructed by translating a windowed function  $\Omega(t)$  in both time and frequency domains. The function  $\Omega(t)$  has a time translation by  $\tau$  and frequency by  $\alpha$ . The analysis is done using Fourier transform by assuming stationarity in finite segment of signal. The STFT projects  $x$  on each of the window function  $\Omega(\tau, \alpha)$ :

$$sx(\tau, \alpha) = \int_{-\infty}^{\infty} x(t)\Omega(t-\tau)e^{-i\alpha t} dt. \quad (3.3)$$



**Fig 3.2. Short time Fourier transform**

The window function  $\Omega(t)$  which is being analyzed is of fixed width. The window is a sliding function which slides along the time axis by  $\tau$ . This procedure is shown in fig 3.2. Hence, it is effective as long as the signal doesn't have any variable time-frequency resolutions. The heart sounds on the other side have structures with variable time-frequency resolutions. So STFT can only work for the cases which have constant time-frequency resolutions but not for varying ones. This problem can be handled by the wavelets.



**Fig 3.3. STFT for a healthy heart sound using Hamming window of size 512.**

### 3.2.2. Wavelet Analysis

Similar to Fourier analysis, wavelets also works to obtain singularity in a signal but wavelets uses localized events to represent the signal using only few coefficients. Unlike STFT, wavelet transform employs a windowing technique which is of variable width. The width

variability allows wavelets to work for different frequency resolutions. Based on the applications, wavelets are divided into two types: continuous and discrete wavelet transform.

### 3.2.2.1. Continuous wavelet transform

Wavelets offer the best representation for non-stationary signals. Here, large amplitude wavelet coefficients can detect and measure short high frequency variations because of the narrow time localization at high frequencies, so it gives better time resolution and at low frequencies their time resolution is lower, but they have a better frequency resolution. This modification of time and frequency resolution is adapted to represent sounds with sharp attacks or signals that have much frequency variations. These sharp attacks and high frequency variations are the exact characteristics of a HS signal.

A wavelet is constructed from a mother wavelet  $\psi$  of zero average which is dilated with a scale parameter  $s$ , and translated by  $\tau$  :

$$\int_{-\infty}^{\infty} \psi(t) dt = 0, \quad (3.4)$$

The continuous wavelet transform of  $x$  at any scale  $s$  and position  $\tau$  is the projection of  $x$  on the corresponding wavelet coefficient:

$$wx(\tau, s) = \int_{-\infty}^{\infty} x(t) \frac{1}{\sqrt{s}} \psi^* \left( \frac{t - \tau}{s} \right) dt. \quad (3.5)$$

It represents one-dimensional signals by highly redundant time-scale coefficients in  $(\tau, s)$  [12].

The scale parameter,  $s$ , is inversely proportional to the frequency which is defined as

$$s = \frac{1}{\omega} \quad (3.6)$$

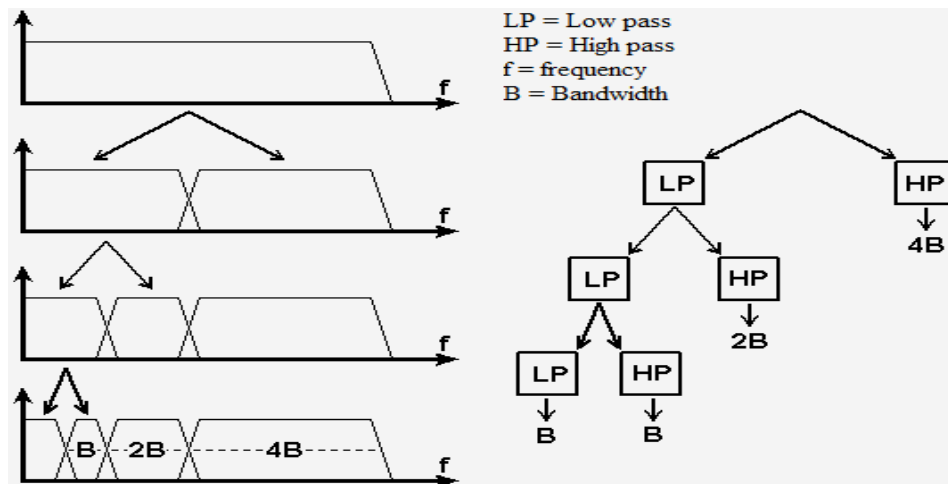
Where  $\omega$  is the frequency in Hertz.

From the wavelet perspective, scaling factor either dilates or compress the wavelet. Larger scales dilate the wavelet which highlights the slow variation activities in the signal and small scales compress the wavelet which retrieves the transient behaviour of the signal. The continuous wavelet

transform measures the similarity between the signal and the wavelet by continuously translating and scaling the mother wavelet. So to represent the coefficients an infinite number of wavelets are required which increases the redundancy and hence is impractical. It also uses 2-Dimension for dealing with 1-Dimension entity which gives extreme redundant information. Discrete wavelet transform works for those cases where redundancy is of much concern.

### 3.2.2.2. Discrete wavelet transform

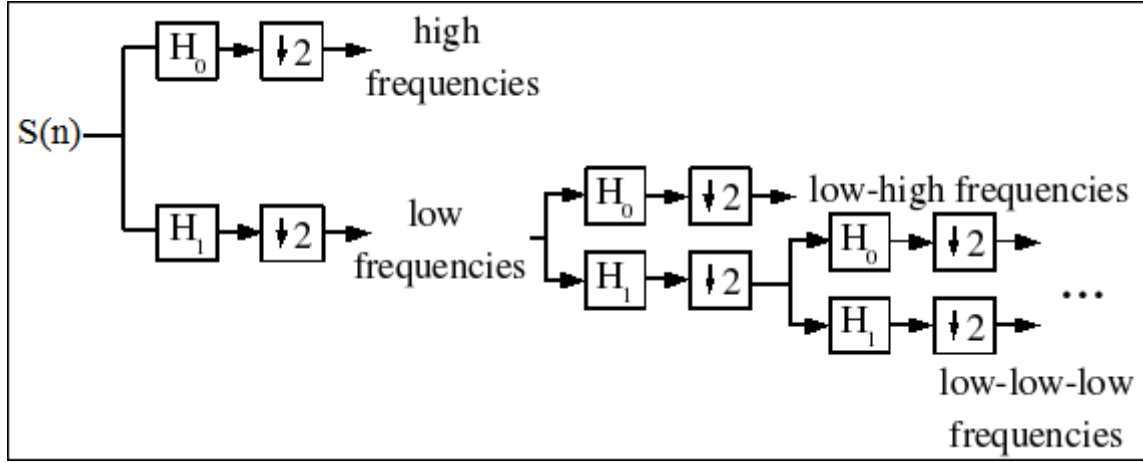
Continuous Wavelet transforms acts as filters in both analysis and synthesis which we call as dyadic discretization. Discretization of scale parameter is equivalent to constructing filter banks. In these cases each wavelet filter bank acts as a band pass filter which allows only certain band of frequencies. Dyadic discretization is a process in which the scale parameter of the wavelet is taken as powers of 2 i.e. the translation by a factor of 2 stretches the frequency by a factor of 2 and shifts the frequency component by a factor of 2. Here each filter bank should be non-overlapping with other filter banks. Distinct range of frequencies are covered by each wavelet where each step has a bandwidth reduction by a factor of 2 which can be seen in Fig 3.4.



**Fig 3.4. Wavelet filter bank.**

The discrete wavelet transform is a combination of consecutive low pass and high pass filters. Each filter divides the input signal into two half band frequencies, one half band towards low pass filter denoted by  $H_1$  and other half band towards high pass filter denoted by  $H_0$ . The low pass filter extracts the lower half of the frequencies which is called as approximation information

and high pass filter extracts upper half of the frequencies which is called as detail information. A three level wavelet decomposition is shown in Fig 3.5.



**Fig 3.5. Implementation of three level wavelet decomposition.**

The expression for one level decomposition is given by the following equation:

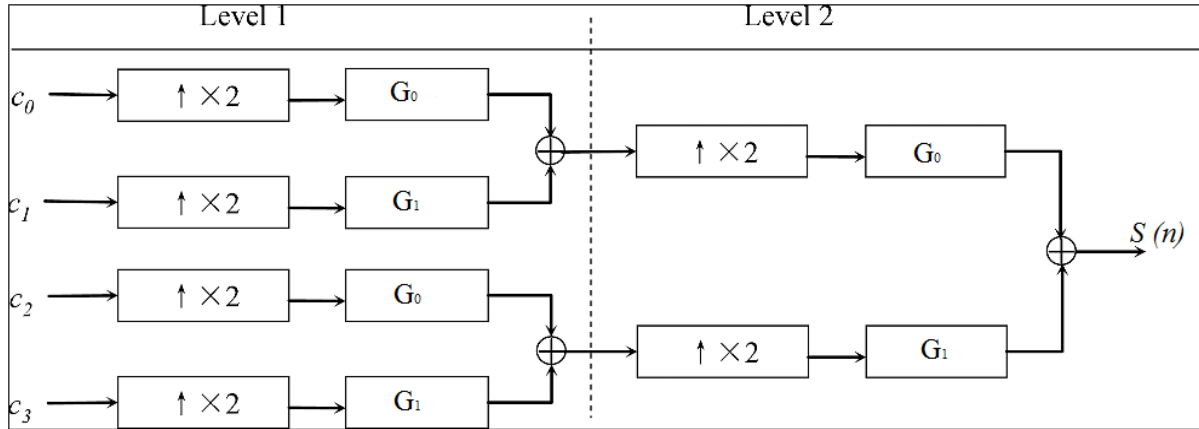
$$f_h(k) = \sum_n s(n)h_0(2k - n) \quad (3.7)$$

$$f_l(k) = \sum_n s(n)h_1(2k - n) \quad (3.8)$$

Where  $f_h(k)$  and  $f_l(k)$  are the subsampled outputs of both high pass and low pass filters. From the Fig 3.5, every decomposition level has a filtering and subsampling blocks in which subsampling is done by a factor of 2. Here each wavelet decomposition level divides the signal into two frequency levels namely, approximation and detail level.

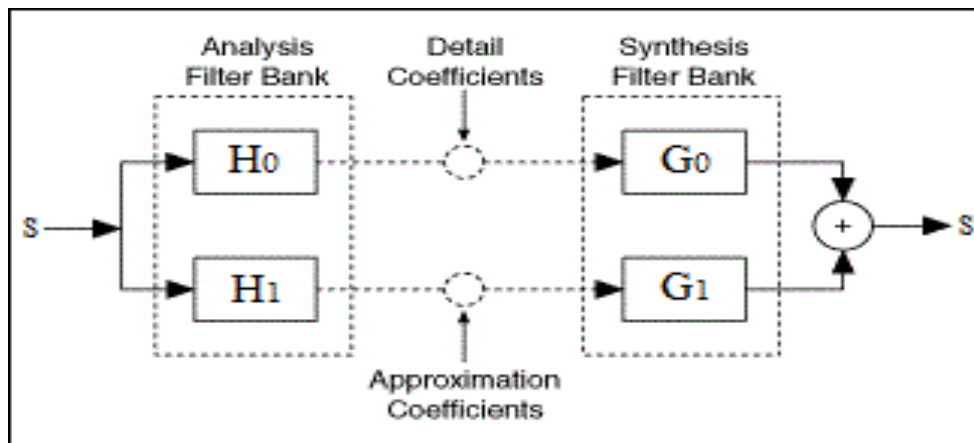
### 3.2.3. Wavelet Synthesis

Synthesis of wavelets is often called as inverse of wavelet decomposition. In many application, reconstruction of the modified wavelets is required for further analysis. Synthesis/reconstruction constitutes of two steps, up sampling and filtering [11]. Fig 3.6 shows a two level wavelet synthesis block:



**Fig 3.6. Implementation of two level wavelet synthesis**

Where  $C_0, C_1, C_2, C_3$  are the approximation and detail coefficients of 2<sup>nd</sup> level wavelet decomposition,  $S(n)$  is the original input signal after reconstruction and  $G_0, G_1$  are the filter banks of high pass and low pass filters. A combination of both decomposition and reconstruction for one level is shown in Fig 3.7:



**Fig 3.7. One level decomposition and synthesis wavelet.**

In order to attain perfect reconstruction, two conditions must be satisfied:

- 1) The reconstructed signal should not be distorted in terms of amplitude.
- 2) The reconstructed signal must cancel out the aliasing effect caused during subsampling process.

### 3.3. Principal component analysis (PCA)

PCA is a method for analysing data sets of high dimension, revealing patterns and highlights the similarities and differences. Although PCA can be used for various types of analysis, here the emphasis will be on data reduction and feature extraction. In data sets with many variable it is obvious that more than one variable is measuring the same driving force. PCA generates a new set of variables called principal components(PC). Each PC is a linear combination of the original variables. The purpose of using this is to remove redundancy of information and replace a group of variables which measures the same information with a single new variable called principal component (PC). The calculation of the principle component is essentially equivalent to performing the singular value decomposition (SVD) on a data set, X which is described in [13,14]. The process is outlined below as:

- 1) Calculate the covariance matrix for the data set X. The matrix is of size  $m \times n$  where rows denote the variable and columns denotes the observation for each variable.
- 2) Calculate the eigenvalues,  $\lambda_i$  ( $i=1,2,\dots,m$ ) of the covariance matrix.
- 3) Now calculate the eigenvectors of the corresponding eigenvalues,  $U_i$  ( $i=1,2,\dots,m$ ).
- 4) Order the eigenvalues in descending order and align the corresponding eigenvectors based on the eigenvalues. These forms principal components and principle eigenvalues.

$$A = \text{diag}(\sigma_1, \sigma_2, \sigma_3, \dots, \sigma_m) \quad \text{where } \sigma_1 > \sigma_2 > \sigma_3 > \dots > \sigma_m$$

$$PC = [PC1 \ PC2 \ \dots \ PCm]. \quad (3.9)$$

Where  $PC_i$  is the Eigen vector that corresponds to Eigen value  $\sigma_i$ .

#### Properties of PCA

There are infinite number of ways to determine an orthogonal basis for a particular set of data. Based on its properties PCA provides great benefits in feature extraction problems.

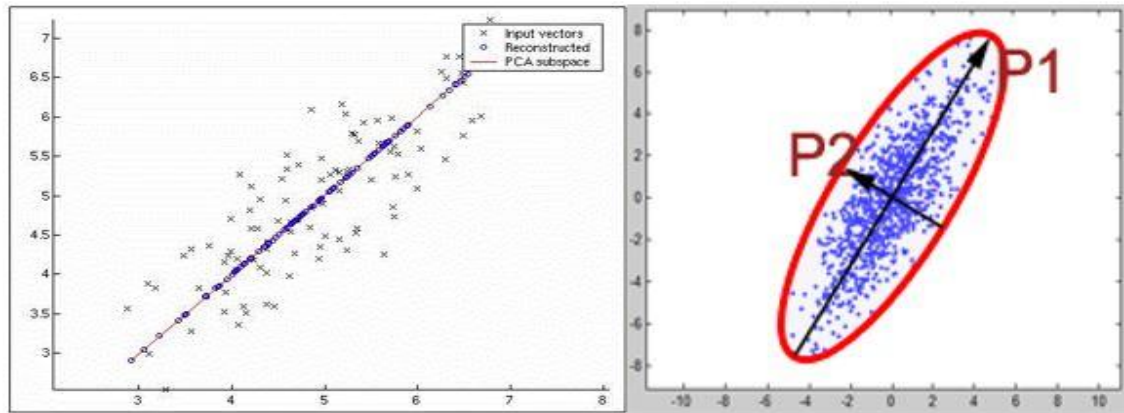


Fig 3.8. Principal component analysis subspace.

The properties of PCA are:

- 1) Each principal component is a linear combination of the original variables.
- 2) All the principal components are orthogonal to each other so there is no redundant information.
- 3) The PC's as a whole form an orthogonal basis for the space of the data.

Each principal eigen value measures the amount of information captured in the direction of a corresponding eigen vector. The 1<sup>st</sup> principle component is a single axis variable and when the data is projected onto the axis, the variance is maximal among all possible choices. The 2<sup>nd</sup> principal component is another variable whos axis is perpendicular to the 1<sup>st</sup> principle component with variance more than the succeeding principal components. Subsequent principle components are determined in the same manner. In this sense, the original data set is transformed so that it is expressed in terms of the patterns between the variables. The transformation/projection can be expressed mathematically using following equation:

$$Y=PC^T \cdot X \quad (3.10)$$

Where,  $PC=[PC1 \ PC2 \ \text{-----} \ PCm]$

$X$  is original data set

$Y$  is transformed data set.



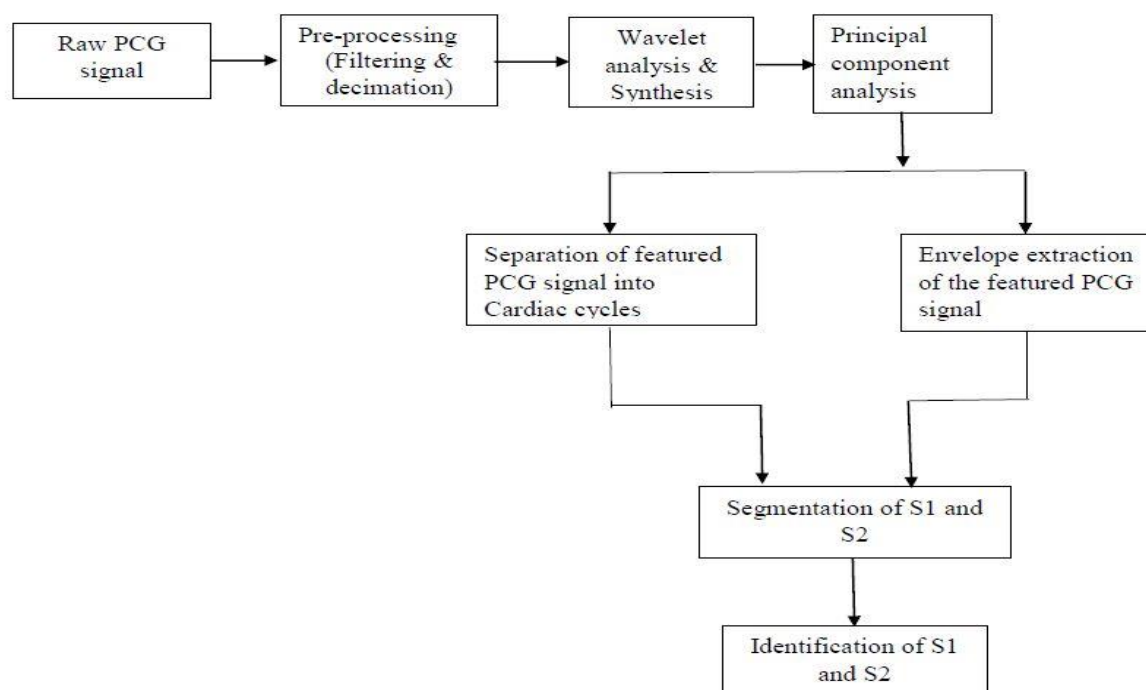
# CHAPTER 4

# SEGMENTATION

# ALGORITHM

## 4. Segmentation of S1 and S2 Sounds

Auscultation of heart sounds (HSs) is the fundamental tool performed by the primary health care Centre's in screening patients for pathology. Simple thresholding algorithms and algorithms based on time-frequency analysis may not work correctly in cases of non-stationary behavior. HS signals have a typical behavior that they are highly non-stationary and exhibit sudden frequency changes and transients. Moreover, the frequency content of the murmurs which have same frequency as primary components (S1 & S2), shows a great impact during segmentation. These constraints provides greater scope to concentrate much in this research field. The novel algorithm developed is to counteract these drawbacks. The technique uses statistical parameters of the HSs and important signal processing elements such as filtering, wavelet analysis (WA) and principal component analysis (PCA).



**Fig 4. Block diagram for segmenting and identifying principal components.**

This chapter explains the segmentation algorithm based on statistical analysis and its implementation.

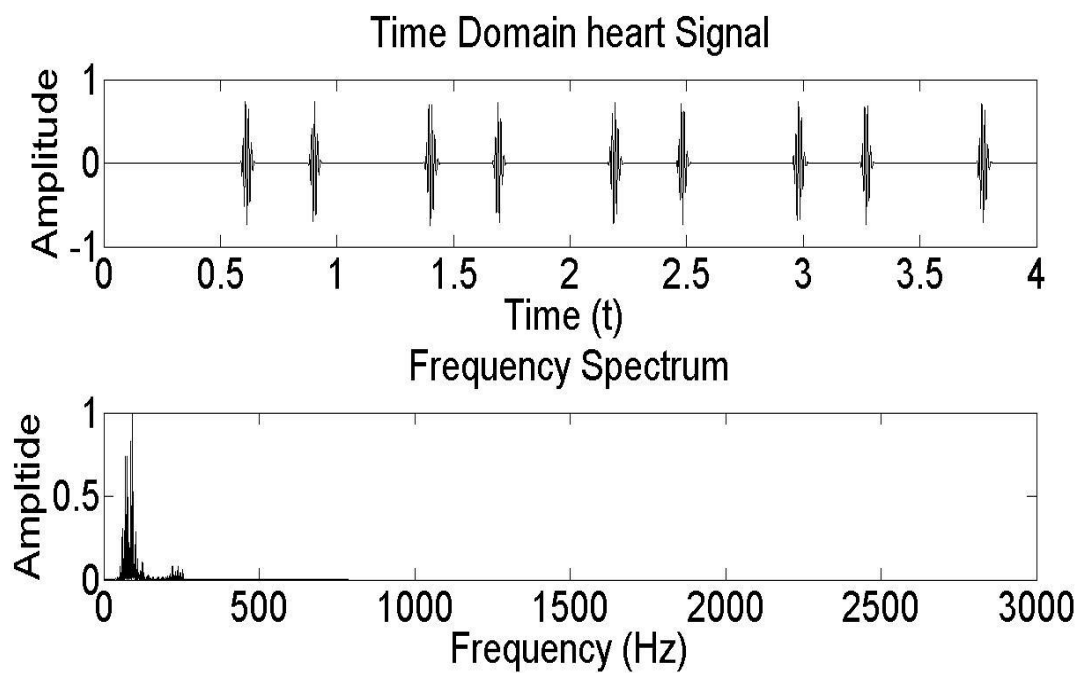
## 4.1. Pre-processing

### Filtering

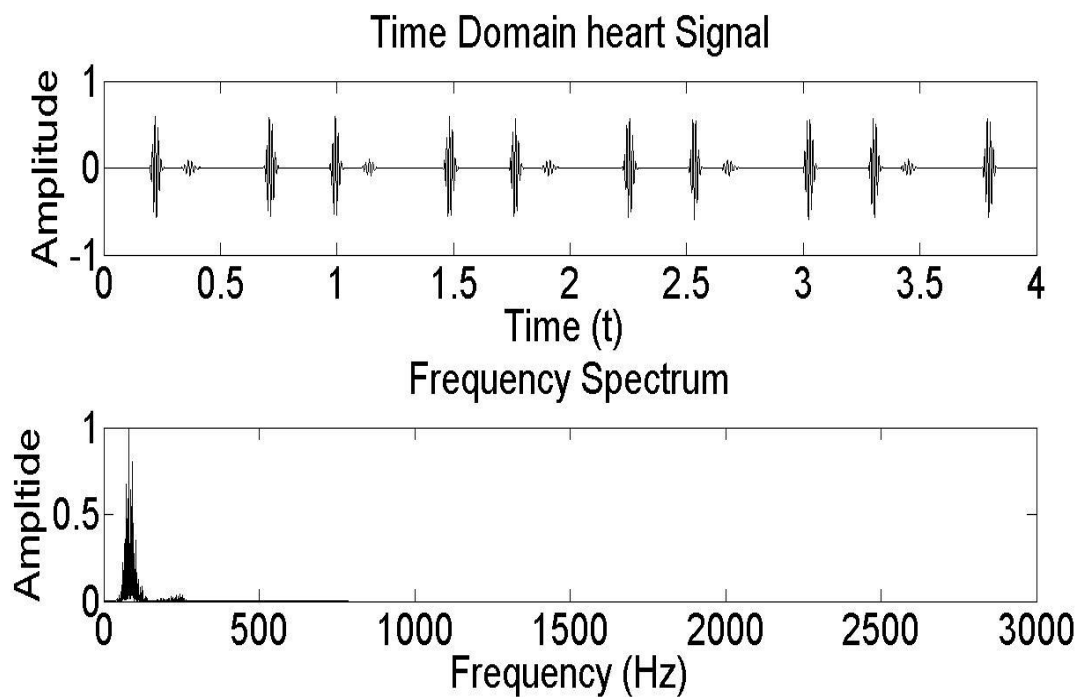
During acquisition process there is a possibility of noise interference. The noises may be due to respiratory tracts in the human being, environmental disturbances or even the measuring equipment itself. The frequency content of these noises would be less than 40Hz. It is necessary to remove these noises at initial state for better boundary detection of S1 and S2. So a filtering technique is performed to remove those low frequency noises using high pass filter (HPF) with a cut-off frequency of 40Hz.

### Decimation

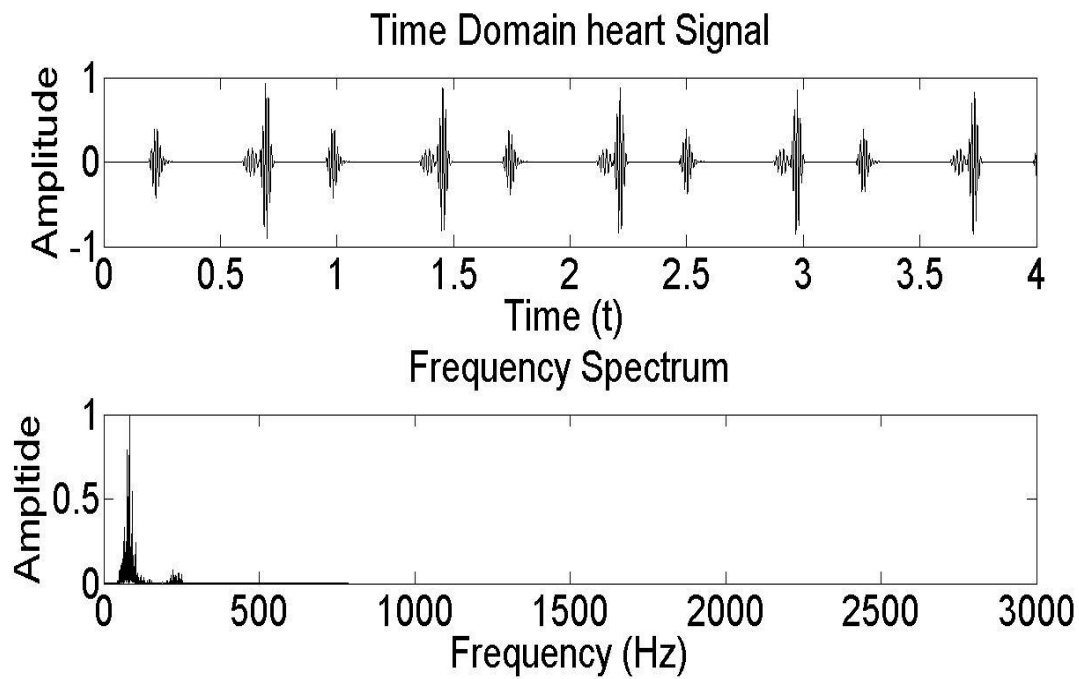
The phonocardiographic signal records used in this study are sampled at a sampling frequency of 22050Hz. Researchers have demonstrated that most of the primary components have a frequency ranges from 40 to 200Hz which are due to the turbulence of blood flow in the heart valves and the murmurs due to valvular dysfunctions have a frequency range up to 600Hz. This shows that it is unnecessary to consider the frequencies which are not of clinical significance for analysis and diagnosis purposes. The justification of the studies are shown in below figures (4.1 – 4.9). In each figure the PCG signal is shown on the top followed by its frequency spectrum. So further processing is required for the HS signal so that the frequencies of interest are only present for further processing. This is done by decimation. Decimation employs an eighth-order low pass Chebyshev type I filter with cut-off frequency of  $0.8 \cdot (F_s/2)/r$ , where  $F_s$  is the sampling frequency and  $r$  is the decimation factor. Here 'r' is chosen to obtain sample rate of 700Hz. It filters the HS in both forward and reverse directions to remove all phase distortions.



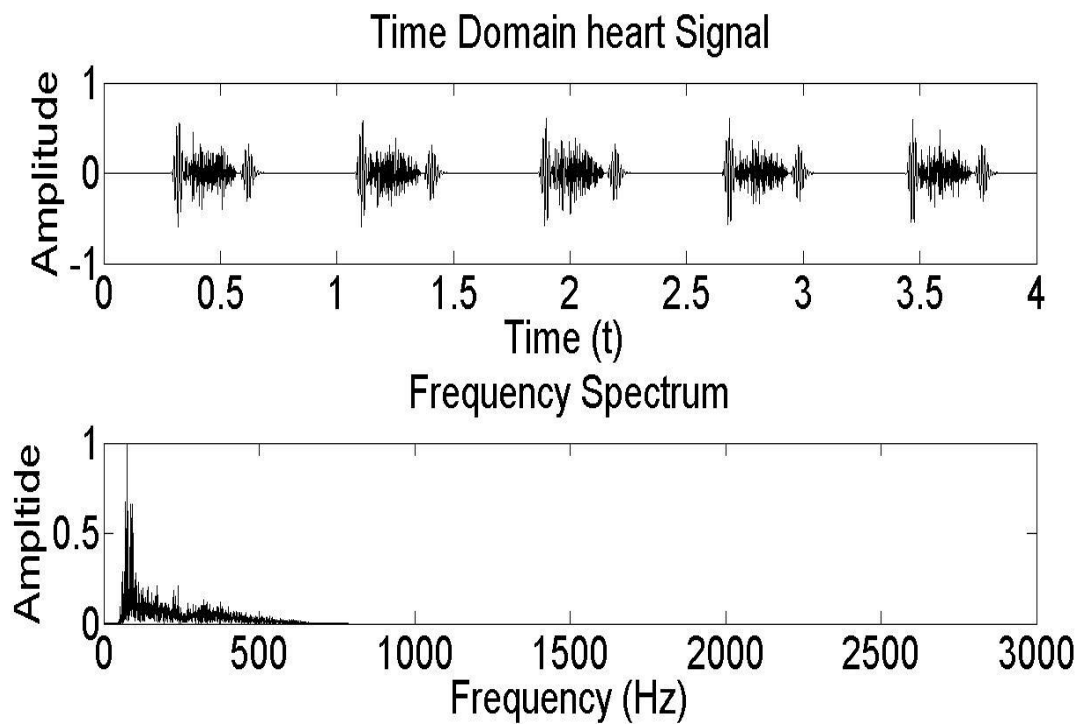
**Fig 4.1.** HS signal and its frequency spectrum for healthy heart.



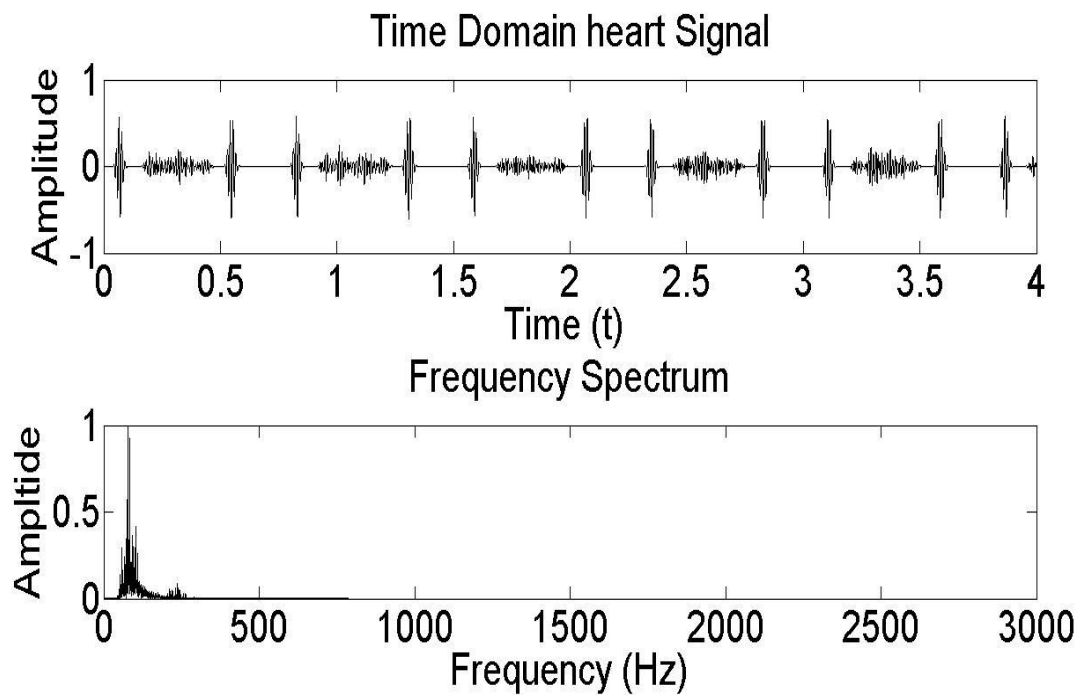
**Fig 4.2.** HS signal and its frequency spectrum for third HS.



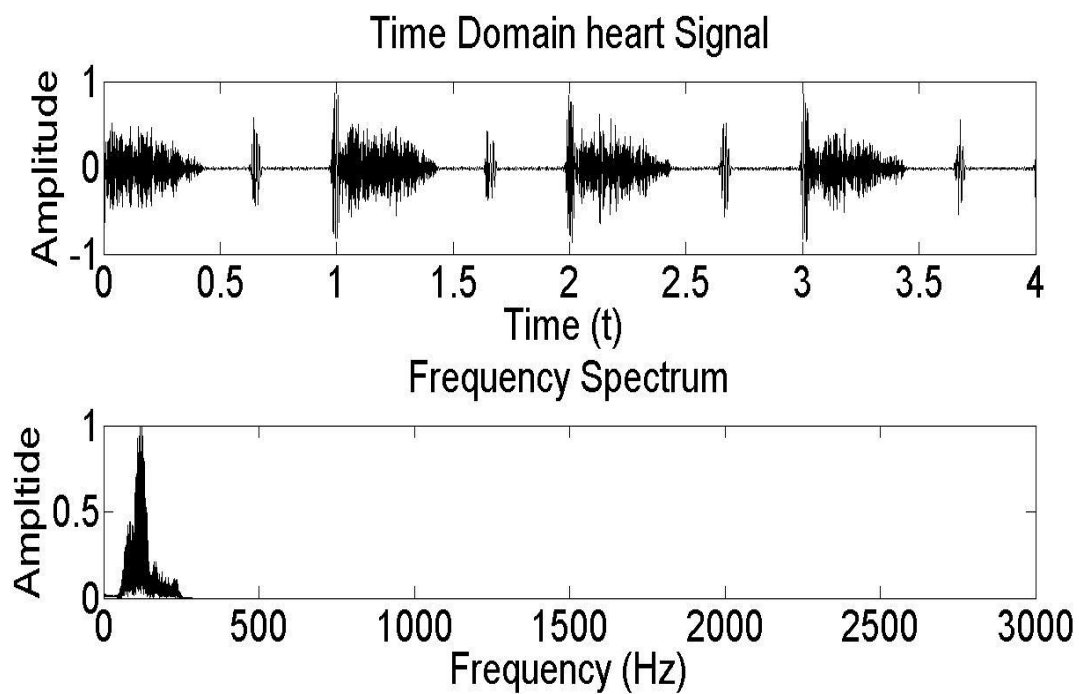
**Fig 4.3. HS signal and its frequency spectrum for fourth HS.**



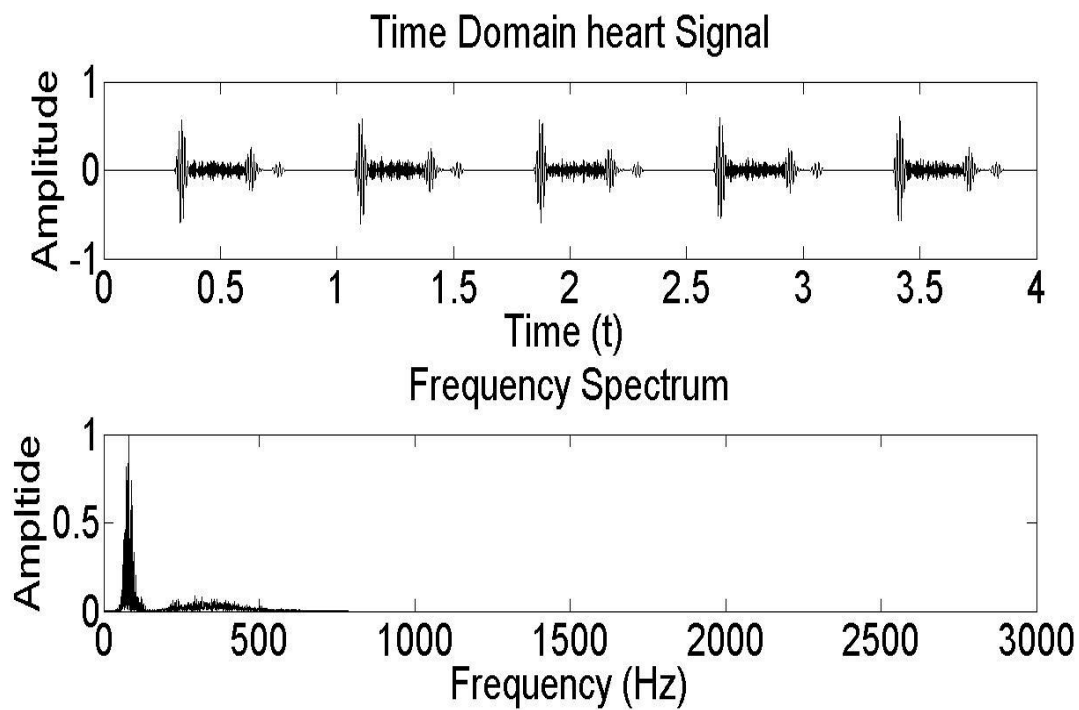
**Fig 4.4. HS signal and its frequency spectrum for Aortic stenosis.**



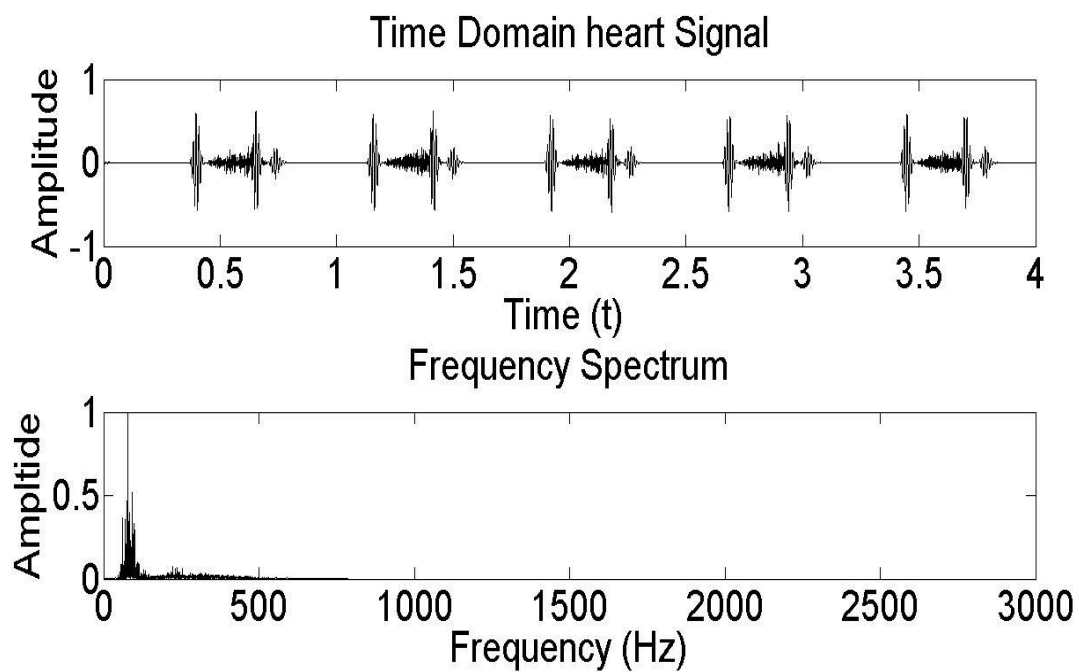
**Fig 4.5. HS signal and its frequency spectrum for mitral stenosis.**



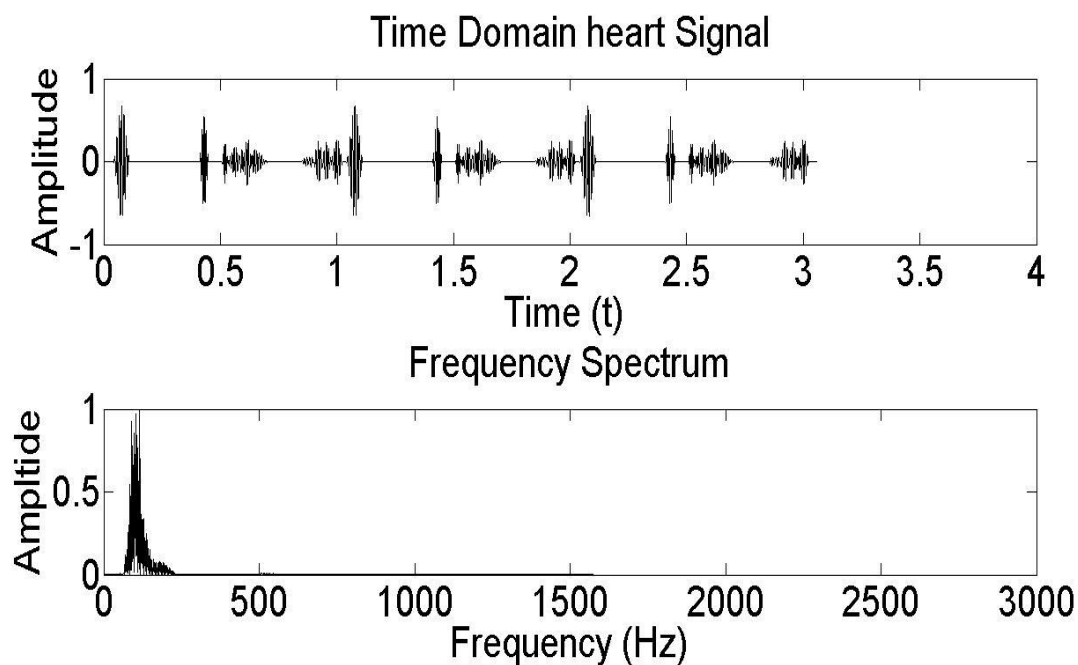
**Fig 4.6. HS signal and its frequency spectrum for Aortic regurgitation.**



**Fig 4.7. HS signal and its frequency spectrum for mitral regurgitation.**



**Fig 4.8. HS signal and its frequency spectrum for pulmonic stenosis.**



**Fig 4.9. HS signal and its frequency spectrum for tricuspid stenosis.**

From the above figures, it is evident that all the important events of the PCG signal lie below 700 Hz frequencies and also it is observed that no data is available at very low frequency area which depicts no important information is present in that frequency range. So it is inevitable to filter and decimate the PCG signal before processing.

## 4.2 Wavelets

Wavelets are capable of handling rapidly changing transient signals because of their scaling and translation property. Due to non-stationary behavior of the HSs, it is unlikely that a single decomposition level serve the purpose of capturing the energy of the primary components for different pathologies.



### 4.2.1 Mother wavelet

Though wavelet plays an important role in analyzing the structure of the coefficients, it is necessary to choose best wavelet, which we call as ‘mother’ wavelet. The wavelet basis is selected from the previous studies done by the scholars M.A.R Santos and M. Souza [10] and Tang Chu Lin [14]. Both of them showed that Daubechies and Meyer wavelets are good candidates for HS signal analysis.

From the results of Tang Chu Lin, Daubechies-15 (db) is chosen as the mother wavelet for decomposing the HS signals. Daubechies wavelet has a property of orthogonality which is used to remove the redundant information and also it has strong resemblance of the primary components of HS signal.

### 4.2.2 Wavelet Decomposition

HS signal is decomposed using 5<sup>th</sup> level wavelet decomposition which breaks the signal into 5 levels. The breakdown of the signal into levels is possible due to the scale factor  $S_0$ , which can be shown through following equation.

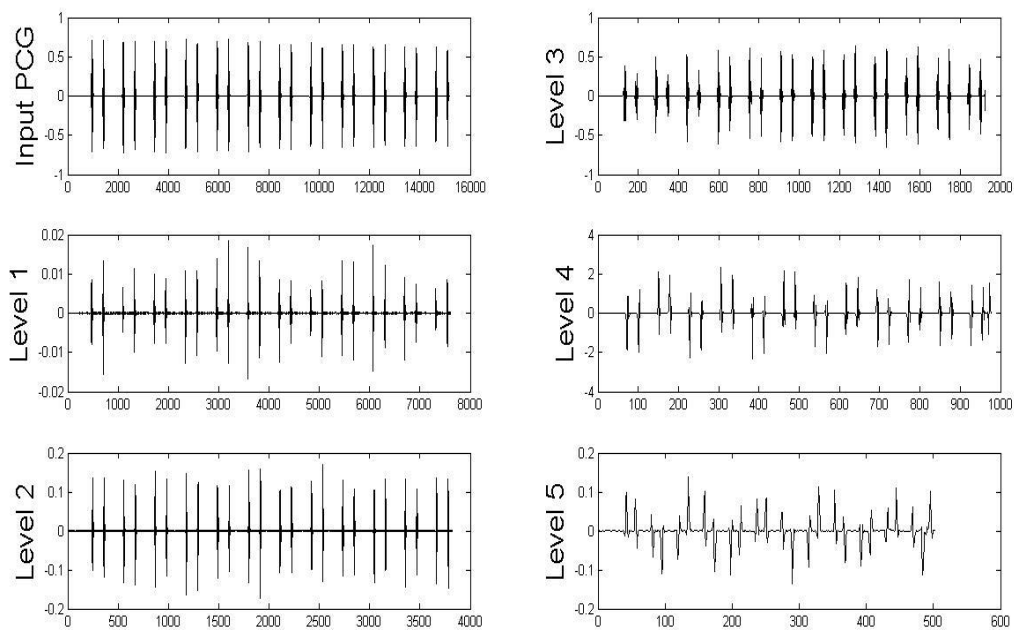
$$S_0 = 2^m \quad (4.1)$$

Where, m is the level parameter. (Here m=5)

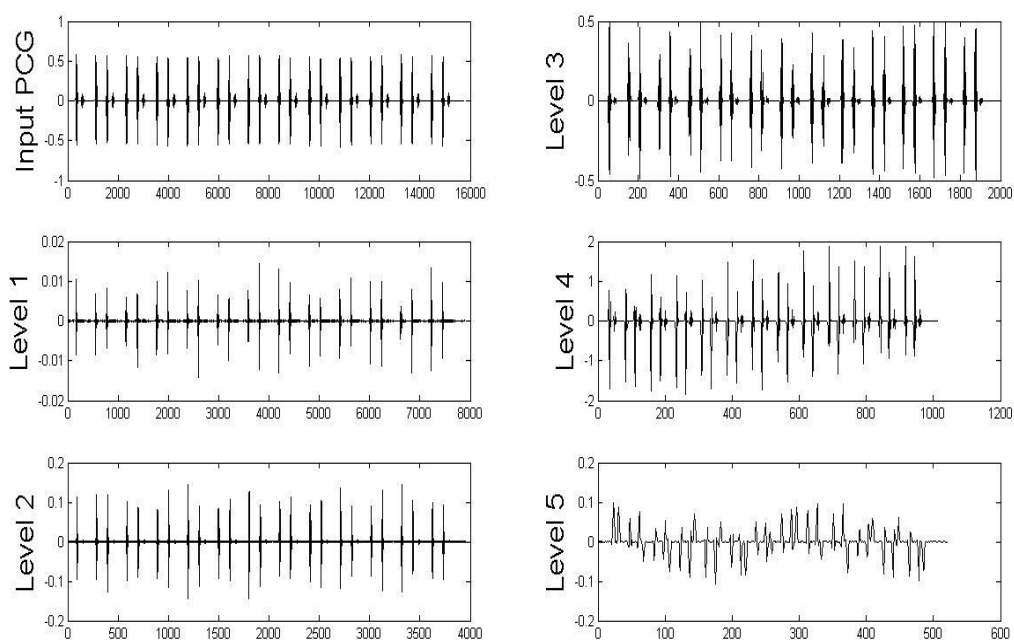
The frequency resolution is defined as

$$\frac{1}{R} = \frac{1}{i} = 2^{-m} \quad (4.2)$$

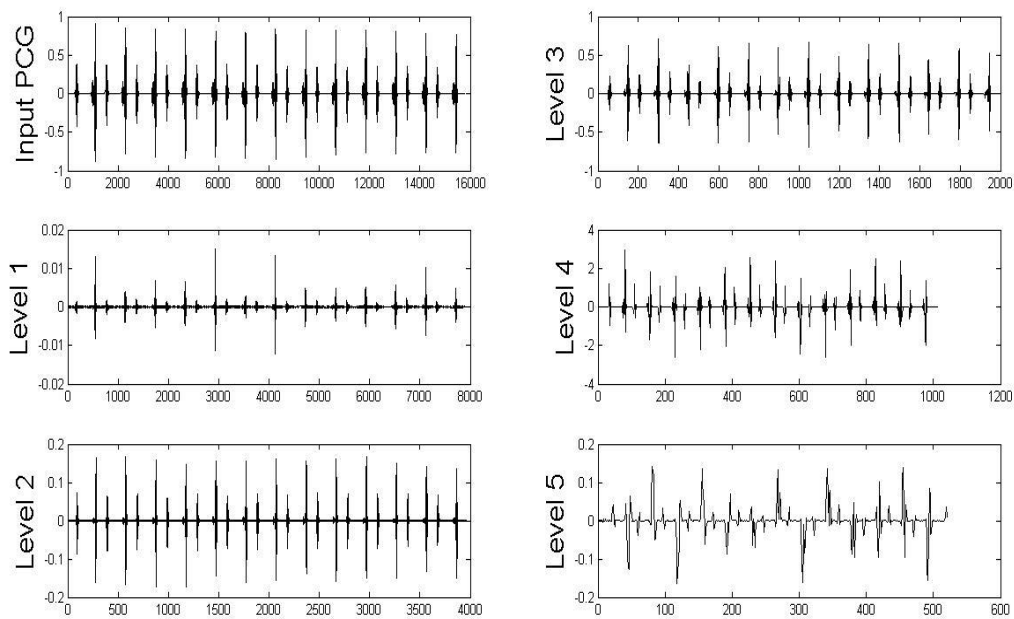
The above equations show that the frequency resolution increases as the scale increases and as the resolution increases the details become finer that are accessible. Here each detail level carries a particular range of frequencies with a different time and frequency resolution. The breaking of HS signal into levels also helps in figuring out the frequencies of key cardiac events. The below figures (4.10 to 4.18), shows wavelet decomposition for each level. From the figures it can be observed that as levels increases their corresponding frequency ranges decreases.



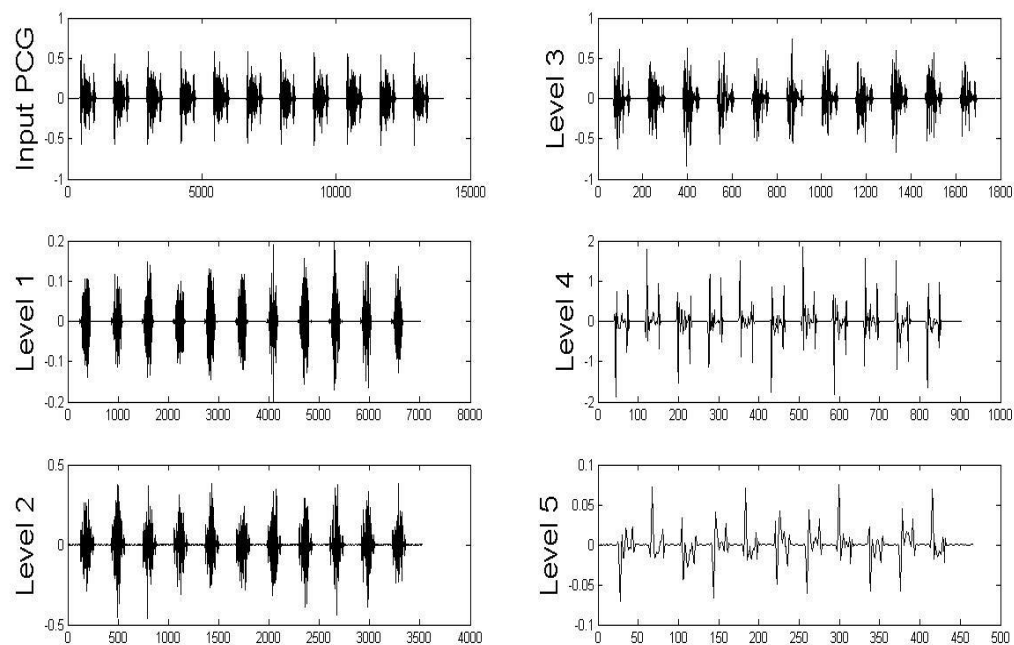
**Fig 4.10. Wavelet decomposition for healthy HS signal.**



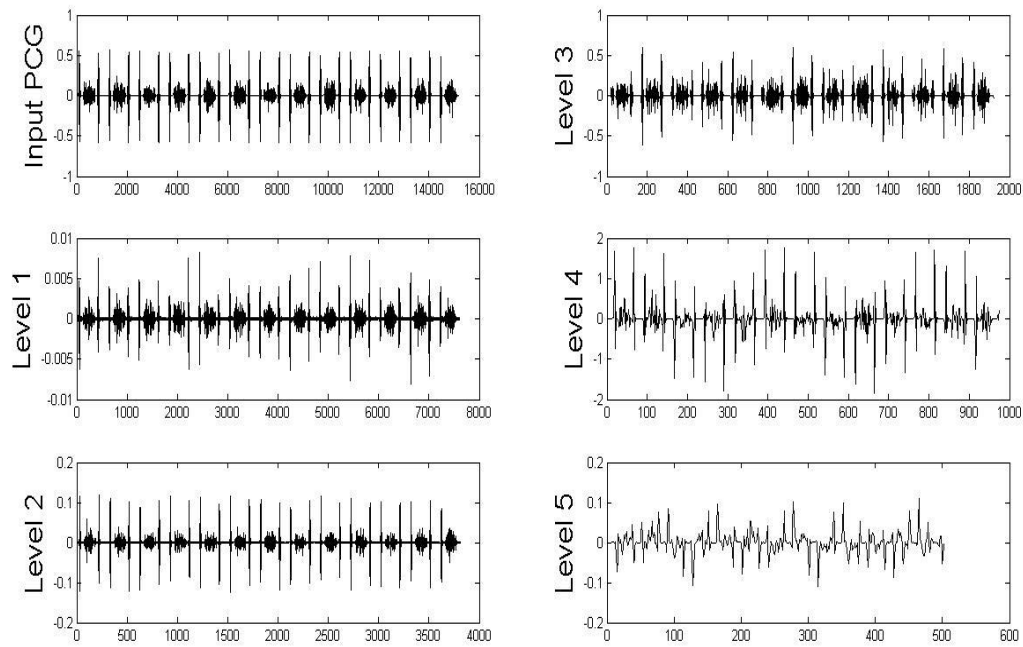
**Fig 4.11. Wavelet decomposition for a patient with third HS signal.**



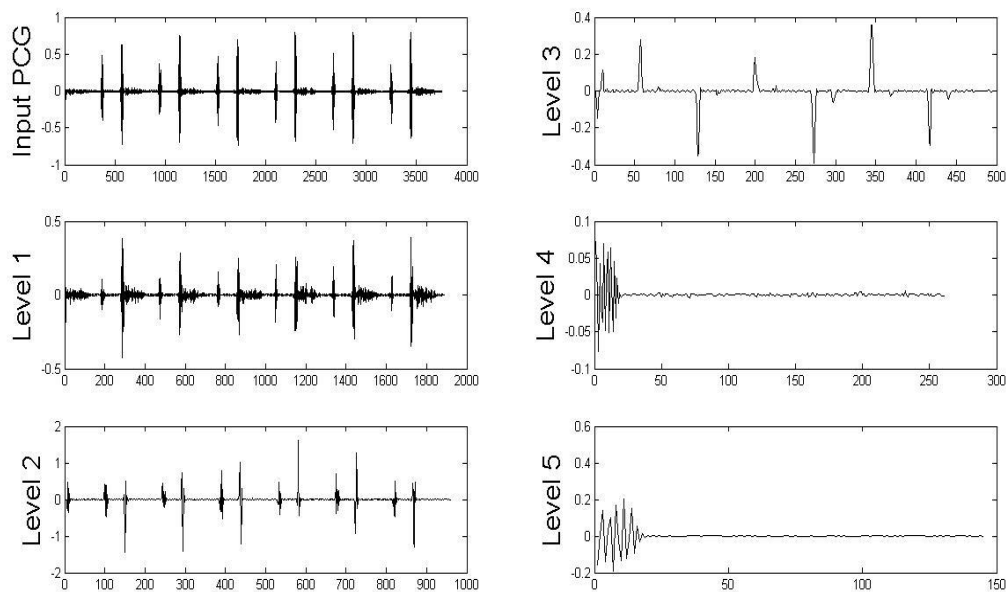
**Fig 4.12. Wavelet decomposition for a patient with fourth HS signal.**



**Fig 4.13. Wavelet decomposition for a patient with aortic stenosis.**

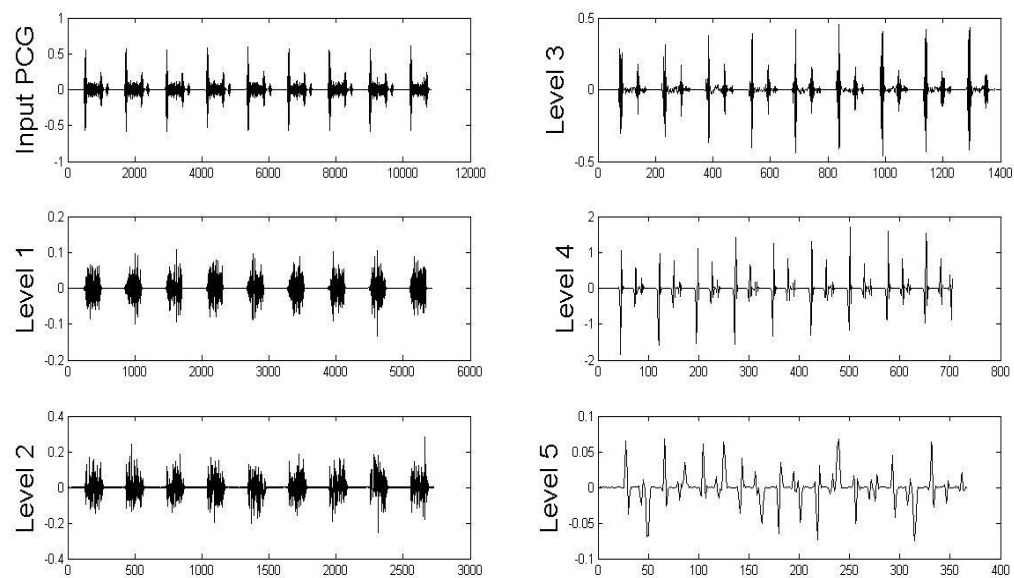


**Fig 4.14. Wavelet decomposition for a patient with mitral stenosis.**

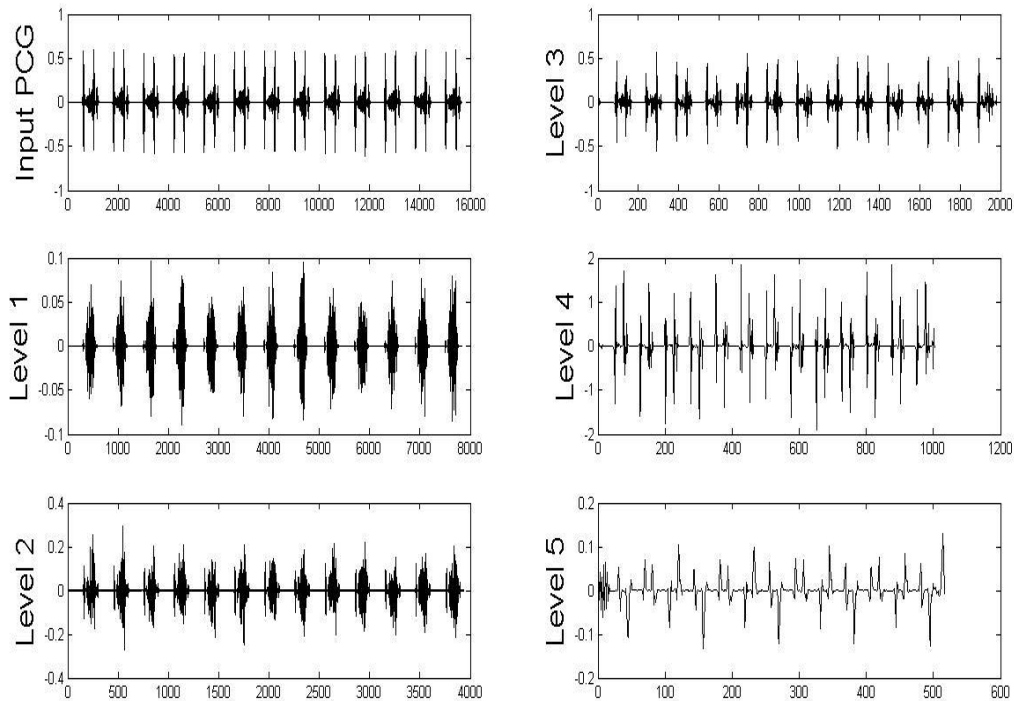


**Fig 4.15. Wavelet decomposition for a patient with aortic regurgitation.**

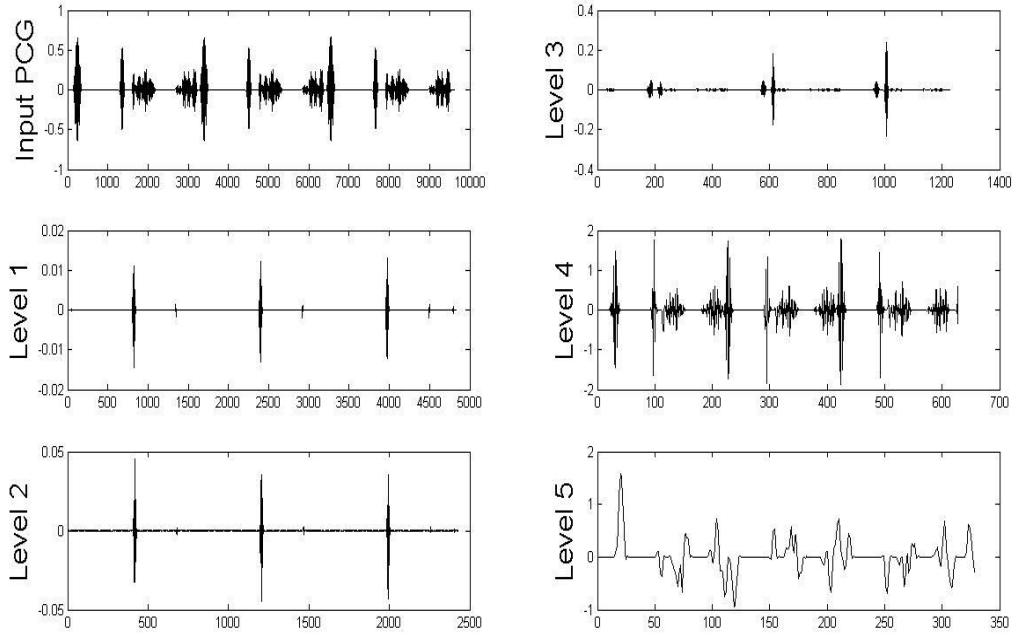
# STATISTICAL SIGNAL PROCESSING APPROACH TO SEGMENT PRIMARY COMPONENTS FROM PATHOLOGICAL PHONOCARDIOGRAM (PCG)



**Fig 4.16. Wavelet decomposition for a patient with mitral regurgitation.**



**Fig 4.17. Wavelet decomposition for a patient with pulmonic stenosis.**

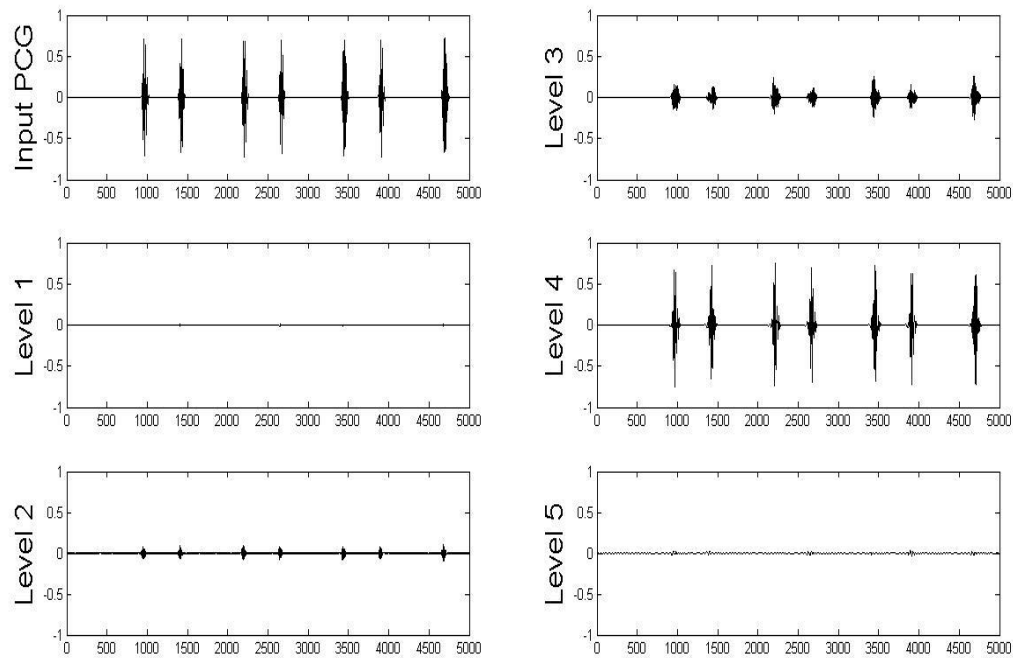


**Fig 4.18. Wavelet decomposition for a patient with tricuspid stenosis.**

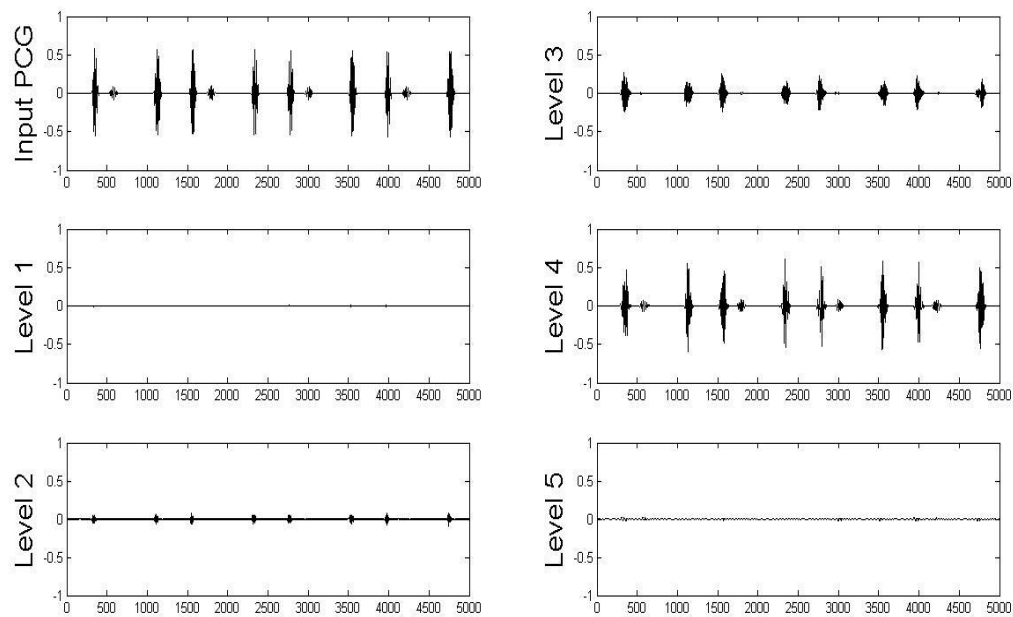
### 4.2.3 Wavelet Synthesis

The wavelet decomposition analysis of HS signals illustrate the information captured in each detail level. In order to obtain best temporal resolution, it is necessary that each of the coefficient vector should be used to synthesize the original HS signal. The representation of the signal components determines the accuracy in segmenting the events. Furthermore the accuracy levels of the segmented components gets diminished due to presence of unwanted elements (either noise or/and murmur) in a signal. The purpose of wavelet synthesis is to obtain a set of featured signals at the highest temporal resolution. From the feature set, each point in the pre-processed HS signal can be viewed as a point in a 5-dimensional space where each dimension corresponds to a detail level. If we consider each sample point as a random variable then there would be five observations per variable. The five synthesized signals generate a feature set for the original HS signal. These features cannot be used as the final set of features for segmentation because obtaining the best feature for each sample point from five obtained observations is not possible using

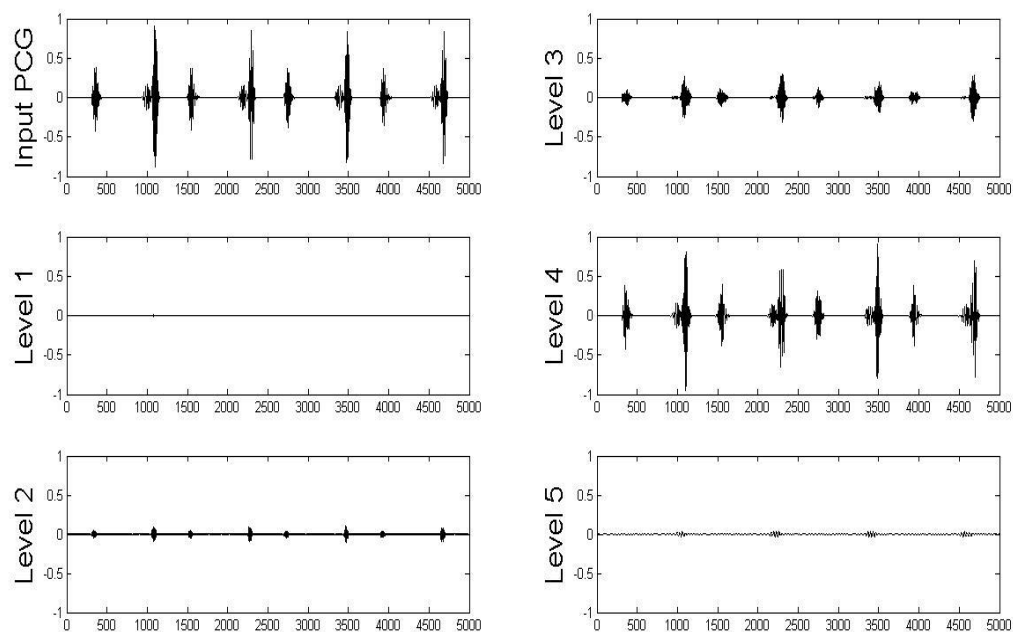
wavelets. So further processing is required which is done by principal component analysis. The figures shown below (4.19 – 4.27) provides a clear idea of how the signal is separated into levels.



**Fig 4.19. Reconstructed HS signal for healthy patient.**

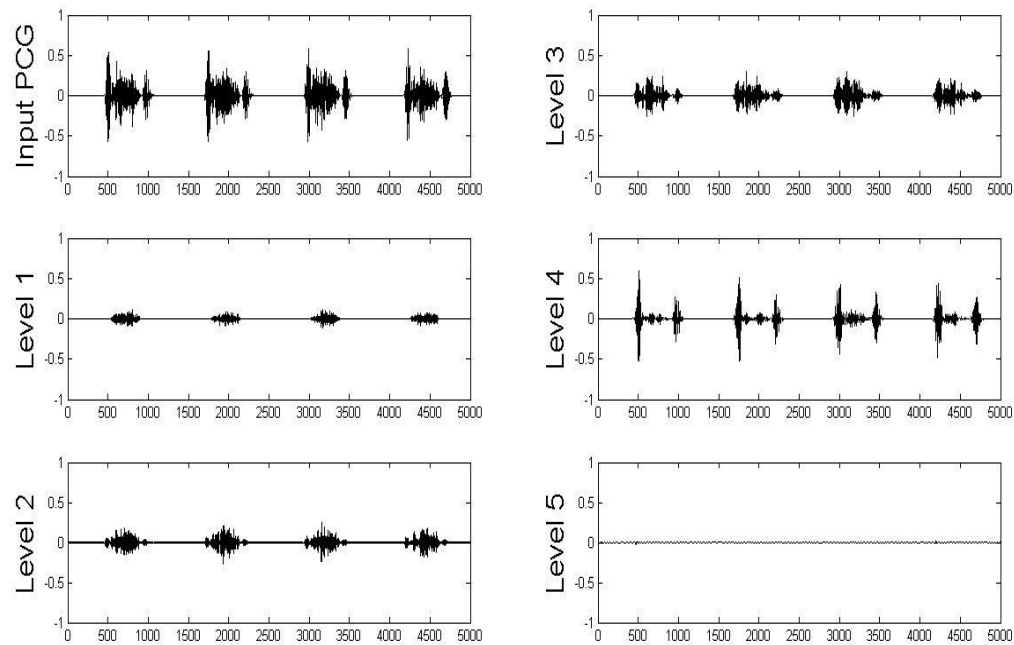


**Fig 4.20. Reconstructed HS signal for third HS patient.**

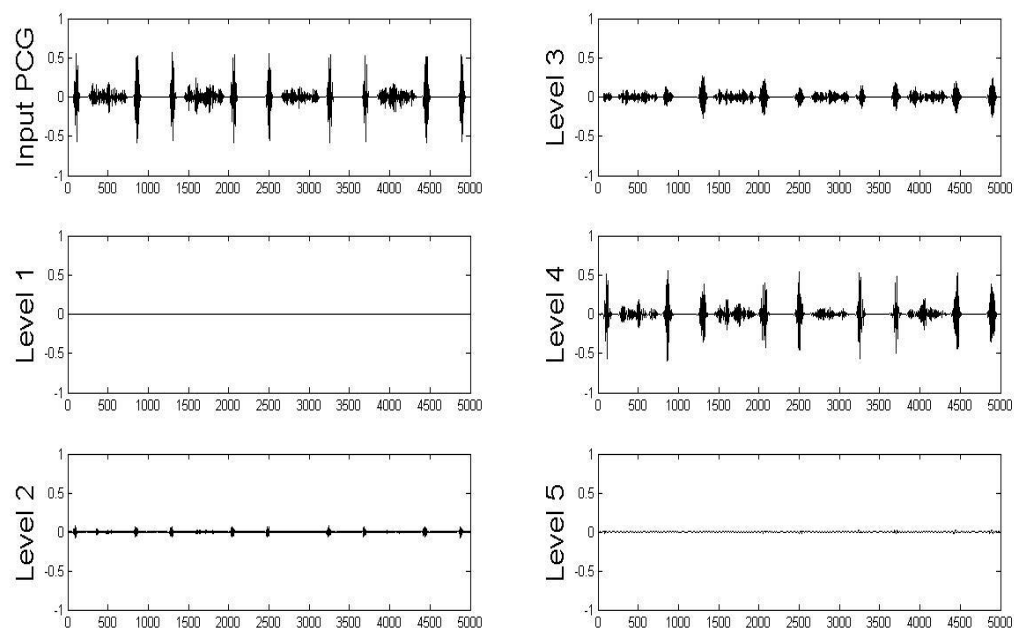


**Fig 4.21. Reconstructed HS signal for fourth HS patient.**

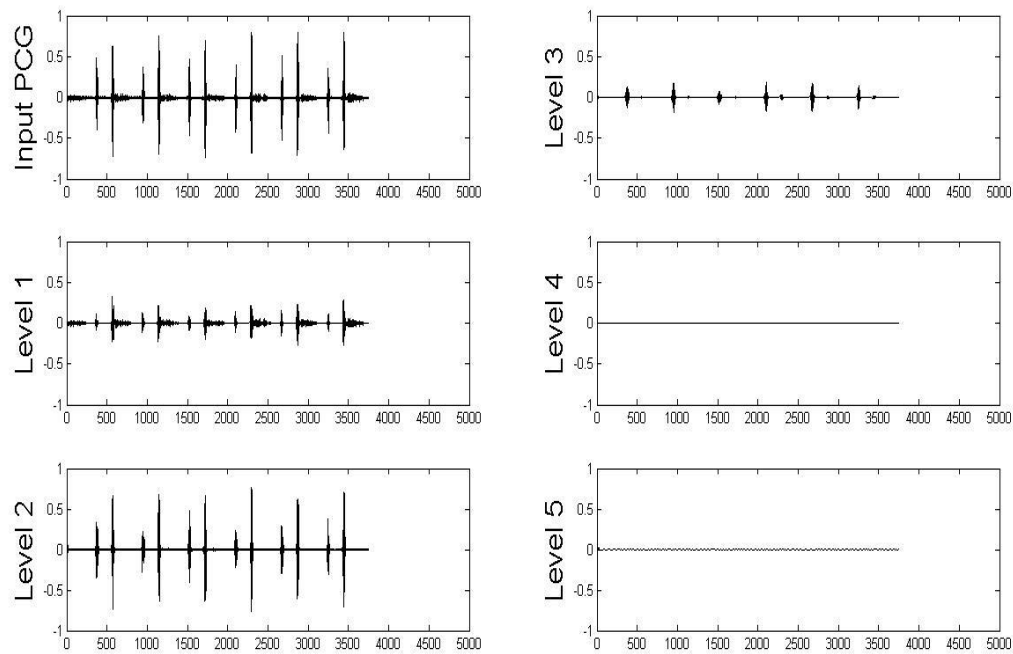




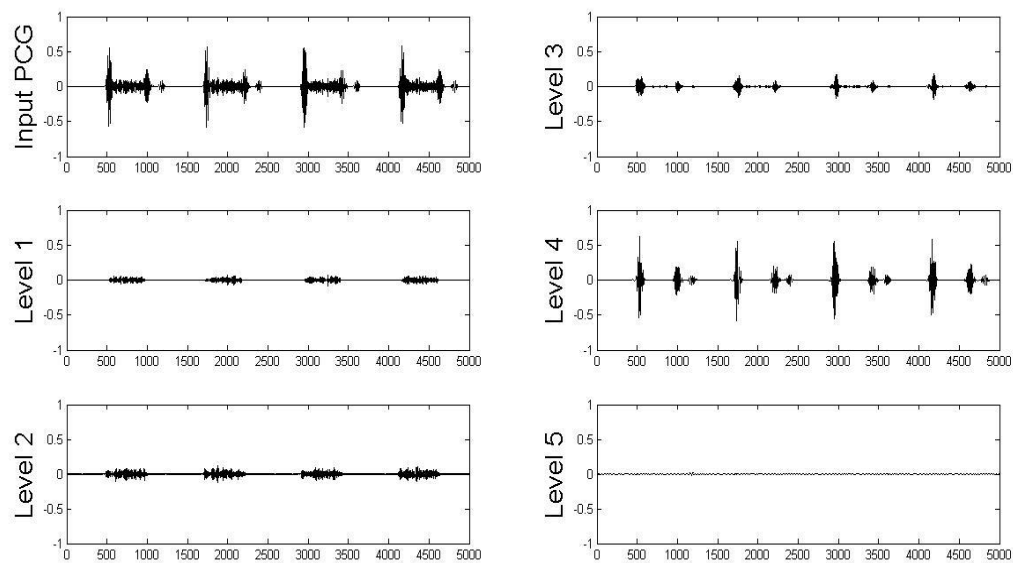
**Fig 4.22. Reconstructed HS signal for patient with aortic stenosis.**



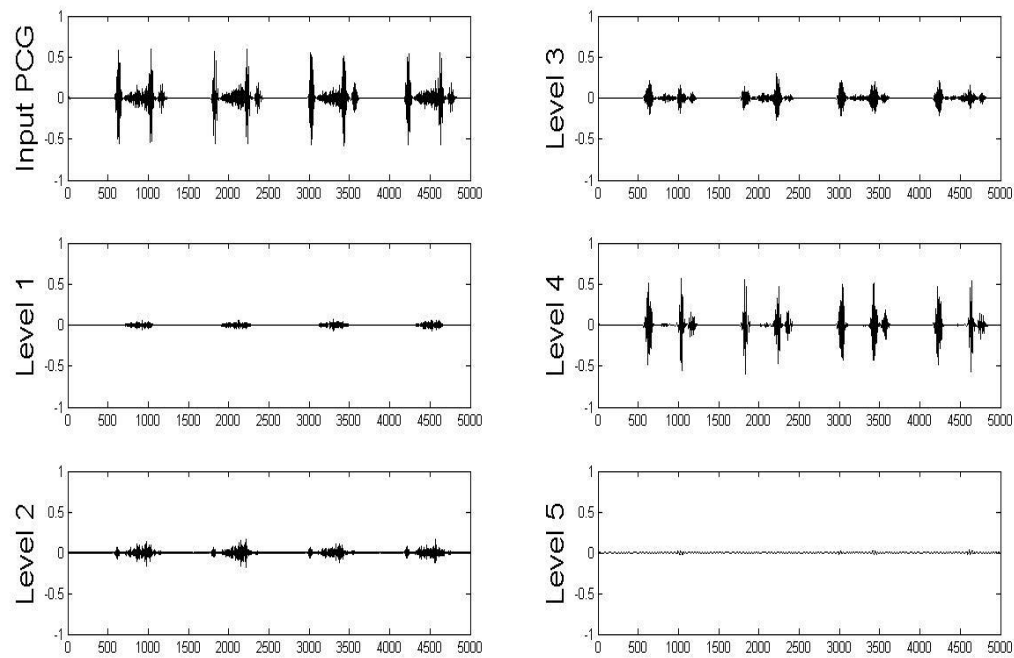
**Fig 4.23. Reconstructed HS signal for patient with mitral stenosis.**



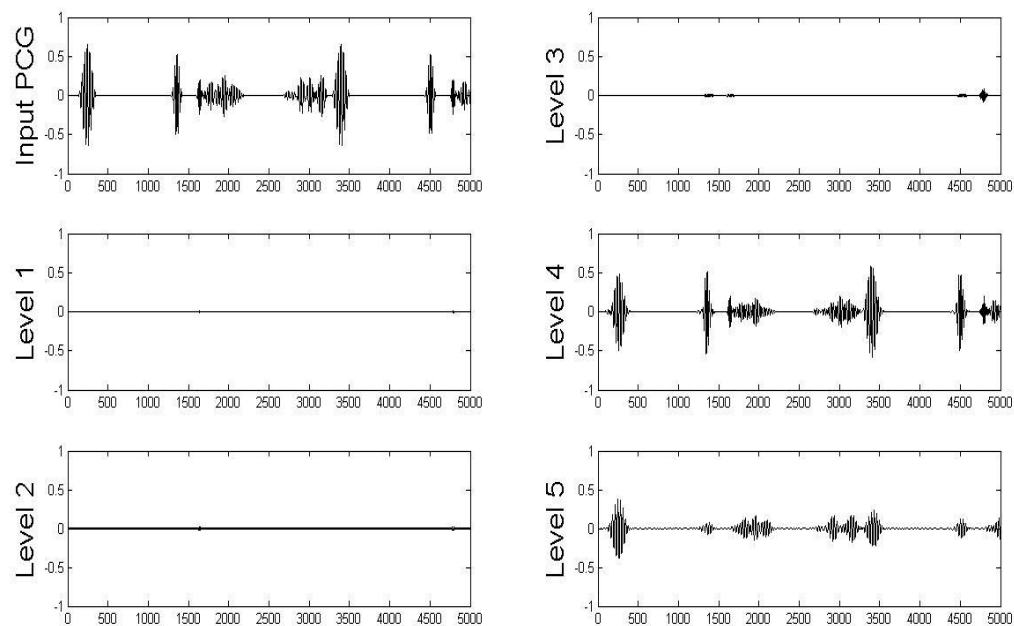
**Fig 4.24. Reconstructed HS signal for patient with aortic regurgitation.**



**Fig 4.25. Reconstructed HS signal for patient with mitral regurgitation.**



**Fig 4.26. Reconstructed HS signal for patient with pulmonic stenosis.**



**Fig 4.27. Reconstructed HS signal for patient with tricuspid stenosis.**

From the figures, we can conclude that level 1 doesn't carry any information about HS which can be neglected. Level 2, 3, 4 & 5 carries the information of the HSs and in that level 3 and level 4 contains maximum information content of the HS components than the other two.

### 4.3 Principal Component Analysis (PCA)

Through wavelet analysis and synthesis a featured set is generated for the HS signal. The main aim of PCA is to acquire a best featured signal such that the HS signal is well represented with the desired components while minimizing the interfering components. The property of orthogonality makes PCA a desirable method for evolving these featured signals.

#### Finding featured signal

It is necessary to find out a feature set which could be capable of segmenting primary components from the original PCG signal. The feature set,  $P$ , is formed such that each row corresponds to a reconstructed signal. The signal can be represented as a linear combination of the five synthesized signals at  $t=t_0$  which is computed using equation:

$$S(t_0) = \sum_{i=1}^5 K_i X_i(t_0) \quad (4.3)$$

Where  $S$  is the original HS signal.

$X_i$  is the  $i^{\text{th}}$  synthesized signal at level  $i$ .

$K_i$  is a scaling constant.

For perfect reconstruction the scaling constant should be  $K_i = 1 \dots 5$ . The new variables obtained are the linear combination of the original variables which are orthogonal to each other and captures as much of the original variance in the data as possible. These new variables set are called principal components (PCs). The PCs are calculated using the following equations:

$$X = P \cdot P^T \quad (4.4)$$

$$PC_i = \sigma_{(i)} \quad (4.5)$$

Where

$P$  is the original feature set

$X$  is the correlation matrix of  $P$

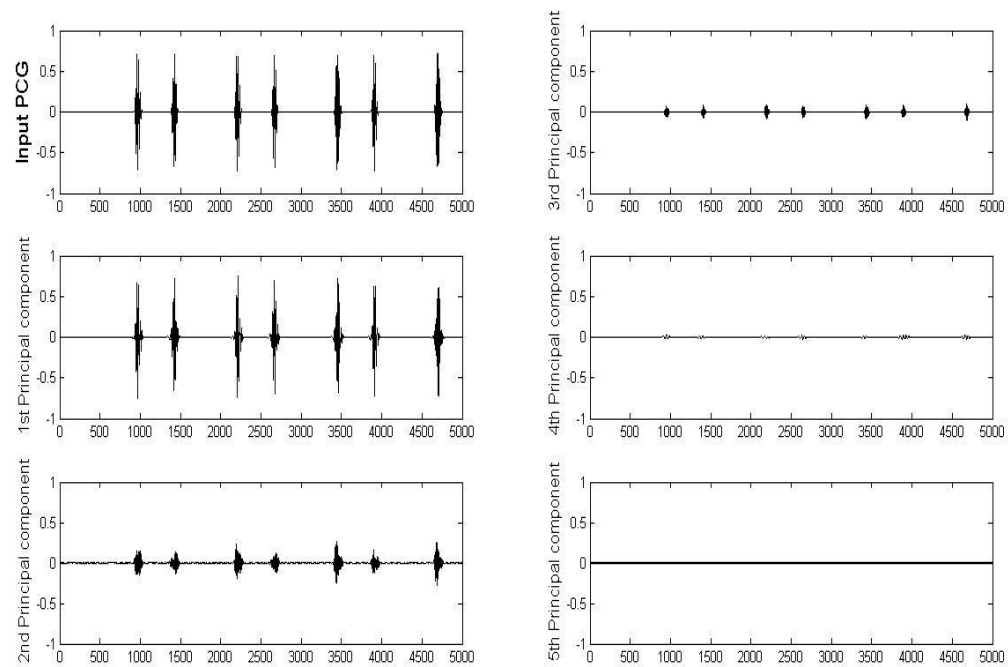
$\sigma_{(i)}$  is the eigenvector that correspond to the  $i^{\text{th}}$  largest eigenvalue i.e.  $\sigma_1 > \sigma_2 > \sigma_3 > \dots > \sigma_i$ .

Each principal eigen value measures the amount of information captured in the direction of a corresponding eigen vector. The 1<sup>st</sup> principal component is a single axis variable and when the data is projected onto the axis, the variance is maximal among all possible choices. The 2<sup>nd</sup> principal component is another variable whos axis is perpendicular to the 1<sup>st</sup> principal component with variance less than that. Subsequent principle components are determined in the same manner. In this sense, the original data set is transformed so that it is expressed in terms of the patterns between the variables. The transformation/projection can be expressed mathematically using following equation:

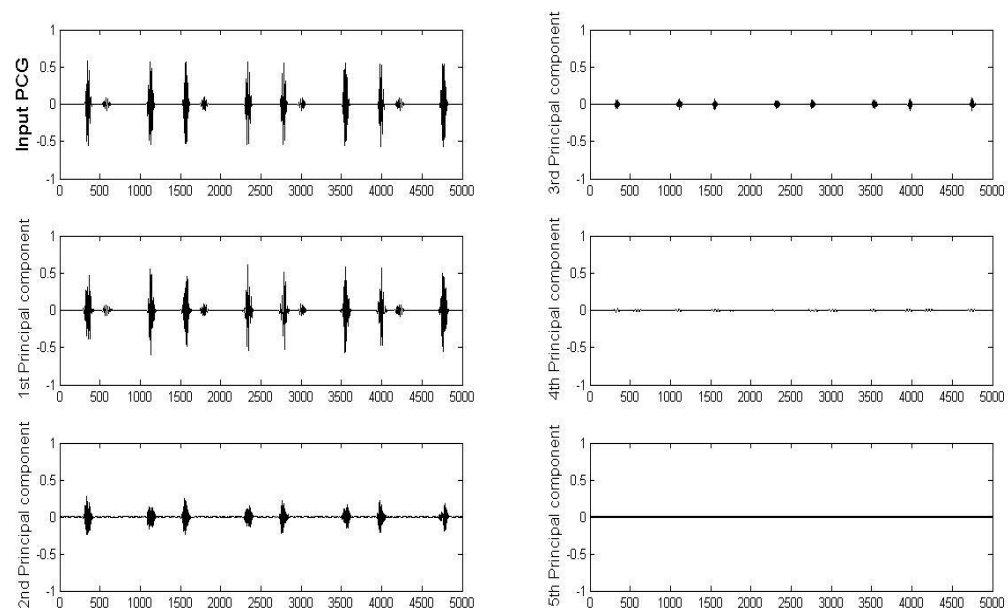
$$Z = PC^T \cdot X^T \quad (4.6)$$

Where  $PC$  is a matrix containing the ordered eigenvectors and  $Z$  is a matrix where each row corresponds to the projection of original data set onto the corresponding principal component.

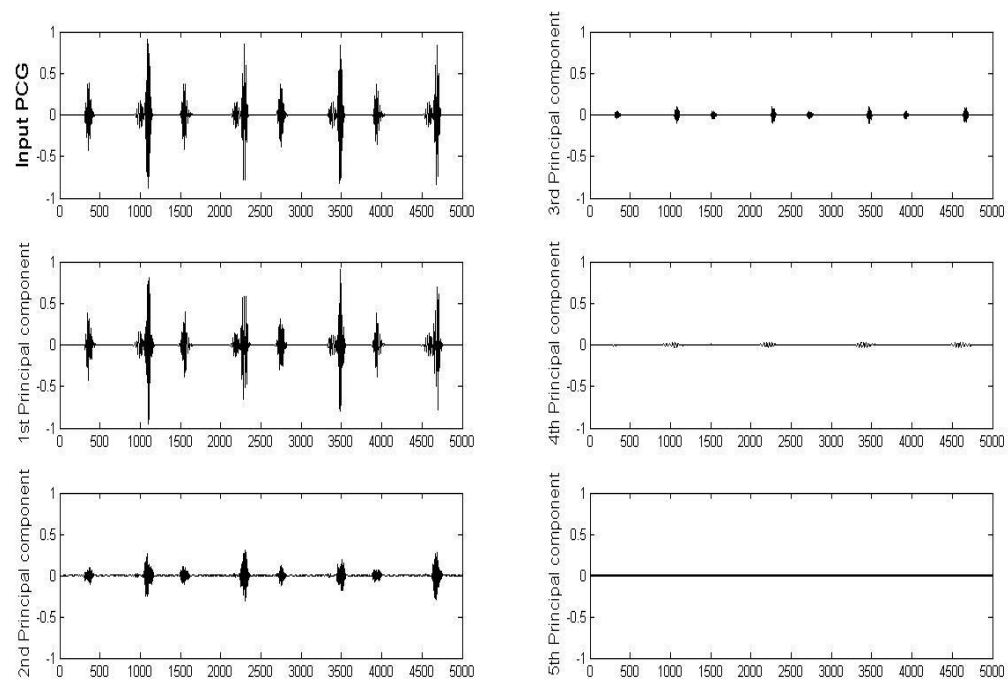
The prominence of this section is to obtain the PCs which extracts the primary components. For this reason pathological PCG features are projected onto the PCs and observed which is shown in figures below (4.28 to 4.36). This ensures that the information captured by the higher order eigenvectors are relatively minute, which can be discarded without any significant loss of information.



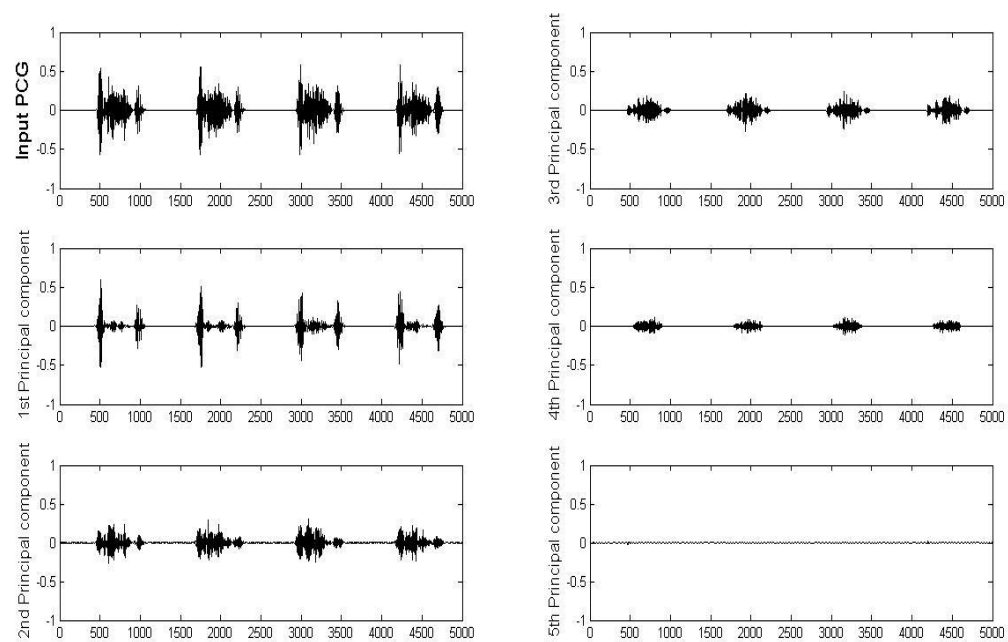
**Fig 4.28. Healthy HS signal projected on principal components.**



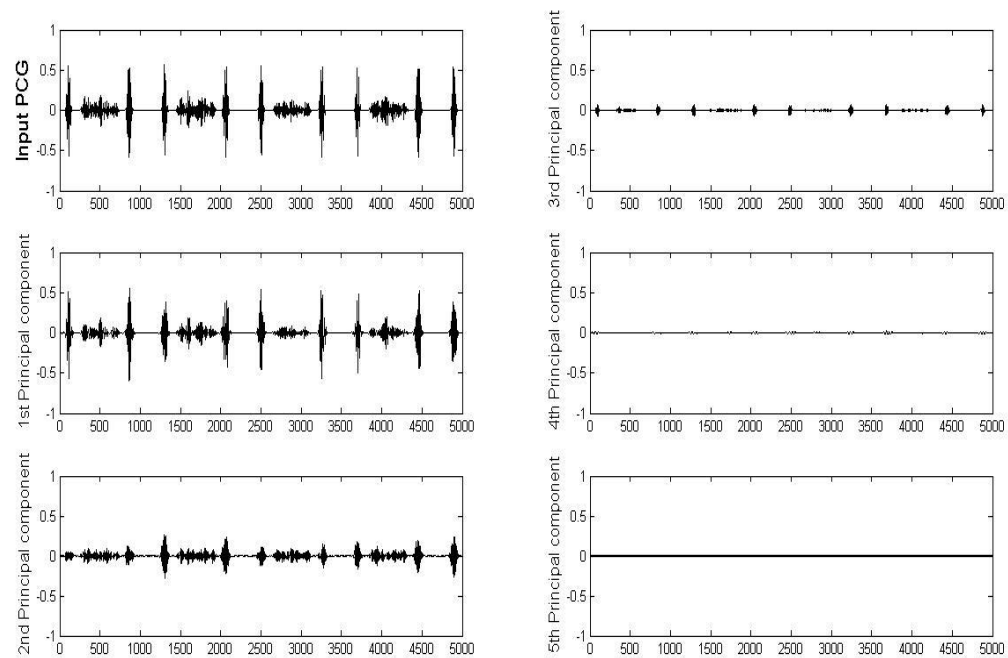
**Fig 4.29. 3<sup>rd</sup> HS signal projected on principal components.**



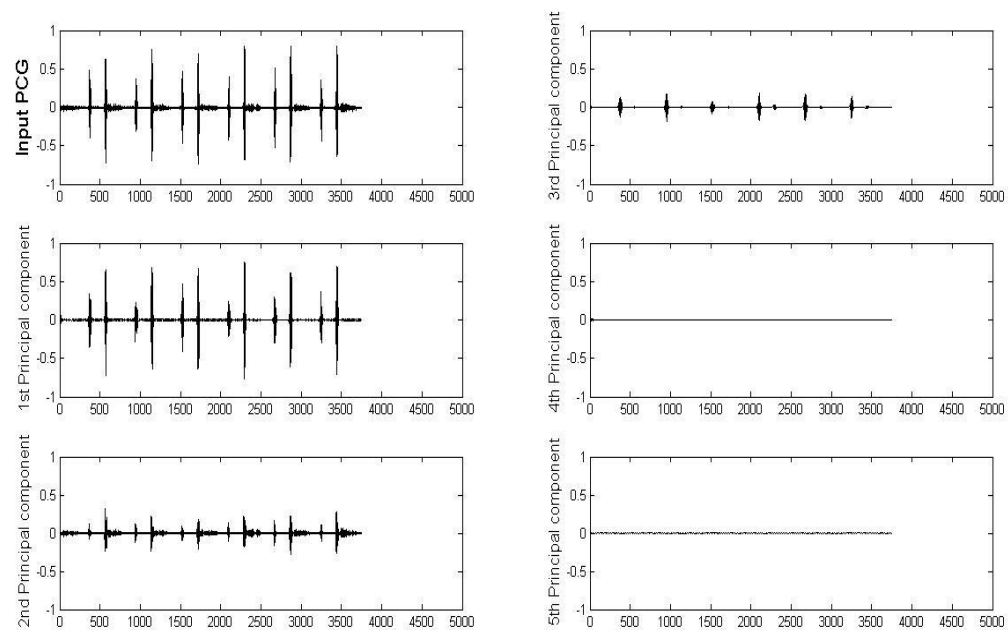
**Fig 4.30. 4<sup>th</sup> HS signal projected on principal components.**



**Fig 4.31. Aortic stenosis signal projected on principal components.**

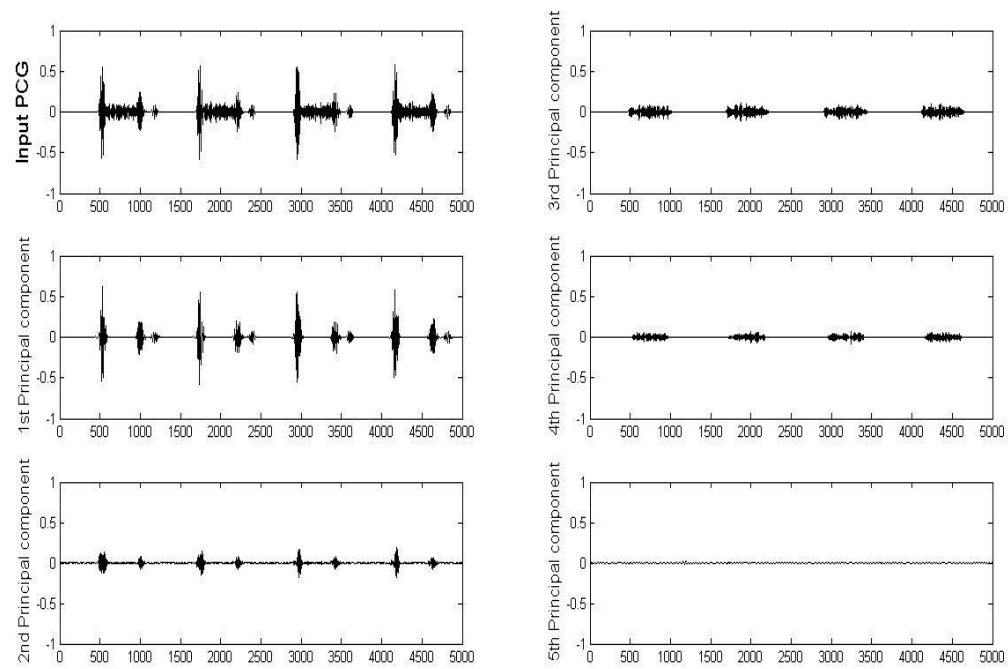


**Fig 4.32. Mitral stenosis signal projected on principal components.**

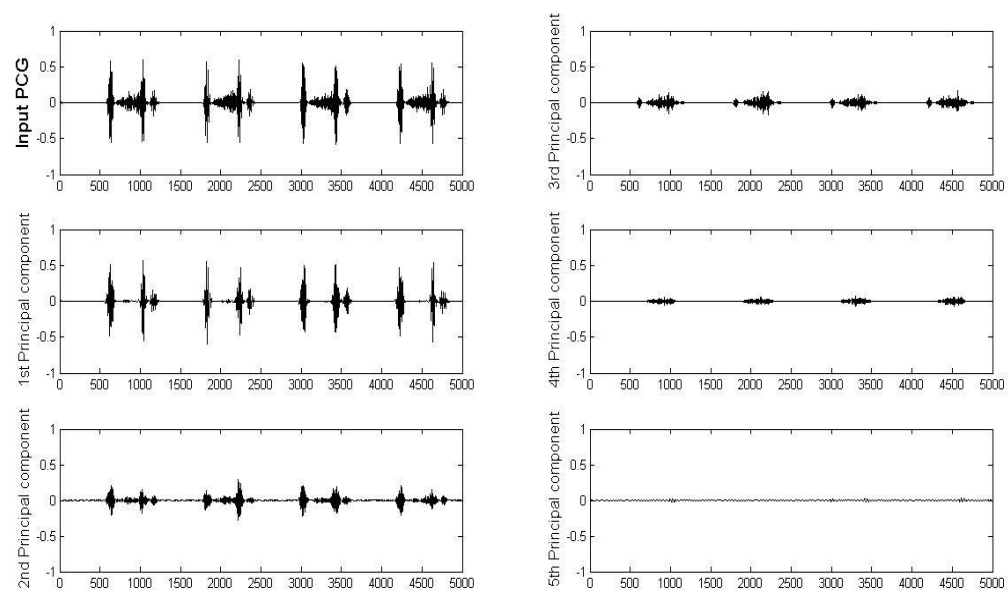


**Fig 4.33. Aortic regurgitation signal projected on principal components.**

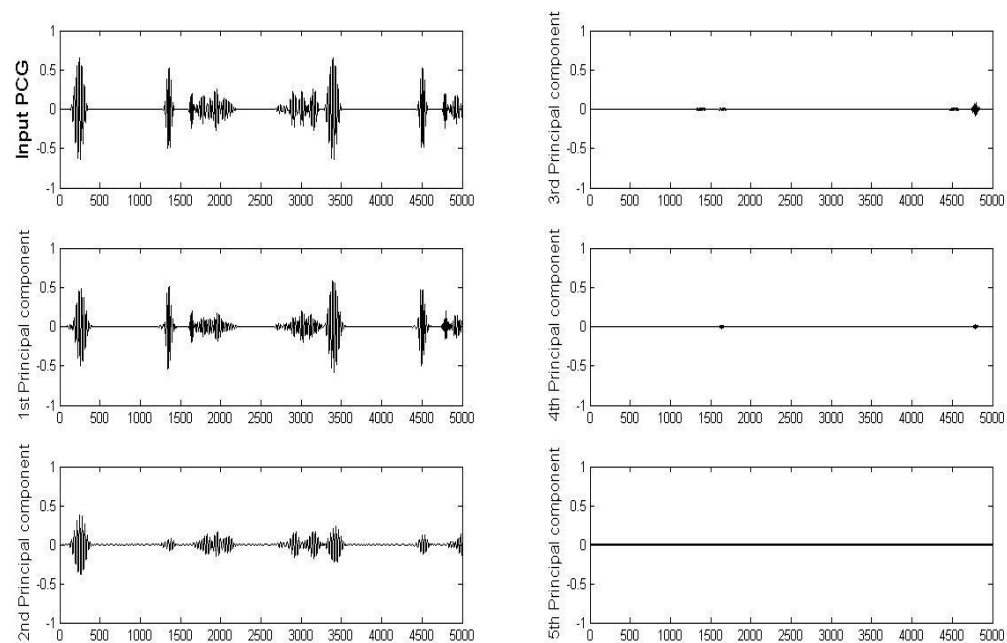




**Fig 4.34. Mitral regurgitation signal projected on principal components.**



**Fig 4.35. Pulmonic stenosis signal projected on principal components.**



**Fig 4.36. Tricuspid stenosis signal projected on principal components.**

**Table 1: Summary of the principal component analysis**

Heart sound	Level(s) reflecting S1	Level(s) reflecting S2	Levels reflecting murmur/extra component
Normal	1,2,3	1,2,3	--
3 <sup>rd</sup> HS	1,2	1,2	1,3
4 <sup>th</sup> HS	1,2	1,2	1,3
Aortic stenosis	1,2	1,2	2,3,4
Aortic regurgitation	1,2	1,2	2,3
Mitral stenosis	1,2	1,2	1,2,3
Mitral regurgitation	1,2	1,2	1,3,4
Pulmonic stenosis	1,2	1,2	2,3,4
Tricuspid stenosis	1,2	1	1,2

The summary of the PCA analysis in table 1 shows that most of the primary components are concentrated in 1<sup>st</sup> and 2<sup>nd</sup> PCs and murmurs are concentrated in all 1, 2, 3 and 4 PCs. From the observations of the above figures, the primary components although concentrates in both 1<sup>st</sup> and 2<sup>nd</sup> PCs, their most of the energy/information content is present in 1<sup>st</sup> PC only. In the same way although the murmurs have their role in all the 4 PCs, their most energy/information content is seen in 2<sup>nd</sup> and 3<sup>rd</sup> Pcs only. As the aim of this study is only to segment and identify primary components, the 1<sup>st</sup> PC which has maximum information content of primary components is chosen for further analysis and the remaining PCs are neglected.

#### 4.4 Separation of HS signal into Cardiac Cycles

Each HS signal is a combination of many cardiac cycles and separating the whole PCG signal into series of cardiac cycles is of clinical importance. After examining several pathological PCGs it is not obvious to conclude that segmentation techniques which uses amplitude thresholding works better for the cases of murmur dominated HSs and primary components diminished HSs. In order to combat these problems segmentation based on cardiac cycle is proposed in this study. Each cardiac cycle consists of S1, systole, S2 and diastole. In order to divide the entire HS signal into combination of these four phases, a well-defined process which can be capable of picking exact boundary positions is prerequisite. So an algorithm based on statistical analysis is proposed to gratify the above conditions, which is called as a splitting algorithm. The algorithm constitutes of two important variance parameters, global variance and local variance. According to the algorithm, the variances of the raw PCG signal and the 1<sup>st</sup> PC of PCA analysed PCG signal are the global variances and the variance of each windowed segment of the 1<sup>st</sup> PC of the PCA analysed HS signal is the local variance. Each local variance is compared with the global variances which acts as thresholds and accordingly further processing is computed. The entire algorithm is assembled in the form of flow chart which is shown in figures 4.37 & 4.38. Here each cardiac cycle will have one start position and one end position. Variances are represented in the form of  $\sigma_{(.)}$  where (.) represents corresponding signal parameter.  $S_n$  is the PCG signal, where n is the n<sup>th</sup> sample of the PCG signal,  $P_l$  is the 1<sup>st</sup> PC of the PCA analysed HS signal, where l is the l<sup>th</sup> sample of the signal. N is the length of the raw HS signal, and L is the length of

the 1<sup>st</sup> PC of the PCA analysed HS signal. In this algorithm, firstly, procedure for finding the start position of the very 1<sup>st</sup> cardiac cycle is carried followed by the search for the corresponding end position of the cycle. The end position is ensured by a special condition which depends on the sampling rate ( $f_s$ ) and the average heart rate (*avgrate*) possibility for an abnormal person.

$$T_L = f_s \times \text{avgrate} \quad \text{where, } f_s = 1575 \text{ samples per second.}$$

Here the variable ' $T_L$ ' denotes the lower limit of the average cardiac cycle. This value is not particular to any individual but in general it is approximately constant. For this study the ' $T_L$ ' is taken as 100beats per minute (1 beat per 0.6 second). Once the end position is obtained, the next start position can be written as the position next to the corresponding end position and the algorithm continues for the search of next end position. The repetition process continues until the length becomes equal to L – window size (W).

### Flow diagram for finding the start and end positions of the cardiac cycles

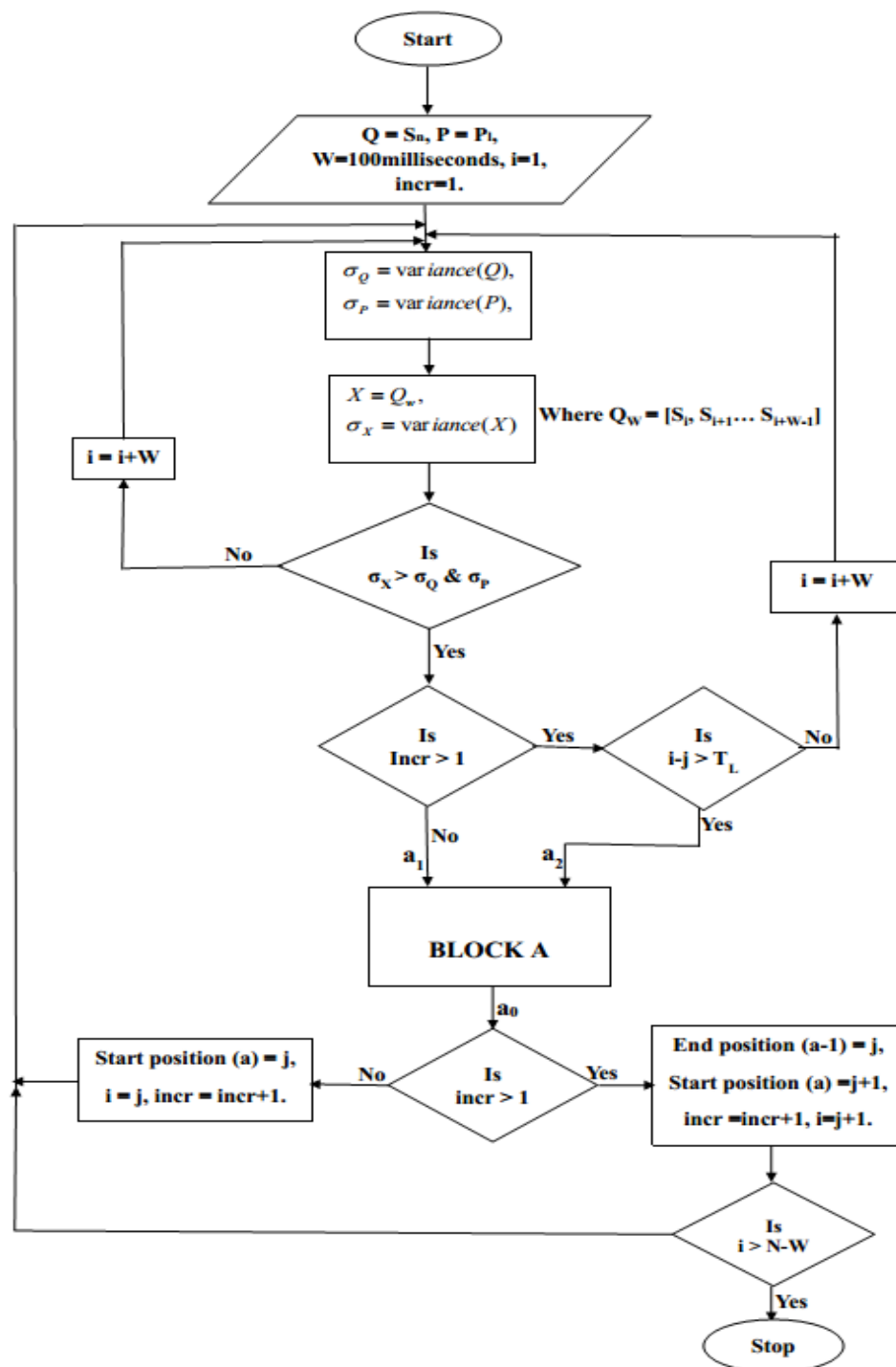
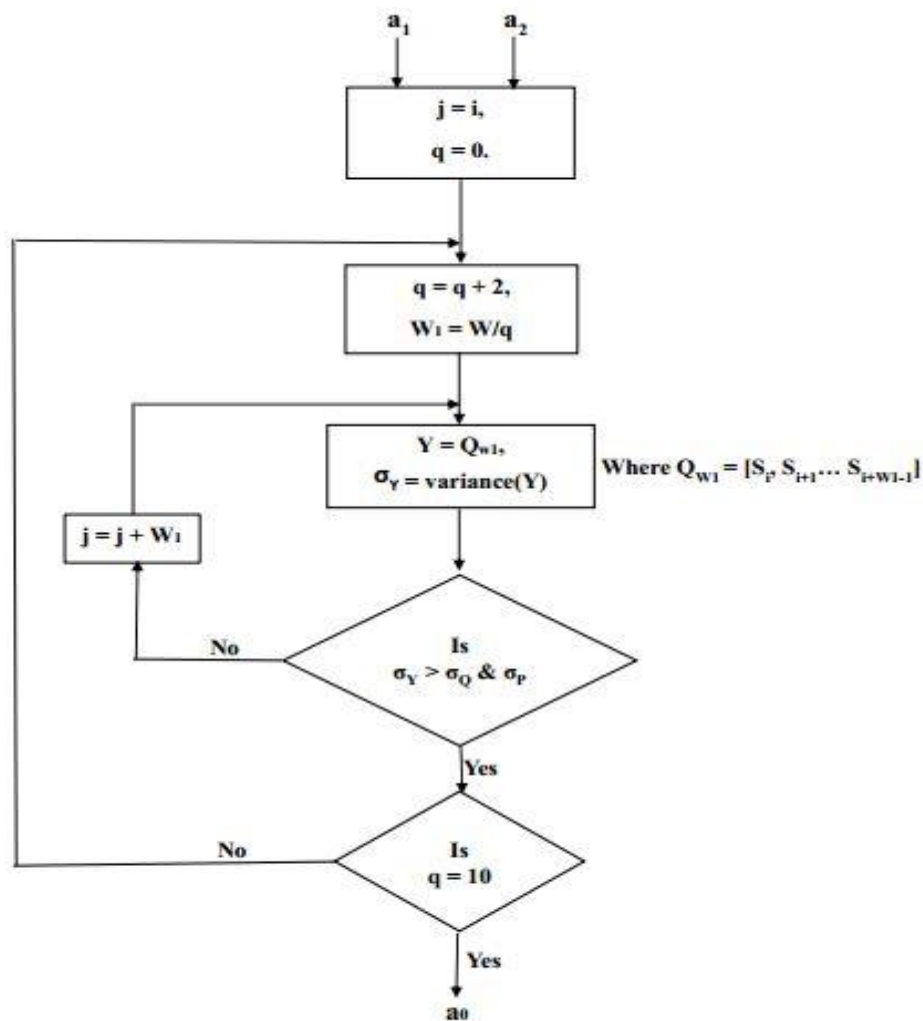


Fig 4.37 Flow diagram for finding start and end positions of cardiac cycles.

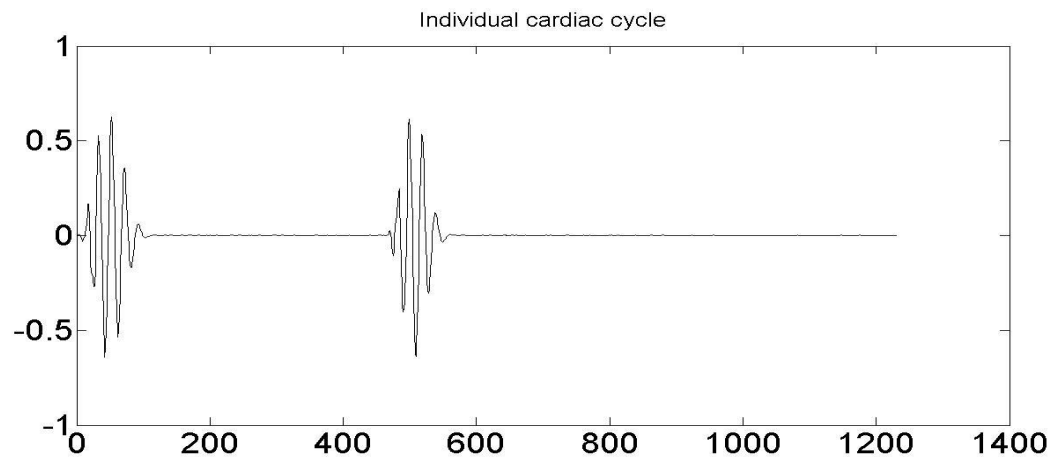
### Flow diagram for Block A



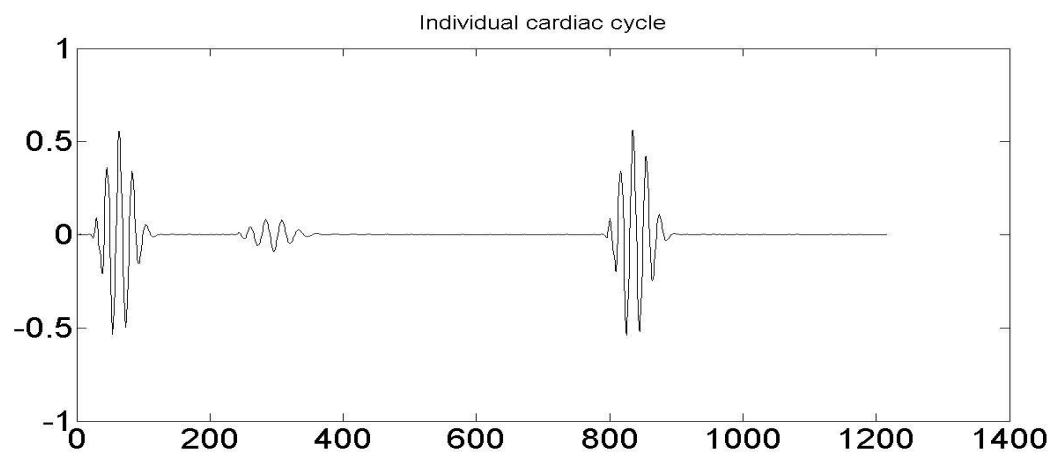
**Fig 4.38 Flow diagram for Block A in fig 4.37.**

The starting position and ending position of the cardiac cycle are recorded as references for further analysis. In this algorithm, the repetition process for better boundary detection is limited to  $q=10$  (i.e. 5 iterations) because of the limitation that, if the algorithm goes for further reduction there may be a chance of getting unnecessary components as the start/end position of the cardiac

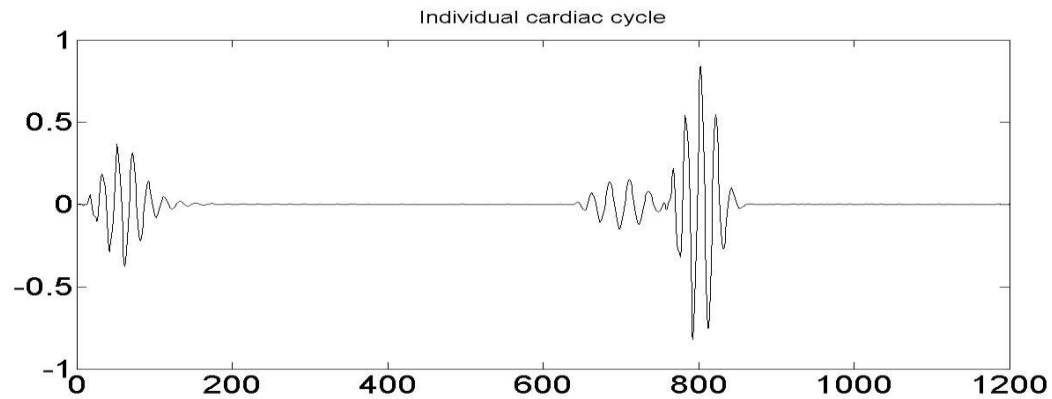
cycle which must not be. So it is restricted to  $q=10$  which has a probability of error as  $1/9$ . The individual cardiac cycle for different PCG signals is shown below.



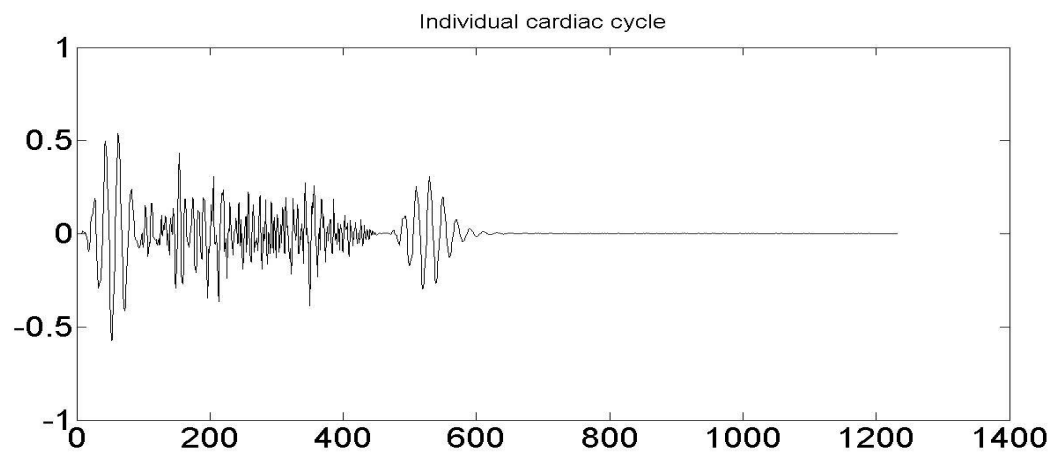
**Fig 4.39. Individual cardiac cycle for person with healthy HS signal.**



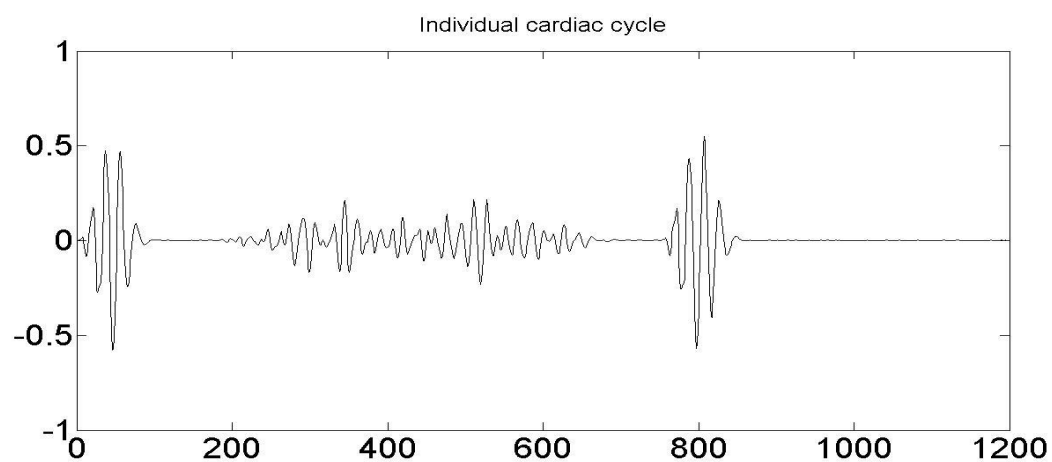
**Fig 4.40. Individual cardiac cycle for patient with 3<sup>rd</sup> HS signal.**



**Fig 4.41. Individual cardiac cycle for patient with 4<sup>th</sup> HS signal.**

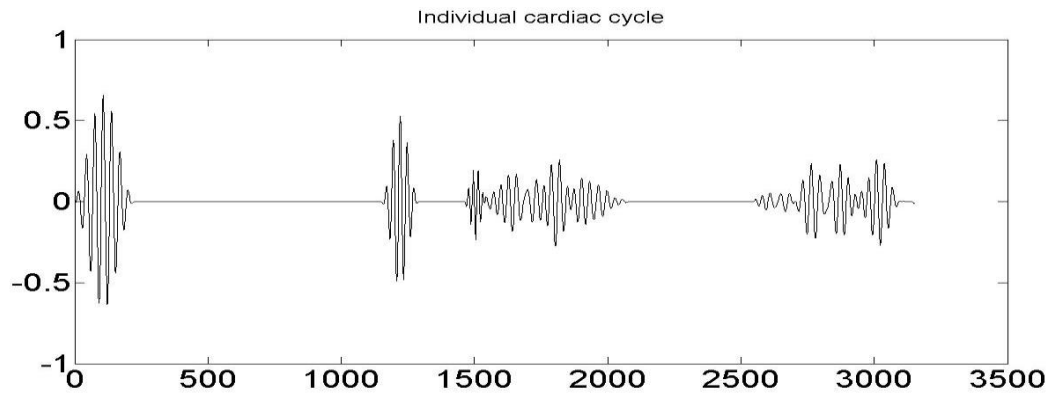


**Fig 4.42. Individual cardiac cycle for patient with aortic stenosis.**



**Fig 4.43. Individual cardiac cycle for patient with mitral stenosis.**

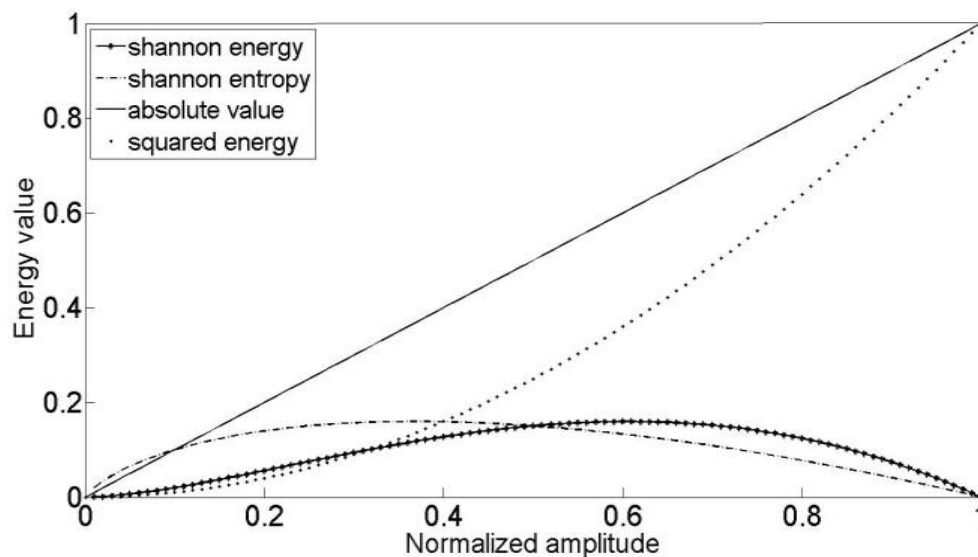




**Fig 4.44. Individual cardiac cycle for patient with tricuspid stenosis.**

## 4.5 Envelope extraction of the featured signal

The segmentation of the primary components depends on the energy as well as the positions of the featured signal. There are various methods for calculating the energy and finding their positions in a signal. The relationship between the energy amplitude and the normalized magnitudes are shown for four different methods. They are absolute value, squared energy, Shannon entropy, and Shannon energy.



**Fig 4.45. Comparison of different envelope methods.**

The absolute value weighs all intensities in a signal equally. The squared energy obscures the low intensity values while increasing the high intensities exponentially. The Shannon entropy magnifies the energy levels from low to medium and diminishes the energy levels from medium to high. The Shannon energy magnifies the medium intensity values while diminishing the high and low intensity values which can be shown in fig 4.37. From the observations, we have chosen to use Shannon energy for its property of attenuating the effects of low energy noises. The Shannon energy is calculated for the short segments of 40millisecond window size with 50% overlapping.

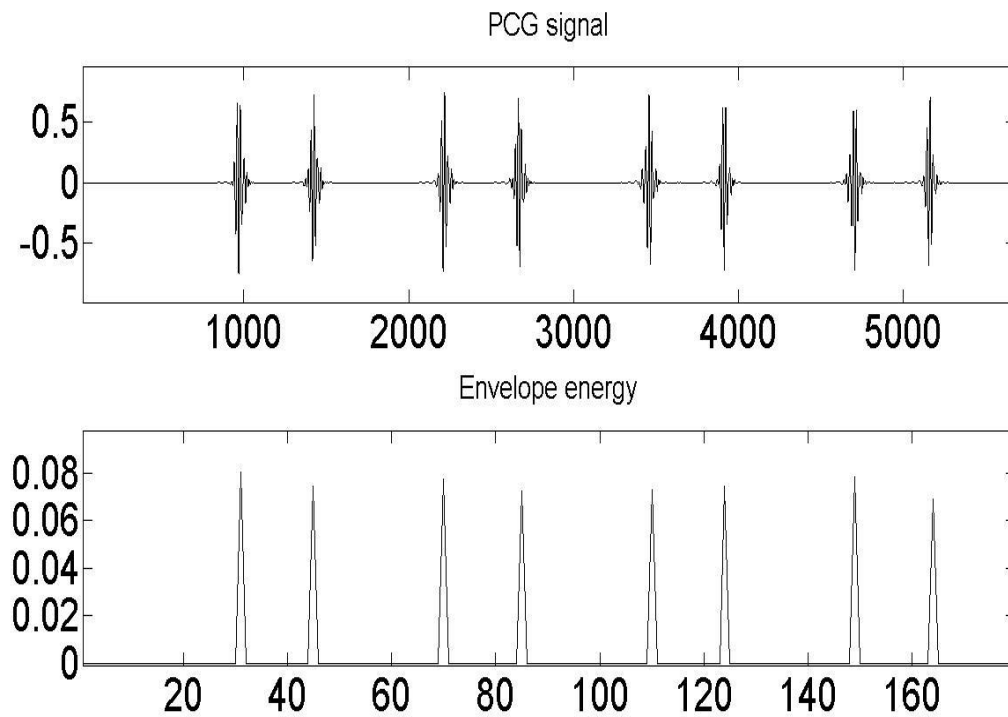
The Shannon energy is calculated using following equation:

$$E = -\frac{1}{N_{seg}} \sum_{i=1}^{N_{seg}} P^2(i) * \log(P^2(i)) \quad (4.6)$$

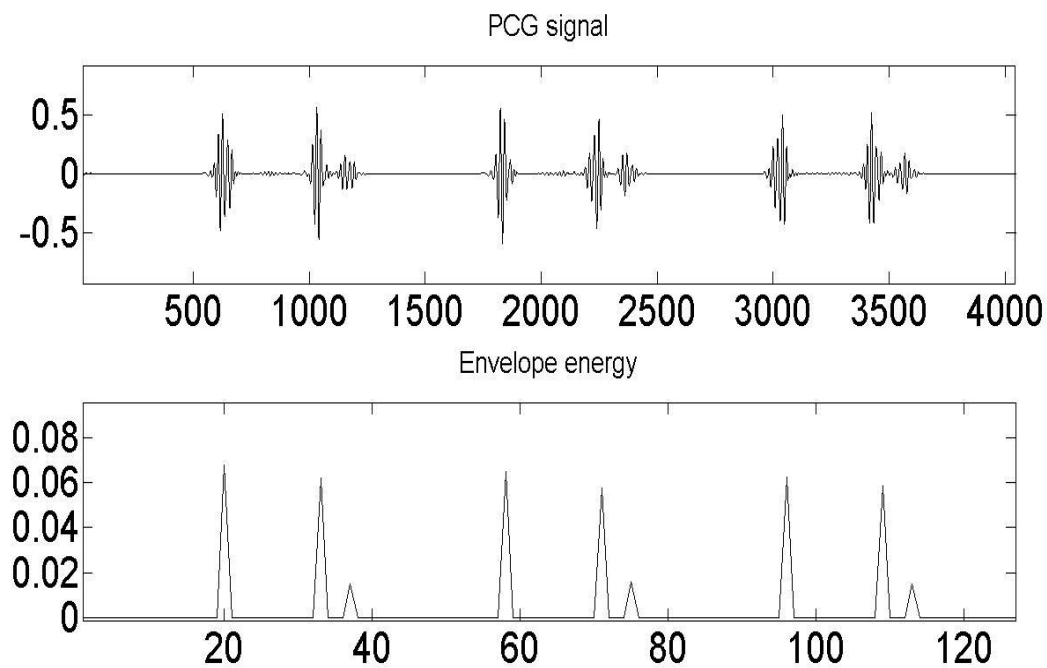
Where

$N_{seg}$  is the number of samples in the 40millisecond segment.

The positions of the energy levels captured by the Shannon energy which are shown in figures below are stored for further analysis.



**Fig 4.46. Extracted envelope energy for healthy HS.**



**Fig 4.47. Extracted envelope energy for patient with pulmonic stenosis.**

## 4.6 Segmentation of primary components

Cardiac anatomy states that the location of occurrence of the murmurs depends on the type of pathology, and the intensity level of the murmur depends on the position of auscultation. So it is unlikely to conclude that every pathology has a specific type of murmur at specific location. To combat this problem first we should segment the stationary components which are common for all pathologies. These stationary components are called primary components or components of interest (S1 and S2). Primary components are the components which has a specific pattern and a specific distribution [15]. Segmentation of primary components is done using the records which are stored from previous two sections. The records include cardiac cycle positions and envelope positions.

### 4.6.1 Missing peak detection

During some pathological conditions there may be a chance that the intensity level of either S1 or S2 get buried due to valve dysfunctionality. So it is necessary to detect those peaks initially. For this the difference between the envelope positions are calculated and compared with the cardiac cycle duration of that particular cardiac event. As each cardiac cycle consists of S1, systole, S2 and diastolic phases, it is mandatory that the difference between consecutive envelope positions should always be less than the cardiac duration. If this condition is not satisfied, it clearly states that one of the primary component is missing and further process is done to extract the missing peak. In this process only missing components are extracted.

### 4.6.2 Detection of S1 and S2 from murmured PCG signal

The main aim of this work is to separate primary components from murmur/noise corrupted HS signal. In this analysis along with the stored records from envelope extraction and cardiac cycle separation, two additional references are taken i.e. difference between consecutive envelopes and time period of the individual energy components. Using these four data sets and two thresholds which are derived from above data sets, primary components are segmented.

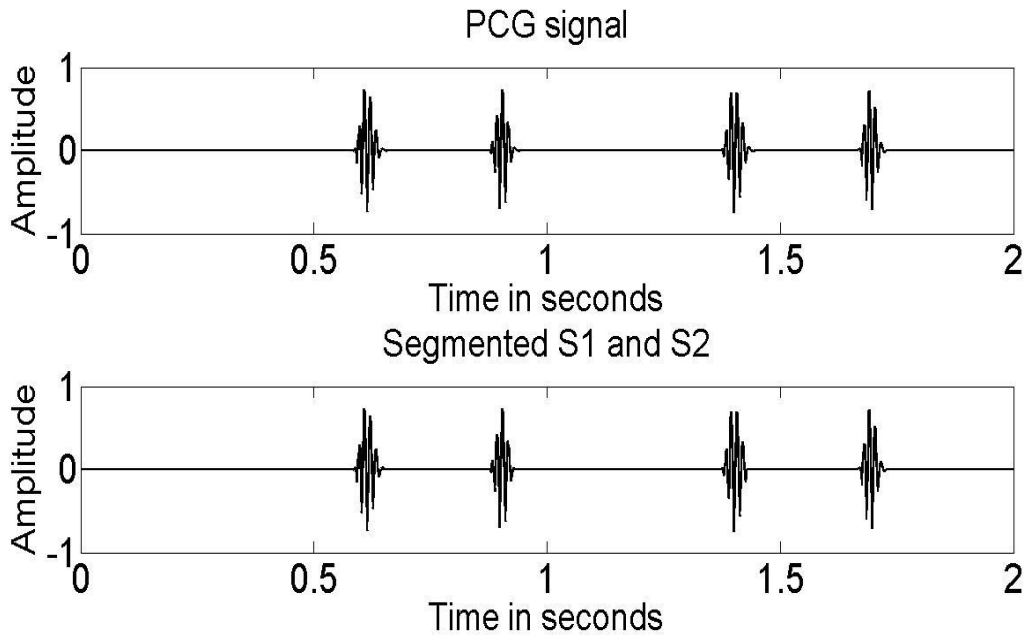
Two thresholds are calculated as follows:

$$T1 = \frac{p(i) + ((p(i+1) - p(i))/3)}{T_j} \quad (4.7)$$

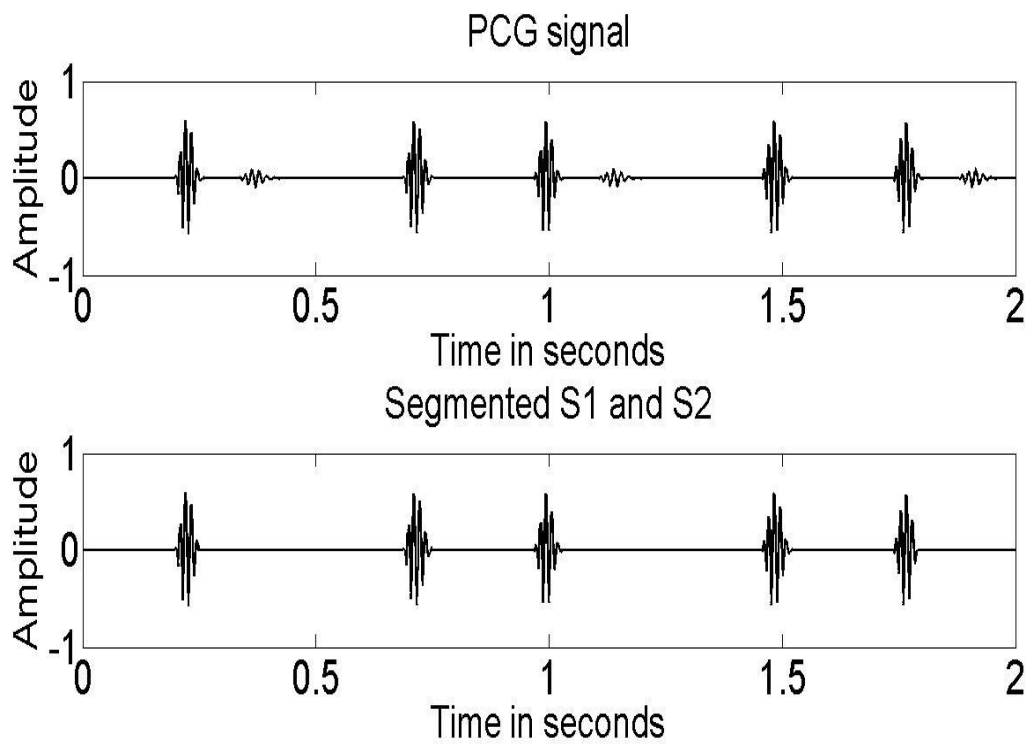
$$T2 = \frac{p(i) + ((p(i+1) - p(i))/2)}{T_j} \quad (4.8)$$

Where  $i=1,2,\dots, n$ ,  $n$ =number of cardiac cycles,  $p(i)$  is the position of the HS envelope,  $T_j$  is the time period of the cardiac cycle at  $j=1,2,\dots,n$ .

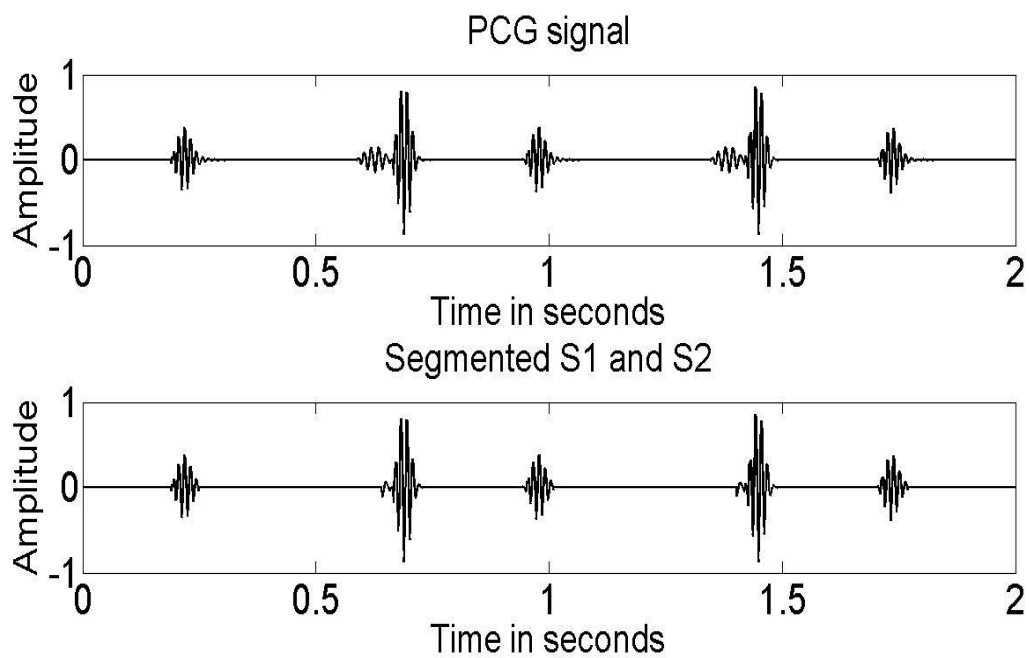
The segmented primary components for different pathologies along with healthy HS is shown in below figures. The algorithm is also able to segment S3 and S4 components by considering them as unnecessary components. After segmentation some of the pathologies which has murmurs mixed with primary components leaves tails at the edges of the primary components. This is because of the inability of Shannon energy to extract exact boundary position of the HS signals.



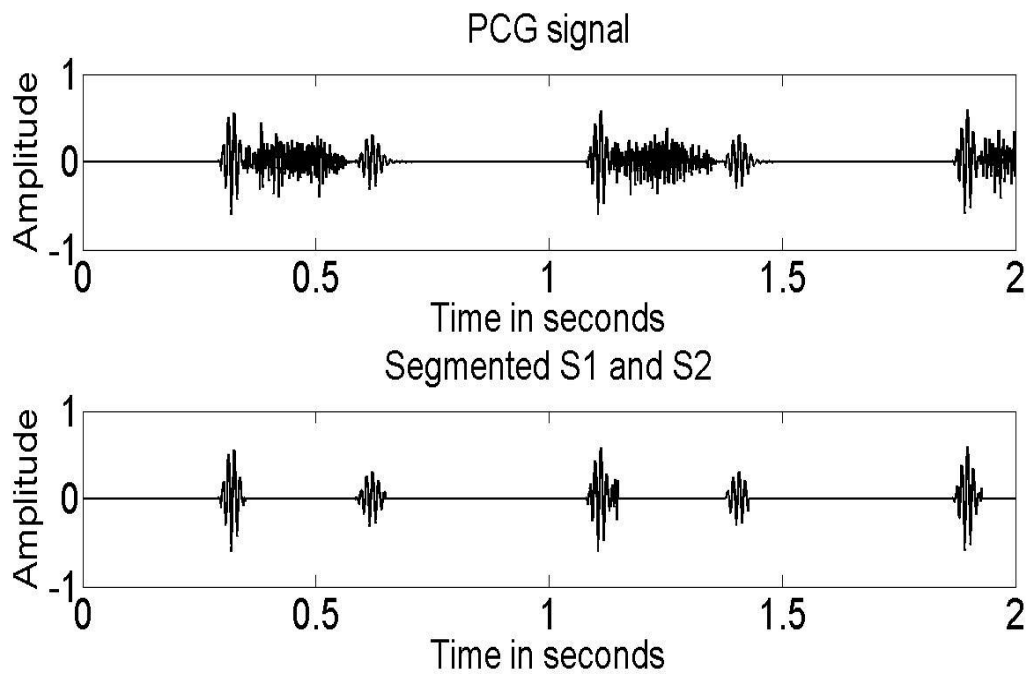
**4.48. S1 and S2 detected for healthy person.**



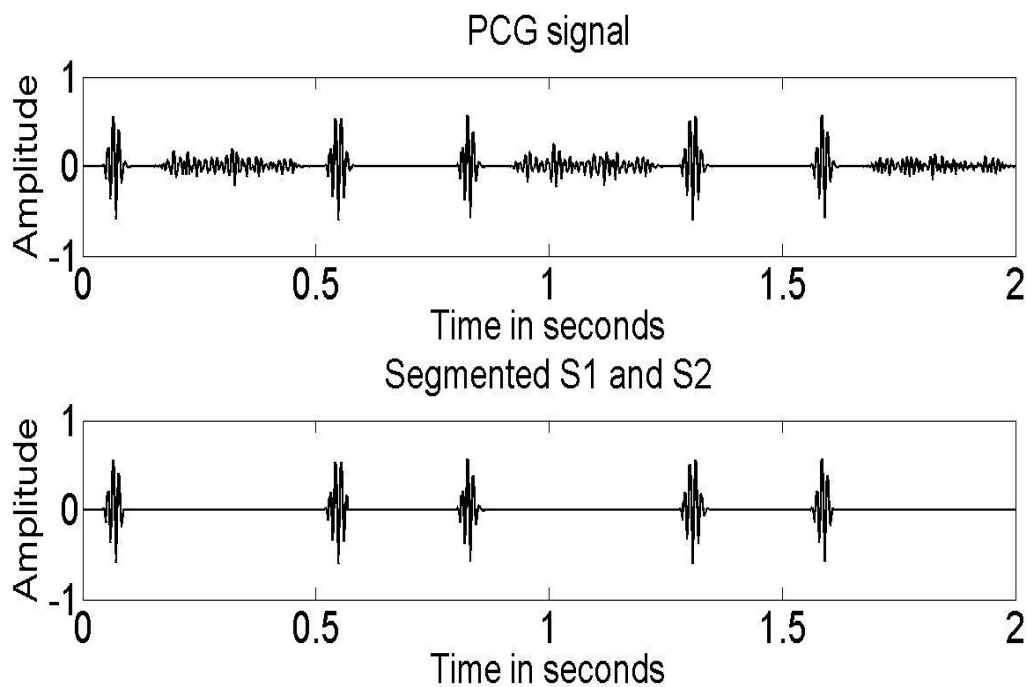
**4.49. S1 and S2 detected for patient with 3<sup>rd</sup> HS.**



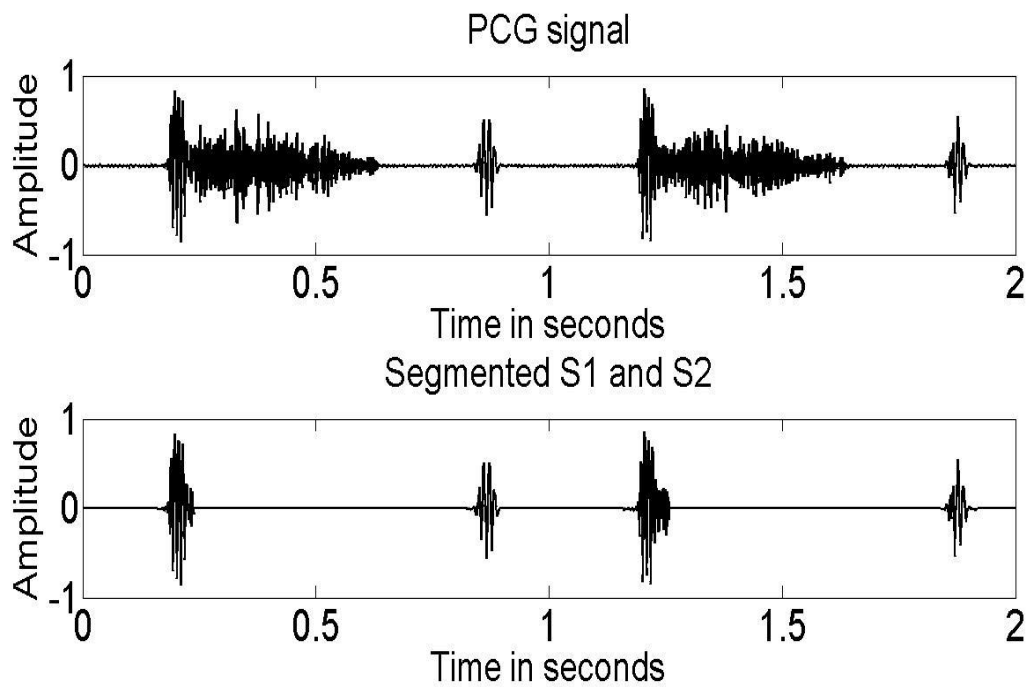
**4.50. S1 and S2 detected for patient with 4<sup>th</sup> HS.**



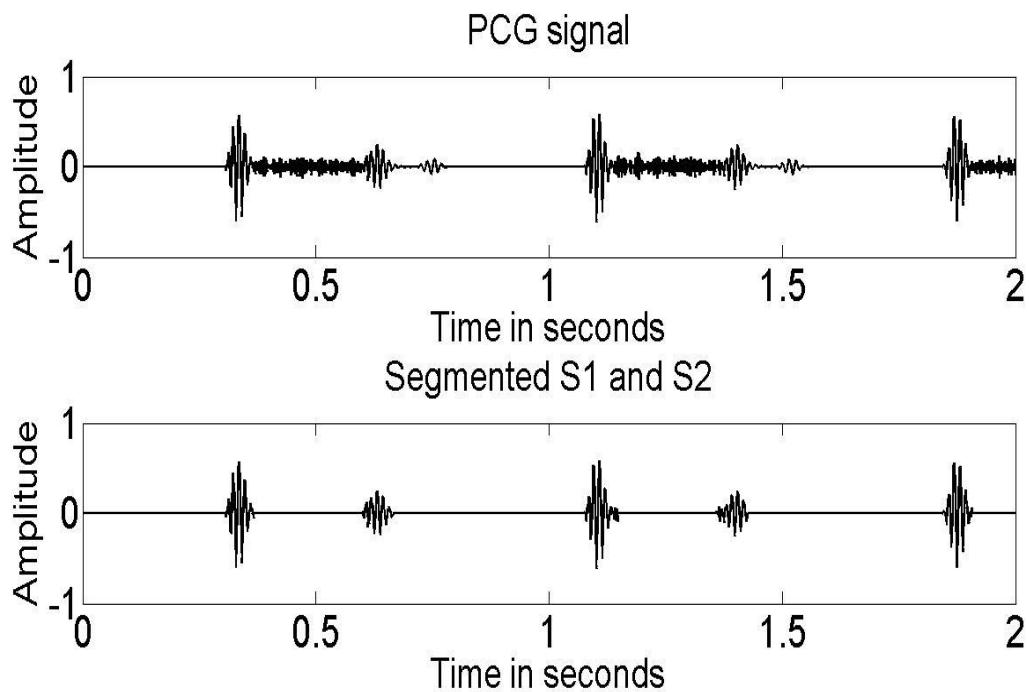
**4.51. S1 and S2 detected for patient with aortic stenosis.**



**4.52. S1 and S2 detected for patient with mitral stenosis.**

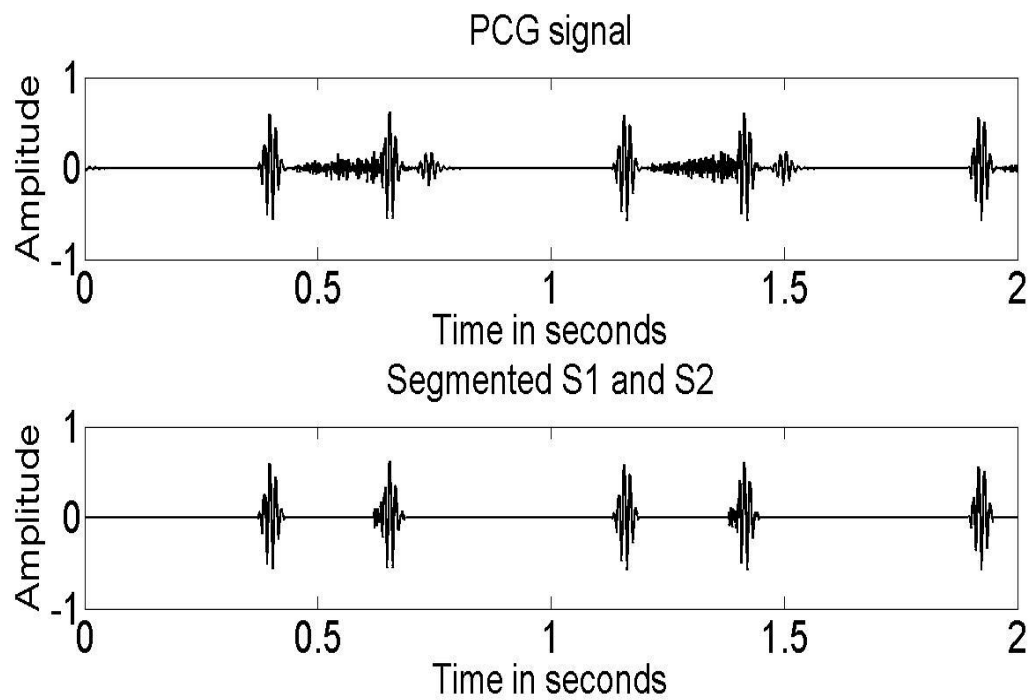


**4.53. S1 and S2 detected for patient with aortic regurgitation.**



**4.54. S1 and S2 detected for patient with mitral regurgitation.**





**4.55. S1 and S2 detected for patient with pulmonic stenosis.**

## CHAPTER 5

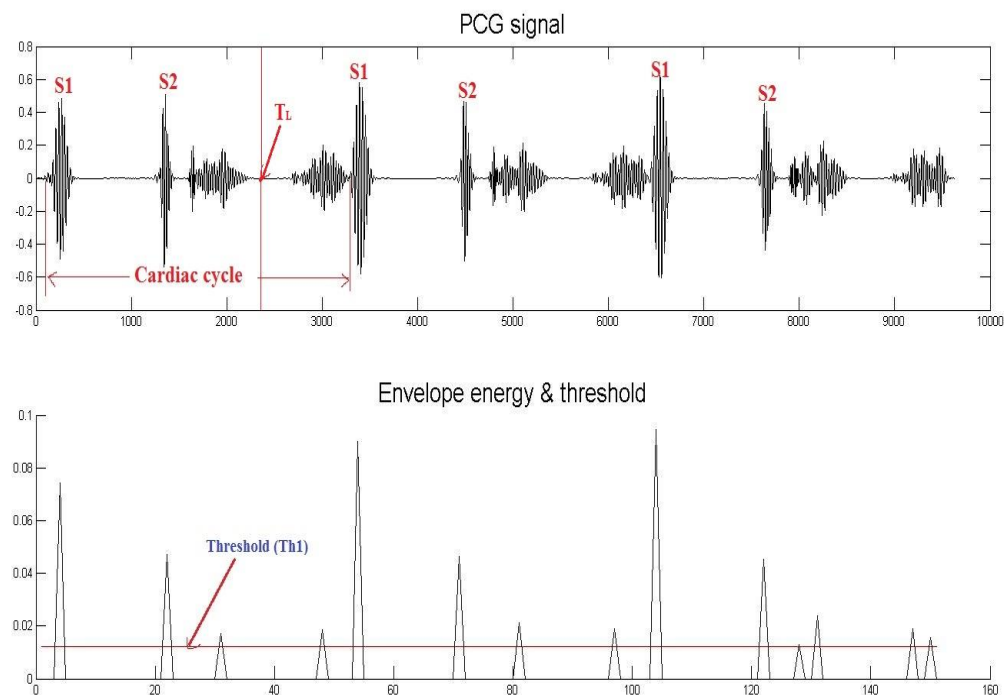
# PERFORMANCE ANALYSIS

Heart sounds are non-stationary and exhibits sudden frequency transients from one cardiac cycle to another cardiac cycle. Many researchers describe that the normal heart rate as regular, but more careful analysis reveals that healthy individuals have heart rate that fluctuates considerably even at rest [15]. This depicts the typical nature of the PCG for any analysis. Despite of any pathology each cardiac event has two components (S1 and S2) as common and is quite stationary. The main focus of this study is to highlight the stationary components which we call them as primary components (S1 and S2).

## 5.1. Performance Analysis

The performance analysis of this study is very difficult to evaluate. But when observing all pathologies, the proposed technique doesn't work quite well in cases where the lower limit for average cardiac period ( $T_L$ ) condition fails to pick the exact cardiac cycle boundaries. This is because of the presence of some unnecessary components which has valid energy (i.e.  $>$  global threshold) between the lower limit point and the actual cardiac end point. This problem arises in tricuspid stenosis which is shown in below figure 5.1. In this figure, the murmur pertains at the end of the cardiac cycle where the average lower limit of the cardiac cycle ( $T_L$ ) is crossed. As in this case, the murmur energy is greater than threshold; the algorithm takes that murmur as valid component and treats as the ending position of the cardiac cycle which gives false representation for the cardiac cycles.

This problem can be eliminated by modelling the signal by using estimators. The primary components always have a stationary behaviour, so it has a constant frequency range from which the non-stationary components can be eliminated and make the algorithm still valid in these cases.



**Fig 5.1. Envelope energy and threshold level for tricuspid stenosis.**

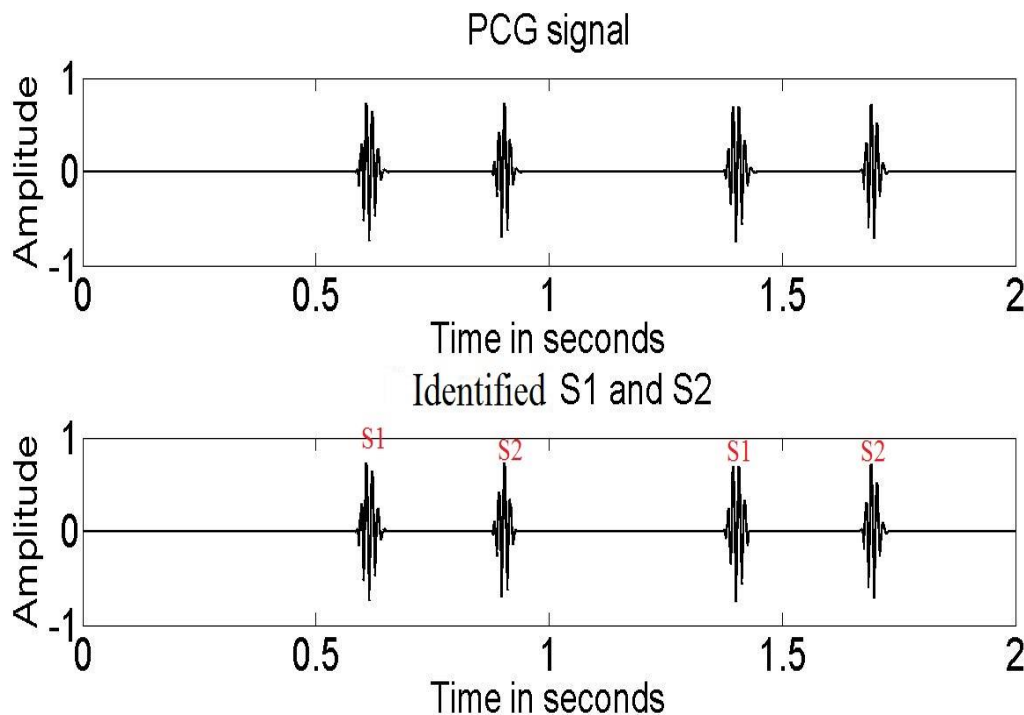
The identification of S1 and S2 is done from the subjective knowledge perspective. The performance analysis is computed assuming that the PCG signal starts with either S1 or S2 and also acquisition is made accordingly. Table 2, shows the results obtained which gives 98.32% accuracy levels in identifying S1 and S2. The error is due to above mentioned lower limit problem during cardiac separation of HS signals.

**Table 2. Summary of segmentation algorithm**

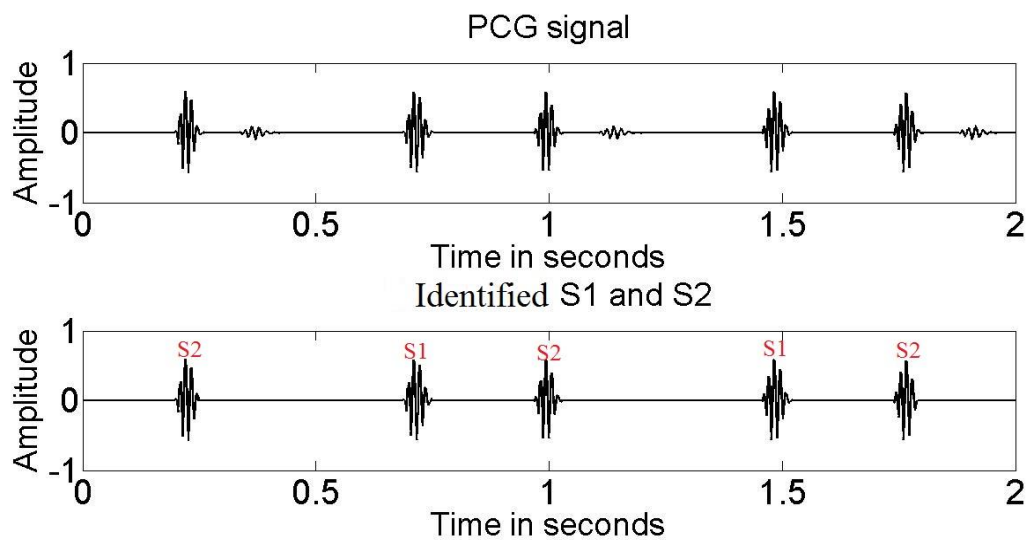
HS	correct	Incorrect	total	Percentage (%)
Normal	89	0	89	100
Abnormal	382	8	390	97.94
Total cycles	471	8	479	98.32

## 5.2. Identification of S1 and S2

In order to identify the type of pathology one must have the knowledge of the murmur location and the auscultation position. So to find the location of the murmur we need to identify which is S1 and which is S2. The identification is computed based on the following subjective facts: 1) the longest duration between two neighbouring peaks is the diastolic period. 2) The systolic period which is relatively constant compared to the diastolic period. Based on these two facts identification of S1 and S2 are computed. The below figures (5.2 – 5.9), resembles the identified S1 and S2 components from normal and pathological PCGs. By knowing the S1 and S2 positions, we can easily identify the position of occurrence of the murmurs there by the type of pathology (provided the auscultation position for the particular PCG is known).

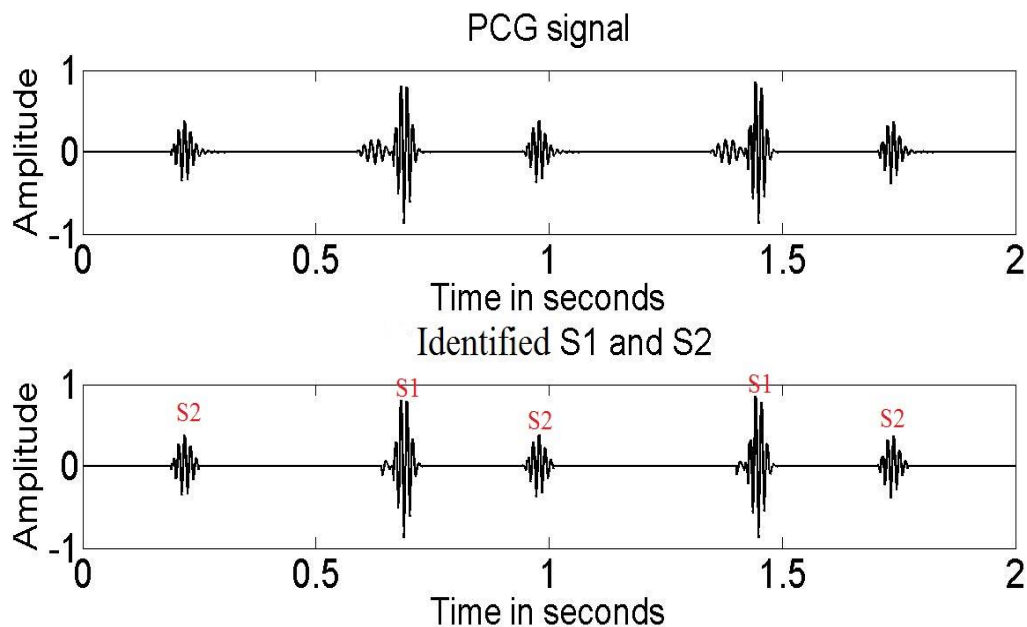


**Fig 5.2. Identified primary components after segmentation for healthy person.**



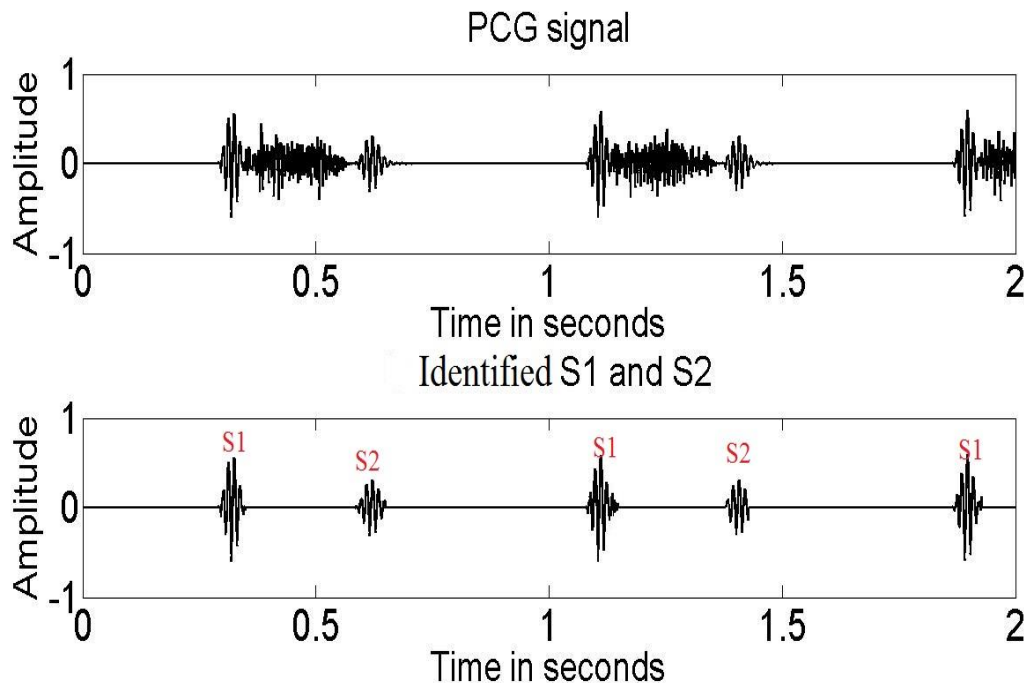
**Fig 5.3. Identified primary components after segmentation for 3<sup>rd</sup> HS patient.**

From the figure 5.3, we can conclude that the murmur/dysfunction occurs between S2 and S1 i.e. in diastolic phase and the position of it is near to S2 which has very low frequency and the auscultation is taken from apex position. This data resembles the extra component as S3 i.e. 3<sup>rd</sup> HS.



**Fig 5.4. Identified primary components after segmentation for 4<sup>th</sup> HS patient.**

The figure 5.4, shows the extra component to be in the diastolic phase (i.e. between S2 and S1) and it is closer to S1 which is very low frequency and auscultated at apex position. This data resembles the extra sound component as S4 i.e. 4<sup>th</sup> HS.

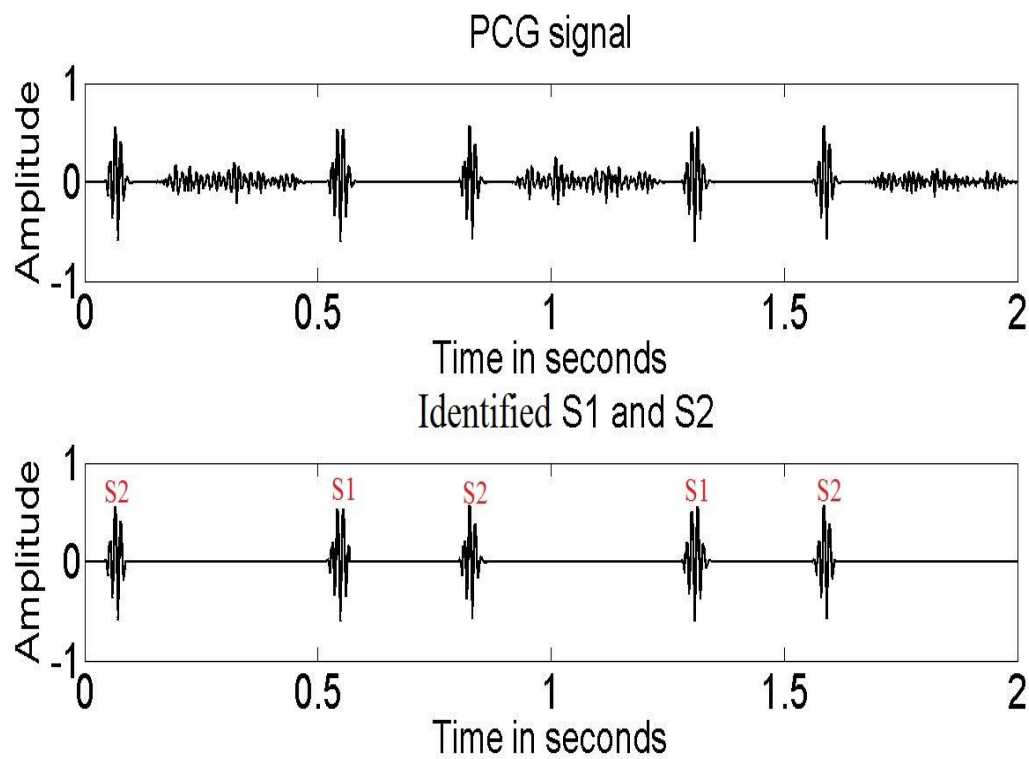


**Fig 5.5. Identified primary components after segmentation for aortic stenosis patient.**

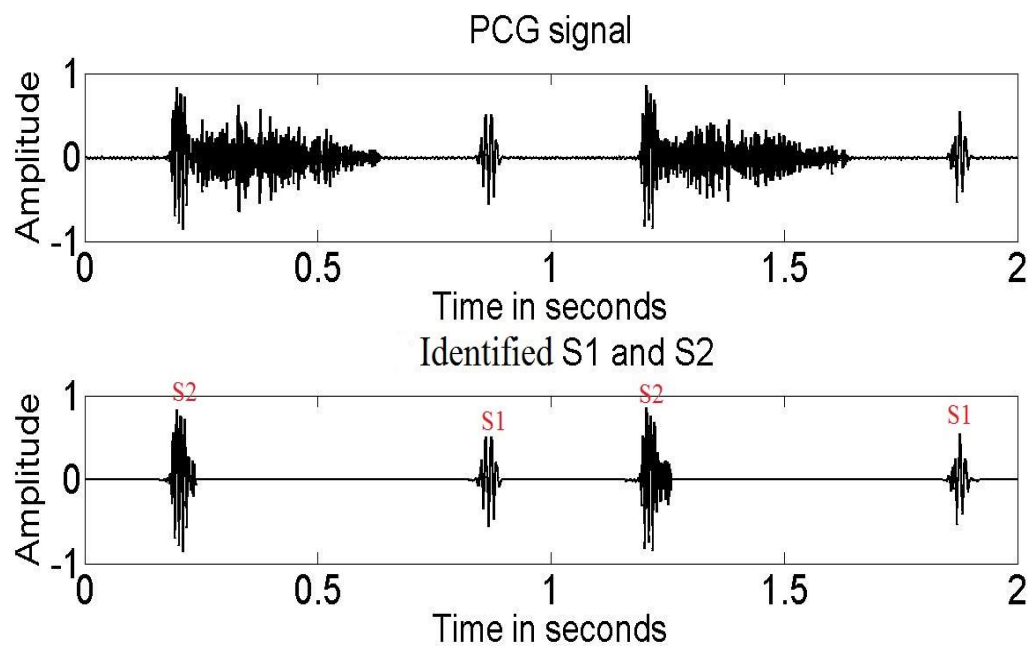
The figure 5.5, shows the extra component to be in the systolic phase (i.e. between S2 and S1) which is distributed throughout the systole and has a diamond shape structure. The auscultation is taken at apex position. This data resembles the extra sound component as a murmur due to its distribution and the pathology may be aortic stenosis.

From figure 5.6, a murmur between S2 and S1 prevails and looks like it has mid diastolic rumbling murmur which is auscultated at apex and sternal border using bell of stethoscope. This kind of murmur resembles the cause of mitral stenosis.

Similarly figure 5.7, resembles a kind of murmur which in medical terminology called as decrescendo murmur between S2 and S1 i.e. diastolic phase. The auscultation position where it can be best heard is 2<sup>nd</sup> left intercostal space using diaphragm of the stethoscope and the pathology can be aortic regurgitation.

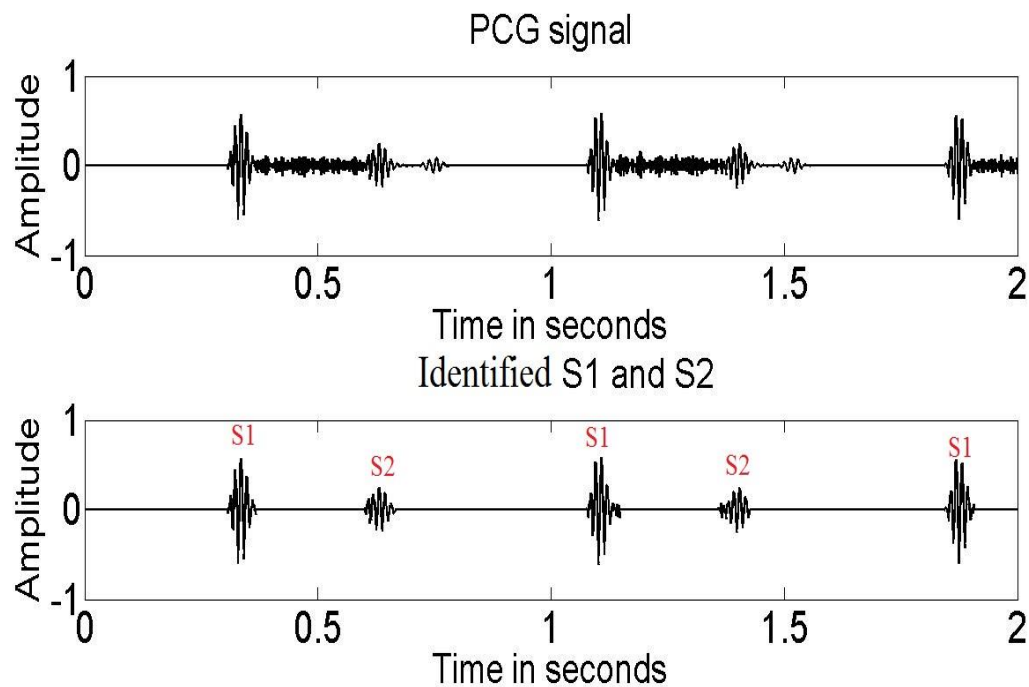


**Fig 5.6. Identified primary components after segmentation for mitral stenosis patient.**

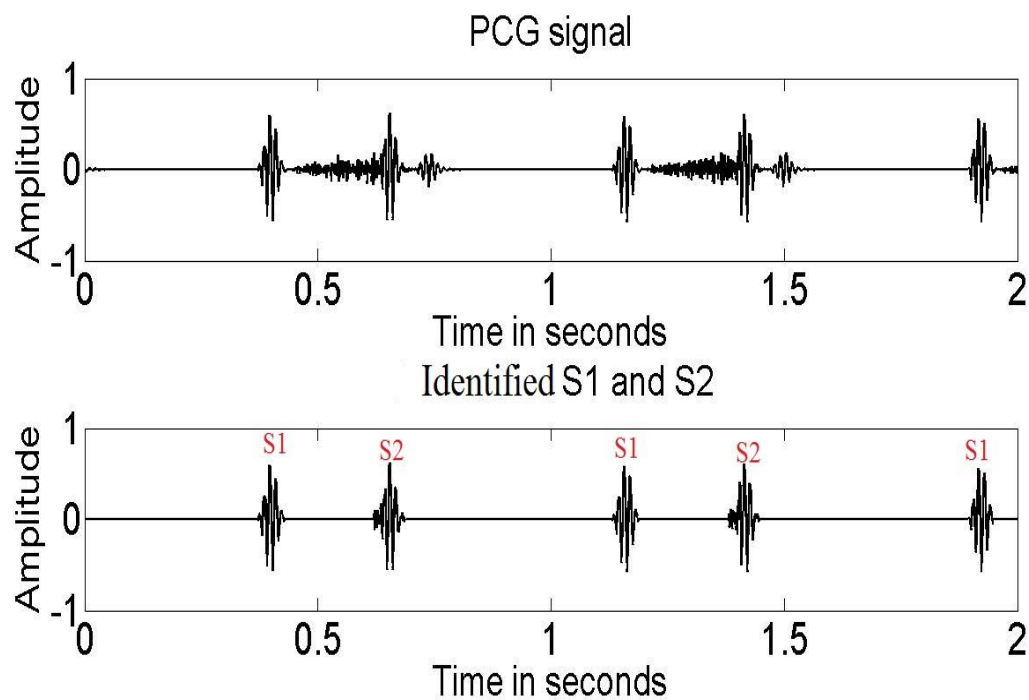


**Fig 5.7. Identified primary components after segmentation for aortic regurgitation patient.**





**Fig 5.8. Identified primary components after segmentation for mitral regurgitation patient.**



**Fig 5.9. Identified primary components after segmentation for pulmonic stenosis patient.**

Figure 5.8, shows a kind of murmur called as pan systolic murmur which occurs at systolic phase i.e. between S1 and S2. It is auscultated at the apex and across the pulmonary area. In this case an extra S3 component is also present which gives an interpretation that the pathology might be mitral regurgitation.

Figure 5.9, has a crescendo murmur at the systolic phase i.e. between S1 and S2. The auscultation position where the acquisition is done is 4<sup>th</sup> left intercostal space. It also has an extra S3 component and this kind of murmur pattern may resembles a kind of pathology called pulmonic stenosis.

## Conclusion

A segmentation algorithm which uses statistical analysis as a major tool for segmenting primary components from abnormal PCG is presented in this study. The study uses wavelets and principal component analysis for extracting the relevant features for processing segmentation algorithm. The peeling algorithm used to separate PCG signal into series of cardiac cycles signifies the importance and feasibility of statistical approach in phonocardiographic analysis. The algorithm gives 98.32% of accuracy in identifying the primary components from variety of pathologies. However, the error probability of 1/9, obtained during peeling algorithm doesn't concede much accuracy distraction. The presented study is simple and can be capable of picking up low energy components without any additional effort.

The identification of exact end positions of the cardiac cycle becomes difficult in some pathological conditions because of the propagation of murmur near to the end position. So further processing is required for exact boundary detection by using valid estimators.

## Dissemination

- [1] D Sandeep Vara Sankar, Lakshi Prosad Roy, “Principal Component Analysis (PCA) Approach to Segment Primary Components from Pathological Phonocardiogram”, *Proceedings of 2014 IEEE International Conference on Communication and Signal Processing*, APEC, Tamil Nadu, pp. 1023-1027, April 2014.

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